

I SEMANA DAS ENGENHARIAS DO INSTITUTO POLITÉCNICO

CONHECENDO O MAPLE

(Versão 13)

por

Germano Amaral Monerat
DMC/IPRJ/UERJ

I. O que é Maple?

Os sistemas de computação algébrica (Computer Algebraic Systems ou CAS), também conhecidos como sistemas de computação simbólica têm por objetivo a automatização de cálculos matemáticos em geral. Isto é especialmente útil quando tais cálculos envolvem um grande número de operações repetitivas e expressões de tamanho muito grande, em que o tempo necessário para realizá-las é muito extenso, e a probabilidade de erro humano durante a sua realização é muito alta.

Exemplo: Utilizando o comando *diff* do Maple, calcular a derivada de 20a. ordem da função $\sin(x e^x)$.

```
> diff(sin(x*exp(x)), x$20);
cos(x ex) (20 ex + x ex) + sin(x ex) (ex + x ex)20 - 1466593128000 cos(x ex) (ex
+ x ex) (2 ex + x ex)2 (3 ex + x ex)2 (5 ex + x ex) (4 ex + x ex)
- 733296564000 cos(x ex) (ex + x ex)2 (2 ex + x ex) (3 ex + x ex) (5 ex
+ x ex) (4 ex + x ex)2 - 139675536000 sin(x ex) (ex + x ex) (3 ex + x ex)2 (7 ex
+ x ex) (2 ex + x ex) (4 ex + x ex) - 209513304000 cos(x ex) (ex + x ex)2 (3 ex
+ x ex) (7 ex + x ex) (2 ex + x ex)2 (4 ex + x ex) + 733296564000 cos(x ex) (ex
+ x ex)4 (2 ex + x ex)2 (3 ex + x ex) (5 ex + x ex) (4 ex + x ex)
- 55870214400 cos(x ex) (ex + x ex)3 (3 ex + x ex) (7 ex + x ex) (5 ex + x ex) (2 ex
+ x ex) + 14108640 sin(x ex) (ex + x ex)6 (11 ex + x ex) (3 ex + x ex)
- 55426800 sin(x ex) (ex + x ex)4 (7 ex + x ex) (9 ex + x ex) + 5426400 sin(x ex) (ex
+ x ex) (3 ex + x ex)2 (13 ex + x ex) - 14108640 cos(x ex) (3 ex + x ex) (6 ex
+ x ex) (11 ex + x ex) - 8817900 sin(x ex) (ex + x ex)4 (12 ex + x ex) (4 ex + x ex)
+ 8139600 sin(x ex) (2 ex + x ex)2 (13 ex + x ex) (3 ex + x ex)
+ 8139600 cos(x ex) (ex + x ex) (2 ex + x ex)3 (13 ex + x ex)
```

$$\begin{aligned}
& + 1939938000 \sin(x e^x) (e^x + x e^x)^8 (3 e^x + x e^x)^4 - 4408950 \sin(x e^x) (e^x \\
& + x e^x)^{12} (4 e^x + x e^x)^2 + 290990700 \cos(x e^x) (e^x + x e^x)^2 (4 e^x + x e^x)^2 (10 e^x \\
& + x e^x) + 9820936125 \cos(x e^x) (2 e^x + x e^x)^8 (4 e^x + x e^x) \\
& + 5237832600 \sin(x e^x) (2 e^x + x e^x)^7 (6 e^x + x e^x) - 174594420 \sin(x e^x) (2 e^x \\
& + x e^x)^5 (10 e^x + x e^x) - 1309458150 \cos(x e^x) (2 e^x + x e^x)^6 (8 e^x + x e^x) \\
& + 488864376 \sin(x e^x) (5 e^x + x e^x)^4 + 12730843125 \sin(x e^x) (e^x + x e^x)^4 (4 e^x \\
& + x e^x)^4 + 66512160 \sin(x e^x) (e^x + x e^x)^6 (7 e^x + x e^x)^2 - 47028800 \sin(x e^x) (e^x \\
& + x e^x)^{11} (3 e^x + x e^x)^3 + 77520 \sin(x e^x) (e^x + x e^x)^7 (13 e^x + x e^x) \\
& - 167960 \sin(x e^x) (e^x + x e^x)^9 (11 e^x + x e^x) - 654729075 \sin(x e^x) (2 e^x + x e^x)^{10} \\
& + 13226850 \cos(x e^x) (2 e^x + x e^x)^4 (12 e^x + x e^x) - 4408950 \cos(x e^x) (4 e^x \\
& + x e^x)^2 (12 e^x + x e^x) + 727476750 \sin(x e^x) (4 e^x + x e^x)^3 (8 e^x + x e^x) \\
& + 2546168625 \cos(x e^x) (4 e^x + x e^x)^5 + 47028800 \sin(x e^x) (3 e^x + x e^x)^3 (11 e^x \\
& + x e^x) + 1939938000 \cos(x e^x) (3 e^x + x e^x)^4 (8 e^x + x e^x) \\
& - 21727305600 \sin(x e^x) (3 e^x + x e^x)^5 (5 e^x + x e^x) - 36212176000 \cos(x e^x) (2 e^x \\
& + x e^x) (3 e^x + x e^x)^6 + 36212176000 \sin(x e^x) (e^x + x e^x)^2 (3 e^x + x e^x)^6 \\
& - 31177575 \sin(x e^x) (e^x + x e^x)^4 (8 e^x + x e^x)^2 - 20 \sin(x e^x) (e^x + x e^x) (19 e^x \\
& + x e^x) - 190 \sin(x e^x) (2 e^x + x e^x) (18 e^x + x e^x) - 1140 \sin(x e^x) (e^x \\
& + x e^x)^{17} (3 e^x + x e^x) - 1140 \sin(x e^x) (3 e^x + x e^x) (17 e^x + x e^x) \\
& - 4845 \sin(x e^x) (4 e^x + x e^x) (16 e^x + x e^x) + 15504 \sin(x e^x) (e^x + x e^x)^{15} (5 e^x \\
& + x e^x) + 167960 \sin(x e^x) (e^x + x e^x)^{11} (9 e^x + x e^x) - 23279256 \cos(x e^x) (5 e^x \\
& + x e^x)^2 (10 e^x + x e^x) - 92378 \sin(x e^x) (10 e^x + x e^x)^2 - 167960 \sin(x e^x) (9 e^x \\
& + x e^x) (11 e^x + x e^x) - 4618900 \cos(x e^x) (2 e^x + x e^x) (9 e^x + x e^x)^2 \\
& + 4618900 \sin(x e^x) (e^x + x e^x)^2 (9 e^x + x e^x)^2 - 125970 \sin(x e^x) (8 e^x + x e^x) (12 e^x \\
& + x e^x) - 31177575 \cos(x e^x) (4 e^x + x e^x) (8 e^x + x e^x)^2 - 77520 \sin(x e^x) (7 e^x \\
& + x e^x) (13 e^x + x e^x) - 15504 \sin(x e^x) (5 e^x + x e^x) (15 e^x + x e^x) \\
& - 38760 \cos(x e^x) (e^x + x e^x)^{14} (6 e^x + x e^x) - 38760 \sin(x e^x) (6 e^x + x e^x) (14 e^x \\
& + x e^x) - 77520 \sin(x e^x) (e^x + x e^x)^{13} (7 e^x + x e^x) - 14535 \cos(x e^x) (2 e^x \\
& + x e^x)^2 (16 e^x + x e^x) + 4845 \cos(x e^x) (e^x + x e^x)^4 (16 e^x + x e^x) \\
& - 15504 \sin(x e^x) (e^x + x e^x)^5 (15 e^x + x e^x) + 1140 \sin(x e^x) (e^x + x e^x)^3 (17 e^x \\
& + x e^x) + 1163962800 \sin(x e^x) (e^x + x e^x)^5 (4 e^x + x e^x) (2 e^x + x e^x) (9 e^x + x e^x) \\
& - 58198140 \sin(x e^x) (e^x + x e^x)^8 (6 e^x + x e^x)^2 - 366648282000 \cos(x e^x) (2 e^x)
\end{aligned}$$

$$\begin{aligned}
& + x e^x)^4 (3 e^x + x e^x) (5 e^x + x e^x) (4 e^x + x e^x) - 366648282000 \cos(x e^x) (e^x \\
& + x e^x) (2 e^x + x e^x)^3 (4 e^x + x e^x)^2 (5 e^x + x e^x) - 488864376000 \cos(x e^x) (e^x \\
& + x e^x) (2 e^x + x e^x)^3 (3 e^x + x e^x) (6 e^x + x e^x) (4 e^x + x e^x) \\
& - 293318625600 \cos(x e^x) (e^x + x e^x) (2 e^x + x e^x)^3 (3 e^x + x e^x) (5 e^x + x e^x)^2 \\
& + 1466593128000 \sin(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^3 (3 e^x + x e^x) (5 e^x + x e^x) (4 e^x \\
& + x e^x) - 325909584000 \cos(x e^x) (e^x + x e^x)^2 (3 e^x + x e^x)^3 (5 e^x + x e^x) (4 e^x \\
& + x e^x) - 488864376000 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x) (3 e^x + x e^x)^2 (6 e^x \\
& + x e^x) (4 e^x + x e^x) - 293318625600 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x) (3 e^x \\
& + x e^x)^2 (5 e^x + x e^x)^2 + 977728752000 \sin(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x) (3 e^x \\
& + x e^x)^2 (5 e^x + x e^x) (4 e^x + x e^x) - 69837768000 \sin(x e^x) (2 e^x + x e^x)^3 (3 e^x \\
& + x e^x) (7 e^x + x e^x) (4 e^x + x e^x) - 52378326000 \sin(x e^x) (e^x + x e^x) (4 e^x \\
& + x e^x)^2 (7 e^x + x e^x) (2 e^x + x e^x)^2 - 52378326000 \sin(x e^x) (e^x + x e^x) (3 e^x \\
& + x e^x) (8 e^x + x e^x) (2 e^x + x e^x)^2 (4 e^x + x e^x) - 83805321600 \sin(x e^x) (e^x \\
& + x e^x) (3 e^x + x e^x) (7 e^x + x e^x) (2 e^x + x e^x)^2 (5 e^x + x e^x) \\
& + 97772875200 \sin(x e^x) (e^x + x e^x)^3 (5 e^x + x e^x) (2 e^x + x e^x)^3 (6 e^x + x e^x) \\
& + 97772875200 \sin(x e^x) (e^x + x e^x)^4 (5 e^x + x e^x) (2 e^x + x e^x) (6 e^x + x e^x) (3 e^x \\
& + x e^x) + 29331862560 \cos(x e^x) (e^x + x e^x)^5 (5 e^x + x e^x) (2 e^x + x e^x)^2 (6 e^x + x e^x) \\
& - 219988969200 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^2 (4 e^x + x e^x) (5 e^x + x e^x)^2 \\
& - 293318625600 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^2 (3 e^x + x e^x) (6 e^x + x e^x) (5 e^x \\
& + x e^x) + 488864376000 \sin(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x)^2 (3 e^x + x e^x) (6 e^x \\
& + x e^x) (4 e^x + x e^x) - 581981400 \cos(x e^x) (e^x + x e^x)^4 (4 e^x + x e^x) (2 e^x \\
& + x e^x) (10 e^x + x e^x) + 38798760 \sin(x e^x) (e^x + x e^x)^{10} (6 e^x + x e^x) (4 e^x + x e^x) \\
& + 23279256 \sin(x e^x) (e^x + x e^x)^{10} (5 e^x + x e^x)^2 + 16295479200 \cos(x e^x) (2 e^x \\
& + x e^x) (3 e^x + x e^x)^2 (6 e^x + x e^x)^2 - 16295479200 \sin(x e^x) (e^x + x e^x)^2 (3 e^x \\
& + x e^x)^2 (6 e^x + x e^x)^2 + 2036934900 \sin(x e^x) (4 e^x + x e^x)^2 (6 e^x + x e^x)^2 \\
& + 3259095840 \sin(x e^x) (3 e^x + x e^x) (6 e^x + x e^x)^2 (5 e^x + x e^x) \\
& + 1163962800 \sin(x e^x) (3 e^x + x e^x)^2 (8 e^x + x e^x) (6 e^x + x e^x) \\
& + 665121600 \sin(x e^x) (3 e^x + x e^x)^2 (7 e^x + x e^x)^2 + 36664828200 \sin(x e^x) (e^x \\
& + x e^x)^6 (2 e^x + x e^x)^5 (4 e^x + x e^x) - 190 \cos(x e^x) (e^x + x e^x)^2 (18 e^x + x e^x) \\
& - 14535 \sin(x e^x) (e^x + x e^x)^{16} (2 e^x + x e^x)^2 - 190 \cos(x e^x) (e^x + x e^x)^{18} (2 e^x \\
& + x e^x) - 3420 \cos(x e^x) (e^x + x e^x) (2 e^x + x e^x) (17 e^x + x e^x) - 19380 \cos(x e^x) (e^x
\end{aligned}$$

$$\begin{aligned}
& + x e^x) (3 e^x + x e^x) (16 e^x + x e^x) + 581400 \sin(x e^x) (e^x + x e^x)^{14} (4 e^x + x e^x) (2 e^x \\
& + x e^x) + 4845 \cos(x e^x) (e^x + x e^x)^{16} (4 e^x + x e^x) + 8314020 \sin(x e^x) (e^x \\
& + x e^x)^{10} (8 e^x + x e^x) (2 e^x + x e^x) + 125970 \cos(x e^x) (e^x + x e^x)^{12} (8 e^x + x e^x) \\
& - 77597520 \cos(x e^x) (5 e^x + x e^x) (9 e^x + x e^x) (6 e^x + x e^x) \\
& + 232792560 \sin(x e^x) (e^x + x e^x) (5 e^x + x e^x)^2 (9 e^x + x e^x) - 1847560 \cos(x e^x) (e^x \\
& + x e^x) (9 e^x + x e^x) (10 e^x + x e^x) - 1511640 \cos(x e^x) (e^x + x e^x) (8 e^x \\
& + x e^x) (11 e^x + x e^x) - 27713400 \cos(x e^x) (3 e^x + x e^x) (8 e^x + x e^x) (9 e^x + x e^x) \\
& + 124710300 \sin(x e^x) (e^x + x e^x) (3 e^x + x e^x) (8 e^x + x e^x)^2 - 1007760 \cos(x e^x) (e^x \\
& + x e^x) (7 e^x + x e^x) (12 e^x + x e^x) - 77520 \cos(x e^x) (e^x + x e^x) (4 e^x + x e^x) (15 e^x \\
& + x e^x) - 1627920 \cos(x e^x) (e^x + x e^x)^{13} (5 e^x + x e^x) (2 e^x + x e^x) \\
& - 542640 \cos(x e^x) (e^x + x e^x) (6 e^x + x e^x) (13 e^x + x e^x) - 232560 \cos(x e^x) (e^x \\
& + x e^x) (5 e^x + x e^x) (14 e^x + x e^x) - 3527160 \sin(x e^x) (e^x + x e^x)^{12} (6 e^x \\
& + x e^x) (2 e^x + x e^x) - 155040 \cos(x e^x) (2 e^x + x e^x) (15 e^x + x e^x) (3 e^x + x e^x) \\
& + 232560 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x)^2 (15 e^x + x e^x) \\
& + 155040 \cos(x e^x) (e^x + x e^x)^3 (15 e^x + x e^x) (2 e^x + x e^x) \\
& - 581400 \sin(x e^x) (e^x + x e^x)^4 (14 e^x + x e^x) (2 e^x + x e^x) - 38760 \cos(x e^x) (e^x \\
& + x e^x)^6 (14 e^x + x e^x) + 29070 \sin(x e^x) (e^x + x e^x)^2 (16 e^x + x e^x) (2 e^x + x e^x) \\
& + 3527160 \sin(x e^x) (e^x + x e^x)^6 (12 e^x + x e^x) (2 e^x + x e^x) \\
& + 125970 \cos(x e^x) (e^x + x e^x)^8 (12 e^x + x e^x) + 6046560 \cos(x e^x) (e^x + x e^x)^7 (11 e^x \\
& + x e^x) (2 e^x + x e^x) - 8314020 \sin(x e^x) (e^x + x e^x)^8 (10 e^x + x e^x) (2 e^x + x e^x) \\
& - 184756 \cos(x e^x) (e^x + x e^x)^{10} (10 e^x + x e^x) + 9820936125 \sin(x e^x) (e^x \\
& + x e^x)^4 (2 e^x + x e^x)^8 + 5237832600 \cos(x e^x) (e^x + x e^x)^6 (2 e^x + x e^x)^7 \\
& - 20369349000 \sin(x e^x) (e^x + x e^x)^6 (4 e^x + x e^x)^3 (2 e^x + x e^x) \\
& - 3491888400 \sin(x e^x) (e^x + x e^x)^7 (4 e^x + x e^x)^2 (5 e^x + x e^x) \\
& - 727476750 \cos(x e^x) (e^x + x e^x)^8 (4 e^x + x e^x)^3 - 9237800 \cos(x e^x) (e^x \\
& + x e^x)^9 (9 e^x + x e^x) (2 e^x + x e^x) - 39283744500 \sin(x e^x) (e^x + x e^x) (2 e^x \\
& + x e^x)^8 (3 e^x + x e^x) - 6547290750 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^9 \\
& + 211629600 \cos(x e^x) (2 e^x + x e^x)^3 (11 e^x + x e^x) (3 e^x + x e^x) \\
& - 158722200 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x)^4 (11 e^x + x e^x) \\
& - 21162960 \cos(x e^x) (4 e^x + x e^x) (11 e^x + x e^x) (5 e^x + x e^x) \\
& + 52907400 \sin(x e^x) (e^x + x e^x) (4 e^x + x e^x)^2 (11 e^x + x e^x) \\
& + 3491888400 \sin(x e^x) (4 e^x + x e^x)^2 (7 e^x + x e^x) (5 e^x + x e^x)
\end{aligned}$$

$$\begin{aligned}
& + 5819814000 \cos(x e^x) (e^x + x e^x) (4 e^x + x e^x)^3 (7 e^x + x e^x) \\
& + 40738698000 \cos(x e^x) (3 e^x + x e^x) (4 e^x + x e^x)^3 (5 e^x + x e^x) \\
& - 50923372500 \sin(x e^x) (e^x + x e^x) (3 e^x + x e^x) (4 e^x + x e^x)^4 \\
& + 387987600 \sin(x e^x) (3 e^x + x e^x)^2 (10 e^x + x e^x) (4 e^x + x e^x) \\
& + 517316800 \cos(x e^x) (e^x + x e^x) (3 e^x + x e^x)^3 (10 e^x + x e^x) \\
& + 15519504000 \cos(x e^x) (3 e^x + x e^x)^3 (7 e^x + x e^x) (4 e^x + x e^x) \\
& - 15519504000 \sin(x e^x) (e^x + x e^x) (3 e^x + x e^x)^4 (7 e^x + x e^x) \\
& - 67897830000 \sin(x e^x) (3 e^x + x e^x)^4 (4 e^x + x e^x)^2 - 108636528000 \cos(x e^x) (e^x \\
& + x e^x) (3 e^x + x e^x)^5 (4 e^x + x e^x) + 997682400 \cos(x e^x) (e^x + x e^x)^2 (7 e^x \\
& + x e^x)^2 (4 e^x + x e^x) - 1330243200 \sin(x e^x) (e^x + x e^x)^3 (7 e^x + x e^x)^2 (3 e^x + x e^x) \\
& + 387600 \sin(x e^x) (e^x + x e^x)^{14} (3 e^x + x e^x)^2 + 22170720 \sin(x e^x) (e^x \\
& + x e^x)^{10} (7 e^x + x e^x) (3 e^x + x e^x) - 58198140 \cos(x e^x) (6 e^x + x e^x)^2 (8 e^x + x e^x) \\
& - 99768240 \cos(x e^x) (5 e^x + x e^x) (8 e^x + x e^x) (7 e^x + x e^x) \\
& + 1047566520 \sin(x e^x) (2 e^x + x e^x) (5 e^x + x e^x)^2 (8 e^x + x e^x) \\
& - 8314020 \cos(x e^x) (2 e^x + x e^x) (8 e^x + x e^x) (10 e^x + x e^x) \\
& + 8314020 \sin(x e^x) (e^x + x e^x)^2 (8 e^x + x e^x) (10 e^x + x e^x) \\
& + 93532725 \sin(x e^x) (2 e^x + x e^x)^2 (8 e^x + x e^x)^2 - 6046560 \cos(x e^x) (2 e^x \\
& + x e^x) (7 e^x + x e^x) (11 e^x + x e^x) + 6046560 \sin(x e^x) (e^x + x e^x)^2 (7 e^x \\
& + x e^x) (11 e^x + x e^x) + 155040 \sin(x e^x) (e^x + x e^x)^2 (3 e^x + x e^x) (15 e^x + x e^x) \\
& - 2713200 \cos(x e^x) (e^x + x e^x)^{13} (4 e^x + x e^x) (3 e^x + x e^x) \\
& - 3527160 \cos(x e^x) (2 e^x + x e^x) (6 e^x + x e^x) (12 e^x + x e^x) \\
& + 3527160 \sin(x e^x) (e^x + x e^x)^2 (6 e^x + x e^x) (12 e^x + x e^x) \\
& - 1627920 \cos(x e^x) (2 e^x + x e^x) (5 e^x + x e^x) (13 e^x + x e^x) \\
& + 1627920 \sin(x e^x) (e^x + x e^x)^2 (5 e^x + x e^x) (13 e^x + x e^x) - 581400 \cos(x e^x) (2 e^x \\
& + x e^x) (4 e^x + x e^x) (14 e^x + x e^x) + 581400 \sin(x e^x) (e^x + x e^x)^2 (4 e^x \\
& + x e^x) (14 e^x + x e^x) - 7054320 \sin(x e^x) (e^x + x e^x)^{12} (5 e^x + x e^x) (3 e^x + x e^x) \\
& - 387600 \cos(x e^x) (3 e^x + x e^x)^2 (14 e^x + x e^x) + 581400 \sin(x e^x) (2 e^x \\
& + x e^x)^3 (14 e^x + x e^x) + 775200 \cos(x e^x) (e^x + x e^x)^3 (14 e^x + x e^x) (3 e^x + x e^x) \\
& - 2713200 \sin(x e^x) (e^x + x e^x)^4 (13 e^x + x e^x) (3 e^x + x e^x) \\
& + 108636528000 \sin(x e^x) (e^x + x e^x)^3 (3 e^x + x e^x)^4 (5 e^x + x e^x) \\
& + 21727305600 \cos(x e^x) (3 e^x + x e^x)^3 (6 e^x + x e^x) (5 e^x + x e^x)
\end{aligned}$$

$$\begin{aligned}
& + 48886437600 \cos(x e^x) (3 e^x + x e^x)^2 (5 e^x + x e^x)^2 (4 e^x + x e^x) \\
& + 20369349000 \cos(x e^x) (2 e^x + x e^x) (4 e^x + x e^x)^3 (6 e^x + x e^x) \\
& - 20369349000 \sin(x e^x) (e^x + x e^x)^2 (4 e^x + x e^x)^3 (6 e^x + x e^x) \\
& + 19554575040 \cos(x e^x) (2 e^x + x e^x) (5 e^x + x e^x)^3 (3 e^x + x e^x) \\
& - 29331862560 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x)^2 (5 e^x + x e^x)^3 \\
& - 19554575040 \sin(x e^x) (e^x + x e^x)^2 (3 e^x + x e^x) (5 e^x + x e^x)^3 \\
& + 133024320 \cos(x e^x) (e^x + x e^x)^7 (6 e^x + x e^x) (7 e^x + x e^x) \\
& + 99768240 \cos(x e^x) (e^x + x e^x)^7 (5 e^x + x e^x) (8 e^x + x e^x) \\
& - 99768240 \sin(x e^x) (e^x + x e^x)^8 (5 e^x + x e^x) (7 e^x + x e^x) \\
& + 55426800 \cos(x e^x) (e^x + x e^x)^7 (4 e^x + x e^x) (9 e^x + x e^x) \\
& - 62355150 \sin(x e^x) (e^x + x e^x)^8 (4 e^x + x e^x) (8 e^x + x e^x) \\
& + 22170720 \cos(x e^x) (e^x + x e^x)^7 (3 e^x + x e^x) (10 e^x + x e^x) \\
& - 27713400 \sin(x e^x) (e^x + x e^x)^8 (3 e^x + x e^x) (9 e^x + x e^x) \\
& + 13226850 \sin(x e^x) (e^x + x e^x)^{12} (2 e^x + x e^x)^4 + 581400 \cos(x e^x) (e^x \\
& + x e^x)^{14} (2 e^x + x e^x)^3 - 66512160 \cos(x e^x) (6 e^x + x e^x) (7 e^x + x e^x)^2 \\
& + 465585120 \sin(x e^x) (e^x + x e^x) (6 e^x + x e^x)^2 (7 e^x + x e^x) \\
& + 399072960 \sin(x e^x) (e^x + x e^x) (5 e^x + x e^x) (7 e^x + x e^x)^2 \\
& + 2793510720 \sin(x e^x) (3 e^x + x e^x) (5 e^x + x e^x)^2 (7 e^x + x e^x) \\
& - 22170720 \cos(x e^x) (3 e^x + x e^x) (7 e^x + x e^x) (10 e^x + x e^x) \\
& - 35271600 \cos(x e^x) (e^x + x e^x)^{12} (3 e^x + x e^x)^2 (2 e^x + x e^x) \\
& - 7054320 \cos(x e^x) (3 e^x + x e^x) (5 e^x + x e^x) (12 e^x + x e^x) \\
& - 2713200 \cos(x e^x) (3 e^x + x e^x) (4 e^x + x e^x) (13 e^x + x e^x) \\
& + 1163962800 \sin(x e^x) (e^x + x e^x)^9 (5 e^x + x e^x) (4 e^x + x e^x) (2 e^x + x e^x) \\
& + 21162960 \cos(x e^x) (e^x + x e^x)^{11} (5 e^x + x e^x) (4 e^x + x e^x) \\
& + 16295479200 \cos(x e^x) (e^x + x e^x) (3 e^x + x e^x) (6 e^x + x e^x)^2 (4 e^x + x e^x) \\
& + 9311702400 \cos(x e^x) (e^x + x e^x) (3 e^x + x e^x)^2 (6 e^x + x e^x) (7 e^x + x e^x) \\
& + 4655851200 \sin(x e^x) (3 e^x + x e^x) (6 e^x + x e^x) (4 e^x + x e^x) (7 e^x + x e^x) \\
& + 12221609400 \sin(x e^x) (e^x + x e^x)^4 (6 e^x + x e^x)^2 (2 e^x + x e^x)^2 \\
& + 20951330400 \sin(x e^x) (e^x + x e^x)^4 (5 e^x + x e^x) (2 e^x + x e^x)^2 (7 e^x + x e^x) \\
& + 73329656400 \sin(x e^x) (e^x + x e^x)^5 (2 e^x + x e^x)^6 (3 e^x + x e^x) \\
& + 122216094000 \sin(x e^x) (e^x + x e^x)^6 (2 e^x + x e^x)^4 (3 e^x + x e^x)^2
\end{aligned}$$

$$\begin{aligned}
& + 20951330400 \cos(x e^x) (e^x + x e^x)^7 (2 e^x + x e^x)^5 (3 e^x + x e^x) \\
& - 183324141000 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^2 (4 e^x + x e^x)^2 (6 e^x + x e^x) \\
& + 366648282000 \sin(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x)^2 (4 e^x + x e^x)^2 (5 e^x + x e^x) \\
& + 293318625600 \sin(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x)^2 (3 e^x + x e^x) (5 e^x + x e^x)^2 \\
& - 122216094000 \cos(x e^x) (2 e^x + x e^x)^4 (3 e^x + x e^x)^2 (6 e^x + x e^x) \\
& - 139675536000 \cos(x e^x) (e^x + x e^x) (2 e^x + x e^x)^3 (3 e^x + x e^x)^2 (7 e^x + x e^x) \\
& + 488864376000 \sin(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^3 (3 e^x + x e^x)^2 (6 e^x + x e^x) \\
& - 54318264000 \cos(x e^x) (e^x + x e^x)^2 (3 e^x + x e^x)^4 (6 e^x + x e^x) \\
& - 93117024000 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x) (3 e^x + x e^x)^3 (7 e^x + x e^x) \\
& + 217273056000 \sin(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x) (3 e^x + x e^x)^3 (6 e^x + x e^x) \\
& + 20951330400 \cos(x e^x) (e^x + x e^x)^5 (4 e^x + x e^x) (2 e^x + x e^x)^2 (7 e^x + x e^x) \\
& - 24443218800 \sin(x e^x) (e^x + x e^x)^6 (4 e^x + x e^x) (2 e^x + x e^x)^2 (6 e^x + x e^x) \\
& + 73329656400 \sin(x e^x) (2 e^x + x e^x)^6 (3 e^x + x e^x) (5 e^x + x e^x) \\
& + 219988969200 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x)^5 (4 e^x + x e^x) (5 e^x + x e^x) \\
& + 146659312800 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x)^5 (3 e^x + x e^x) (6 e^x + x e^x) \\
& + 366648282000 \cos(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x)^4 (4 e^x + x e^x) (5 e^x + x e^x) \\
& + 244432188000 \cos(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x)^4 (3 e^x + x e^x) (6 e^x + x e^x) \\
& - 366648282000 \sin(x e^x) (e^x + x e^x)^4 (2 e^x + x e^x)^4 (3 e^x + x e^x) (5 e^x + x e^x) \\
& + 20951330400 \cos(x e^x) (2 e^x + x e^x)^2 (4 e^x + x e^x) (7 e^x + x e^x) (5 e^x + x e^x) \\
& + 10475665200 \cos(x e^x) (2 e^x + x e^x)^2 (3 e^x + x e^x) (8 e^x + x e^x) (5 e^x + x e^x) \\
& + 13967553600 \cos(x e^x) (2 e^x + x e^x)^2 (3 e^x + x e^x) (7 e^x + x e^x) (6 e^x + x e^x) \\
& - 27935107200 \sin(x e^x) (e^x + x e^x)^2 (3 e^x + x e^x)^2 (7 e^x + x e^x) (5 e^x + x e^x) \\
& - 146659312800 \sin(x e^x) (2 e^x + x e^x)^2 (3 e^x + x e^x)^2 (5 e^x + x e^x)^2 \\
& - 65181916800 \sin(x e^x) (e^x + x e^x) (3 e^x + x e^x)^3 (5 e^x + x e^x)^2 \\
& + 14665931280 \cos(x e^x) (2 e^x + x e^x)^2 (5 e^x + x e^x)^2 (6 e^x + x e^x) \\
& + 12221609400 \cos(x e^x) (2 e^x + x e^x)^2 (4 e^x + x e^x) (6 e^x + x e^x)^2 \\
& - 29331862560 \sin(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x) (5 e^x + x e^x)^2 (6 e^x + x e^x) \\
& - 24443218800 \sin(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x) (4 e^x + x e^x) (6 e^x + x e^x)^2 \\
& + 274986211500 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^5 (4 e^x + x e^x)^2 \\
& - 733296564000 \sin(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x)^5 (3 e^x + x e^x) (4 e^x + x e^x) \\
& - 1222160940000 \sin(x e^x) (e^x + x e^x)^4 (2 e^x + x e^x)^3 (3 e^x + x e^x)^2 (4 e^x + x e^x)
\end{aligned}$$

$$\begin{aligned}
& + 135795660000 \cos(x e^x) (e^x + x e^x)^4 (3 e^x + x e^x)^4 (4 e^x + x e^x) \\
& + 325909584000 \cos(x e^x) (e^x + x e^x)^4 (2 e^x + x e^x) (3 e^x + x e^x)^3 (5 e^x + x e^x) \\
& - 325909584000 \sin(x e^x) (e^x + x e^x)^5 (2 e^x + x e^x) (3 e^x + x e^x)^3 (4 e^x + x e^x) \\
& + 152770117500 \cos(x e^x) (e^x + x e^x)^4 (2 e^x + x e^x)^2 (4 e^x + x e^x)^3 \\
& - 366648282000 \sin(x e^x) (e^x + x e^x)^5 (2 e^x + x e^x)^2 (3 e^x + x e^x) (4 e^x + x e^x)^2 \\
& + 73329656400 \cos(x e^x) (e^x + x e^x)^4 (5 e^x + x e^x)^2 (2 e^x + x e^x)^3 \\
& - 146659312800 \sin(x e^x) (e^x + x e^x)^5 (4 e^x + x e^x) (2 e^x + x e^x)^3 (5 e^x + x e^x) \\
& + 6547290750 \cos(x e^x) (2 e^x + x e^x)^2 (4 e^x + x e^x)^2 (8 e^x + x e^x) \\
& + 5819814000 \cos(x e^x) (2 e^x + x e^x)^2 (3 e^x + x e^x) (9 e^x + x e^x) (4 e^x + x e^x) \\
& + 2909907000 \cos(x e^x) (e^x + x e^x) (4 e^x + x e^x)^2 (9 e^x + x e^x) (2 e^x + x e^x) \\
& + 8729721000 \cos(x e^x) (e^x + x e^x) (4 e^x + x e^x)^2 (8 e^x + x e^x) (3 e^x + x e^x) \\
& - 13094581500 \sin(x e^x) (e^x + x e^x)^2 (4 e^x + x e^x)^2 (8 e^x + x e^x) (2 e^x + x e^x) \\
& - 17459442000 \sin(x e^x) (e^x + x e^x)^2 (3 e^x + x e^x)^2 (8 e^x + x e^x) (4 e^x + x e^x) \\
& - 34918884000 \sin(x e^x) (e^x + x e^x)^2 (4 e^x + x e^x)^2 (7 e^x + x e^x) (3 e^x + x e^x) \\
& + 69837768000 \cos(x e^x) (e^x + x e^x)^4 (3 e^x + x e^x) (7 e^x + x e^x) (2 e^x + x e^x)^3 \\
& - 97772875200 \sin(x e^x) (e^x + x e^x)^5 (3 e^x + x e^x) (6 e^x + x e^x) (2 e^x + x e^x)^3 \\
& + 27935107200 \cos(x e^x) (e^x + x e^x)^5 (3 e^x + x e^x)^2 (7 e^x + x e^x) (2 e^x + x e^x) \\
& + 21727305600 \cos(x e^x) (e^x + x e^x)^5 (3 e^x + x e^x)^3 (6 e^x + x e^x) \\
& - 32590958400 \sin(x e^x) (e^x + x e^x)^6 (3 e^x + x e^x)^2 (6 e^x + x e^x) (2 e^x + x e^x) \\
& - 97772875200 \cos(x e^x) (e^x + x e^x)^6 (2 e^x + x e^x)^3 (5 e^x + x e^x) (3 e^x + x e^x) \\
& - 61108047000 \cos(x e^x) (e^x + x e^x)^6 (2 e^x + x e^x)^3 (4 e^x + x e^x)^2 \\
& + 69837768000 \sin(x e^x) (e^x + x e^x)^7 (2 e^x + x e^x)^3 (4 e^x + x e^x) (3 e^x + x e^x) \\
& - 15519504000 \cos(x e^x) (e^x + x e^x)^7 (3 e^x + x e^x)^3 (4 e^x + x e^x) \\
& - 27935107200 \cos(x e^x) (e^x + x e^x)^7 (2 e^x + x e^x) (5 e^x + x e^x) (3 e^x + x e^x)^2 \\
& + 17459442000 \sin(x e^x) (e^x + x e^x)^8 (2 e^x + x e^x) (4 e^x + x e^x) (3 e^x + x e^x)^2 \\
& - 40738698000 \cos(x e^x) (e^x + x e^x)^3 (4 e^x + x e^x)^3 (5 e^x + x e^x) \\
& - 81477396000 \cos(x e^x) (e^x + x e^x)^3 (3 e^x + x e^x) (6 e^x + x e^x) (4 e^x + x e^x)^2 \\
& + 122216094000 \sin(x e^x) (e^x + x e^x)^4 (3 e^x + x e^x) (5 e^x + x e^x) (4 e^x + x e^x)^2 \\
& - 19554575040 \cos(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x) (5 e^x + x e^x)^3 \\
& + 73329656400 \sin(x e^x) (e^x + x e^x)^4 (2 e^x + x e^x) (4 e^x + x e^x) (5 e^x + x e^x)^2 \\
& - 407386980000 \cos(x e^x) (2 e^x + x e^x)^2 (3 e^x + x e^x)^4 (4 e^x + x e^x)
\end{aligned}$$

$$\begin{aligned}
& -325909584000 \cos(x e^x) (e^x + x e^x) (2 e^x + x e^x) (3 e^x + x e^x)^4 (5 e^x + x e^x) \\
& + 814773960000 \sin(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x) (3 e^x + x e^x)^4 (4 e^x + x e^x) \\
& - 611080470000 \cos(x e^x) (2 e^x + x e^x)^3 (3 e^x + x e^x)^2 (4 e^x + x e^x)^2 \\
& + 1833241410000 \sin(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^2 (3 e^x + x e^x)^2 (4 e^x + x e^x)^2 \\
& - 203693490000 \cos(x e^x) (e^x + x e^x)^2 (3 e^x + x e^x)^2 (4 e^x + x e^x)^3 \\
& - 76385058750 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x) (4 e^x + x e^x)^4 \\
& + 407386980000 \sin(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x) (3 e^x + x e^x) (4 e^x + x e^x)^3 \\
& - 244432188000 \sin(x e^x) (2 e^x + x e^x)^2 (3 e^x + x e^x)^2 (6 e^x + x e^x) (4 e^x + x e^x) \\
& - 108636528000 \sin(x e^x) (e^x + x e^x) (3 e^x + x e^x)^3 (6 e^x + x e^x) (4 e^x + x e^x) \\
& + 997682400 \cos(x e^x) (e^x + x e^x)^2 (7 e^x + x e^x) (3 e^x + x e^x) (8 e^x + x e^x) \\
& - 2993047200 \sin(x e^x) (e^x + x e^x)^2 (7 e^x + x e^x)^2 (2 e^x + x e^x)^2 \\
& - 997682400 \sin(x e^x) (e^x + x e^x)^3 (7 e^x + x e^x) (2 e^x + x e^x) (8 e^x + x e^x) \\
& - 997682400 \cos(x e^x) (e^x + x e^x)^4 (7 e^x + x e^x)^2 (2 e^x + x e^x) \\
& + 8139600 \sin(x e^x) (e^x + x e^x)^{13} (3 e^x + x e^x) (2 e^x + x e^x)^2 \\
& + 155040 \cos(x e^x) (e^x + x e^x)^{15} (3 e^x + x e^x) (2 e^x + x e^x) \\
& + 166280400 \sin(x e^x) (e^x + x e^x)^9 (7 e^x + x e^x) (2 e^x + x e^x)^2 \\
& + 6046560 \cos(x e^x) (e^x + x e^x)^{11} (7 e^x + x e^x) (2 e^x + x e^x) \\
& + 698377680 \sin(x e^x) (e^x + x e^x) (5 e^x + x e^x) (8 e^x + x e^x) (6 e^x + x e^x) \\
& + 1047566520 \cos(x e^x) (e^x + x e^x)^2 (5 e^x + x e^x)^2 (8 e^x + x e^x) \\
& + 83140200 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x) (8 e^x + x e^x) (9 e^x + x e^x) \\
& + 187065450 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x) (8 e^x + x e^x)^2 \\
& + 27713400 \cos(x e^x) (e^x + x e^x)^3 (8 e^x + x e^x) (9 e^x + x e^x) \\
& - 26453700 \cos(x e^x) (e^x + x e^x)^{12} (4 e^x + x e^x) (2 e^x + x e^x)^2 \\
& - 63488880 \sin(x e^x) (e^x + x e^x)^{11} (5 e^x + x e^x) (2 e^x + x e^x)^2 \\
& + 2325600 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x) (14 e^x + x e^x) (3 e^x + x e^x) \\
& + 1744200 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^2 (14 e^x + x e^x) \\
& - 8139600 \sin(x e^x) (e^x + x e^x)^3 (13 e^x + x e^x) (2 e^x + x e^x)^2 \\
& - 1627920 \cos(x e^x) (e^x + x e^x)^5 (13 e^x + x e^x) (2 e^x + x e^x) \\
& - 325909584000 \cos(x e^x) (2 e^x + x e^x)^3 (3 e^x + x e^x)^3 (5 e^x + x e^x) \\
& + 271591320000 \sin(x e^x) (e^x + x e^x)^3 (3 e^x + x e^x)^3 (4 e^x + x e^x)^2 \\
& + 305540235000 \sin(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^3 (4 e^x + x e^x)^3
\end{aligned}$$

$$\begin{aligned}
& + 40738698000 \cos(x e^x) (3 e^x + x e^x)^2 (6 e^x + x e^x) (4 e^x + x e^x)^2 \\
& - 36664828200 \sin(x e^x) (e^x + x e^x)^2 (4 e^x + x e^x)^2 (5 e^x + x e^x)^2 \\
& + 2793510720 \cos(x e^x) (e^x + x e^x)^6 (5 e^x + x e^x) (7 e^x + x e^x) (2 e^x + x e^x) \\
& + 1745944200 \cos(x e^x) (e^x + x e^x)^6 (4 e^x + x e^x) (8 e^x + x e^x) (2 e^x + x e^x) \\
& - 1995364800 \sin(x e^x) (e^x + x e^x)^7 (4 e^x + x e^x) (7 e^x + x e^x) (2 e^x + x e^x) \\
& - 55426800 \cos(x e^x) (e^x + x e^x)^9 (4 e^x + x e^x) (7 e^x + x e^x) \\
& + 775975200 \cos(x e^x) (e^x + x e^x)^6 (3 e^x + x e^x) (9 e^x + x e^x) (2 e^x + x e^x) \\
& - 997682400 \sin(x e^x) (e^x + x e^x)^7 (3 e^x + x e^x) (8 e^x + x e^x) (2 e^x + x e^x) \\
& - 27713400 \cos(x e^x) (e^x + x e^x)^9 (3 e^x + x e^x) (8 e^x + x e^x) \\
& + 775975200 \sin(x e^x) (e^x + x e^x)^9 (6 e^x + x e^x) (3 e^x + x e^x) (2 e^x + x e^x) \\
& + 14108640 \cos(x e^x) (e^x + x e^x)^{11} (6 e^x + x e^x) (3 e^x + x e^x) \\
& + 2793510720 \sin(x e^x) (2 e^x + x e^x) (5 e^x + x e^x) (7 e^x + x e^x) (6 e^x + x e^x) \\
& + 66512160 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x) (7 e^x + x e^x) (10 e^x + x e^x) \\
& + 22170720 \cos(x e^x) (e^x + x e^x)^3 (7 e^x + x e^x) (10 e^x + x e^x) \\
& + 21162960 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x) (5 e^x + x e^x) (12 e^x + x e^x) \\
& + 7054320 \cos(x e^x) (e^x + x e^x)^3 (5 e^x + x e^x) (12 e^x + x e^x) + 8139600 \sin(x e^x) (e^x \\
& + x e^x) (2 e^x + x e^x) (4 e^x + x e^x) (13 e^x + x e^x) + 2713200 \cos(x e^x) (e^x \\
& + x e^x)^3 (4 e^x + x e^x) (13 e^x + x e^x) - 211629600 \sin(x e^x) (e^x + x e^x)^{11} (4 e^x \\
& + x e^x) (3 e^x + x e^x) (2 e^x + x e^x) + 42325920 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x) (6 e^x \\
& + x e^x) (11 e^x + x e^x) + 14108640 \cos(x e^x) (e^x + x e^x)^3 (6 e^x + x e^x) (11 e^x + x e^x) \\
& + 16279200 \cos(x e^x) (e^x + x e^x)^2 (13 e^x + x e^x) (3 e^x + x e^x) (2 e^x + x e^x) \\
& - 70543200 \sin(x e^x) (e^x + x e^x)^3 (12 e^x + x e^x) (3 e^x + x e^x) (2 e^x + x e^x) \\
& - 7054320 \cos(x e^x) (e^x + x e^x)^5 (12 e^x + x e^x) (3 e^x + x e^x) \\
& + 63488880 \sin(x e^x) (e^x + x e^x)^5 (11 e^x + x e^x) (2 e^x + x e^x)^2 \\
& + 465585120 \sin(x e^x) (e^x + x e^x)^5 (10 e^x + x e^x) (3 e^x + x e^x) (2 e^x + x e^x) \\
& - 187065450 \cos(x e^x) (e^x + x e^x)^8 (8 e^x + x e^x) (2 e^x + x e^x)^2 \\
& - 166280400 \sin(x e^x) (e^x + x e^x)^7 (9 e^x + x e^x) (2 e^x + x e^x)^2 \\
& - 104756652000 \cos(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x)^7 (3 e^x + x e^x) \\
& + 36664828200 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^6 (6 e^x + x e^x) \\
& + 1163962800 \cos(x e^x) (2 e^x + x e^x)^2 (10 e^x + x e^x) (3 e^x + x e^x)^2 \\
& - 2327925600 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x)^3 (10 e^x + x e^x) (3 e^x + x e^x)
\end{aligned}$$

$$\begin{aligned}
& -5819814000 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x)^3 (9 e^x + x e^x) (4 e^x + x e^x) \\
& -872972100 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^4 (10 e^x + x e^x) \\
& -17459442000 \sin(x e^x) (2 e^x + x e^x)^3 (8 e^x + x e^x) (3 e^x + x e^x)^2 \\
& -26189163000 \cos(x e^x) (e^x + x e^x) (2 e^x + x e^x)^4 (8 e^x + x e^x) (3 e^x + x e^x) \\
& -52378326000 \cos(x e^x) (e^x + x e^x) (2 e^x + x e^x)^4 (7 e^x + x e^x) (4 e^x + x e^x) \\
& +104756652000 \sin(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^4 (7 e^x + x e^x) (3 e^x + x e^x) \\
& +20951330400 \cos(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x)^5 (7 e^x + x e^x) \\
& +232792560 \sin(x e^x) (e^x + x e^x) (4 e^x + x e^x) (10 e^x + x e^x) (5 e^x + x e^x) \\
& +387987600 \sin(x e^x) (e^x + x e^x) (4 e^x + x e^x) (9 e^x + x e^x) (6 e^x + x e^x) \\
& +1163962800 \sin(x e^x) (2 e^x + x e^x) (4 e^x + x e^x) (9 e^x + x e^x) (5 e^x + x e^x) \\
& -13967553600 \cos(x e^x) (e^x + x e^x)^7 (3 e^x + x e^x) (6 e^x + x e^x) (2 e^x + x e^x)^2 \\
& -293318625600 \sin(x e^x) (e^x + x e^x)^5 (2 e^x + x e^x)^2 (5 e^x + x e^x) (3 e^x + x e^x)^2 \\
& +5819814000 \cos(x e^x) (e^x + x e^x)^9 (2 e^x + x e^x)^2 (4 e^x + x e^x) (3 e^x + x e^x) \\
& -325909584000 \cos(x e^x) (e^x + x e^x) (2 e^x + x e^x)^2 (3 e^x + x e^x)^3 (6 e^x + x e^x) \\
& +122216094000 \cos(x e^x) (e^x + x e^x)^4 (4 e^x + x e^x) (2 e^x + x e^x)^3 (6 e^x + x e^x) \\
& +97772875200 \cos(x e^x) (e^x + x e^x)^5 (4 e^x + x e^x) (2 e^x + x e^x) (6 e^x + x e^x) (3 e^x \\
& +x e^x) +733296564000 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x)^4 (3 e^x + x e^x)^2 (5 e^x \\
& +x e^x) +439977938400 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^5 (3 e^x + x e^x) (5 e^x \\
& +x e^x) +977728752000 \sin(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^2 (3 e^x + x e^x)^3 (5 e^x \\
& +x e^x) +977728752000 \cos(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x)^3 (3 e^x + x e^x)^2 (5 e^x \\
& +x e^x) +27935107200 \cos(x e^x) (2 e^x + x e^x) (3 e^x + x e^x)^2 (7 e^x + x e^x) (5 e^x \\
& +x e^x) +8380532160 \cos(x e^x) (e^x + x e^x) (5 e^x + x e^x)^2 (7 e^x + x e^x) (2 e^x + x e^x) \\
& +10475665200 \cos(x e^x) (e^x + x e^x) (4 e^x + x e^x) (8 e^x + x e^x) (5 e^x + x e^x) (2 e^x \\
& +x e^x) +13967553600 \cos(x e^x) (e^x + x e^x) (4 e^x + x e^x) (7 e^x + x e^x) (6 e^x \\
& +x e^x) (2 e^x + x e^x) +27935107200 \cos(x e^x) (e^x + x e^x) (4 e^x + x e^x) (7 e^x \\
& +x e^x) (5 e^x + x e^x) (3 e^x + x e^x) -41902660800 \sin(x e^x) (e^x + x e^x)^2 (4 e^x \\
& +x e^x) (7 e^x + x e^x) (5 e^x + x e^x) (2 e^x + x e^x) +4655851200 \cos(x e^x) (e^x \\
& +x e^x) (3 e^x + x e^x) (9 e^x + x e^x) (5 e^x + x e^x) (2 e^x + x e^x) \\
& +6983776800 \cos(x e^x) (e^x + x e^x) (3 e^x + x e^x) (8 e^x + x e^x) (6 e^x + x e^x) (2 e^x \\
& +x e^x) +6983776800 \cos(x e^x) (e^x + x e^x) (3 e^x + x e^x)^2 (8 e^x + x e^x) (5 e^x + x e^x) \\
& -20951330400 \sin(x e^x) (e^x + x e^x)^2 (3 e^x + x e^x) (8 e^x + x e^x) (5 e^x + x e^x) (2 e^x \\
& +x e^x) +3990729600 \cos(x e^x) (e^x + x e^x) (3 e^x + x e^x) (7 e^x + x e^x)^2 (2 e^x + x e^x)
\end{aligned}$$

$$\begin{aligned}
& -27935107200 \sin(x e^x) (e^x + x e^x)^2 (3 e^x + x e^x) (7 e^x + x e^x) (6 e^x + x e^x) (2 e^x \\
& + x e^x) - 34918884000 \cos(x e^x) (e^x + x e^x)^3 (4 e^x + x e^x)^2 (7 e^x + x e^x) (2 e^x + x e^x) \\
& - 34918884000 \cos(x e^x) (e^x + x e^x)^3 (3 e^x + x e^x) (8 e^x + x e^x) (4 e^x + x e^x) (2 e^x \\
& + x e^x) - 46558512000 \cos(x e^x) (e^x + x e^x)^3 (3 e^x + x e^x)^2 (7 e^x + x e^x) (4 e^x + x e^x) \\
& + 69837768000 \sin(x e^x) (e^x + x e^x)^4 (3 e^x + x e^x) (7 e^x + x e^x) (4 e^x + x e^x) (2 e^x \\
& + x e^x) - 97772875200 \cos(x e^x) (e^x + x e^x)^3 (4 e^x + x e^x) (6 e^x + x e^x) (5 e^x \\
& + x e^x) (2 e^x + x e^x) - 32590958400 \cos(x e^x) (e^x + x e^x)^3 (3 e^x + x e^x) (6 e^x \\
& + x e^x)^2 (2 e^x + x e^x) - 65181916800 \cos(x e^x) (e^x + x e^x)^3 (3 e^x + x e^x)^2 (6 e^x \\
& + x e^x) (5 e^x + x e^x) + 58663725120 \cos(x e^x) (e^x + x e^x)^5 (5 e^x + x e^x)^2 (3 e^x \\
& + x e^x) (2 e^x + x e^x) + 73329656400 \cos(x e^x) (e^x + x e^x)^5 (4 e^x + x e^x)^2 (5 e^x \\
& + x e^x) (2 e^x + x e^x) + 97772875200 \cos(x e^x) (e^x + x e^x)^5 (4 e^x + x e^x) (3 e^x \\
& + x e^x)^2 (5 e^x + x e^x) - 97772875200 \sin(x e^x) (e^x + x e^x)^6 (4 e^x + x e^x) (3 e^x \\
& + x e^x) (5 e^x + x e^x) (2 e^x + x e^x) - 293318625600 \sin(x e^x) (e^x + x e^x) (2 e^x \\
& + x e^x) (3 e^x + x e^x) (5 e^x + x e^x)^2 (4 e^x + x e^x) - 195545750400 \sin(x e^x) (e^x \\
& + x e^x) (2 e^x + x e^x) (3 e^x + x e^x)^2 (5 e^x + x e^x) (6 e^x + x e^x) \\
& - 97772875200 \sin(x e^x) (2 e^x + x e^x)^3 (3 e^x + x e^x) (5 e^x + x e^x) (6 e^x + x e^x) \\
& - 146659312800 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x)^2 (4 e^x + x e^x) (5 e^x + x e^x) (6 e^x \\
& + x e^x) - 48886437600 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x)^2 (3 e^x + x e^x) (6 e^x + x e^x)^2 \\
& + 97772875200 \cos(x e^x) (2 e^x + x e^x) (3 e^x + x e^x) (5 e^x + x e^x) (4 e^x + x e^x) (6 e^x \\
& + x e^x) + 24443218800 \cos(x e^x) (e^x + x e^x) (4 e^x + x e^x)^2 (5 e^x + x e^x) (6 e^x + x e^x) \\
& + 19554575040 \cos(x e^x) (e^x + x e^x) (3 e^x + x e^x) (5 e^x + x e^x)^2 (6 e^x + x e^x) \\
& - 97772875200 \sin(x e^x) (e^x + x e^x)^2 (3 e^x + x e^x) (5 e^x + x e^x) (4 e^x + x e^x) (6 e^x \\
& + x e^x) + 9777287520 \cos(x e^x) (e^x + x e^x) (2 e^x + x e^x) (5 e^x + x e^x) (6 e^x + x e^x)^2 \\
& + 366648282000 \cos(x e^x) (e^x + x e^x) (2 e^x + x e^x)^6 (3 e^x + x e^x) (4 e^x + x e^x) \\
& + 1833241410000 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^4 (3 e^x + x e^x)^2 (4 e^x + x e^x) \\
& + 1629547920000 \cos(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x)^2 (3 e^x + x e^x)^3 (4 e^x + x e^x) \\
& + 1222160940000 \cos(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x)^3 (3 e^x + x e^x) (4 e^x + x e^x)^2 \\
& + 611080470000 \cos(x e^x) (e^x + x e^x)^4 (2 e^x + x e^x) (3 e^x + x e^x)^2 (4 e^x + x e^x)^2 \\
& + 17459442000 \cos(x e^x) (2 e^x + x e^x) (3 e^x + x e^x)^2 (8 e^x + x e^x) (4 e^x + x e^x) \\
& + 2327925600 \cos(x e^x) (e^x + x e^x) (3 e^x + x e^x) (10 e^x + x e^x) (2 e^x + x e^x) (4 e^x \\
& + x e^x) + 3879876000 \cos(x e^x) (e^x + x e^x) (3 e^x + x e^x)^2 (9 e^x + x e^x) (4 e^x + x e^x)
\end{aligned}$$

$$\begin{aligned}
& -11639628000 \sin(x e^x) (e^x + x e^x)^2 (3 e^x + x e^x) (9 e^x + x e^x) (2 e^x + x e^x) (4 e^x \\
& + x e^x) + 244432188000 \cos(x e^x) (e^x + x e^x)^4 (3 e^x + x e^x)^2 (6 e^x + x e^x) (2 e^x \\
& + x e^x)^2 + 61108047000 \sin(x e^x) (e^x + x e^x)^4 (4 e^x + x e^x)^2 (6 e^x + x e^x) (2 e^x + x e^x) \\
& + 81477396000 \sin(x e^x) (e^x + x e^x)^4 (3 e^x + x e^x)^2 (6 e^x + x e^x) (4 e^x + x e^x) \\
& - 366648282000 \cos(x e^x) (e^x + x e^x)^5 (2 e^x + x e^x)^4 (4 e^x + x e^x) (3 e^x + x e^x) \\
& - 244432188000 \cos(x e^x) (e^x + x e^x)^6 (2 e^x + x e^x)^2 (4 e^x + x e^x) (3 e^x + x e^x)^2 \\
& - 34918884000 \cos(x e^x) (e^x + x e^x)^7 (2 e^x + x e^x) (4 e^x + x e^x)^2 (3 e^x + x e^x) \\
& - 97772875200 \cos(x e^x) (e^x + x e^x)^3 (3 e^x + x e^x) (5 e^x + x e^x)^2 (4 e^x + x e^x) \\
& - 814773960000 \cos(x e^x) (e^x + x e^x) (2 e^x + x e^x) (3 e^x + x e^x)^3 (4 e^x + x e^x)^2 \\
& - 611080470000 \cos(x e^x) (e^x + x e^x) (2 e^x + x e^x)^2 (3 e^x + x e^x) (4 e^x + x e^x)^3 \\
& - 366648282000 \sin(x e^x) (2 e^x + x e^x)^2 (3 e^x + x e^x) (5 e^x + x e^x) (4 e^x + x e^x)^2 \\
& - 244432188000 \sin(x e^x) (e^x + x e^x) (3 e^x + x e^x)^2 (5 e^x + x e^x) (4 e^x + x e^x)^2 \\
& - 122216094000 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x) (4 e^x + x e^x)^3 (5 e^x + x e^x) \\
& - 244432188000 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x) (3 e^x + x e^x) (6 e^x \\
& + x e^x) (4 e^x + x e^x)^2 - 325909584000 \sin(x e^x) (2 e^x + x e^x) (3 e^x + x e^x)^3 (5 e^x \\
& + x e^x) (4 e^x + x e^x) + 38798760 \sin(x e^x) (e^x + x e^x)^6 (10 e^x + x e^x) (4 e^x + x e^x) \\
& + 203693490000 \sin(x e^x) (2 e^x + x e^x)^4 (3 e^x + x e^x)^4 \\
& + 366648282000 \sin(x e^x) (2 e^x + x e^x)^5 (3 e^x + x e^x)^2 (4 e^x + x e^x) \\
& + 488864376000 \cos(x e^x) (e^x + x e^x) (2 e^x + x e^x)^5 (3 e^x + x e^x)^3 \\
& + 52378326000 \cos(x e^x) (2 e^x + x e^x)^7 (3 e^x + x e^x)^2 \\
& - 366648282000 \sin(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^6 (3 e^x + x e^x)^2 \\
& + 31426995600 \cos(x e^x) (e^x + x e^x) (2 e^x + x e^x)^7 (5 e^x + x e^x) \\
& - 78567489000 \sin(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^7 (4 e^x + x e^x) \\
& + 10475665200 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x)^6 (7 e^x + x e^x) \\
& + 581981400 \cos(x e^x) (2 e^x + x e^x)^3 (10 e^x + x e^x) (4 e^x + x e^x) \\
& + 1163962800 \cos(x e^x) (2 e^x + x e^x)^3 (9 e^x + x e^x) (5 e^x + x e^x) \\
& - 2909907000 \sin(x e^x) (2 e^x + x e^x)^4 (9 e^x + x e^x) (3 e^x + x e^x) \\
& - 1745944200 \cos(x e^x) (e^x + x e^x) (2 e^x + x e^x)^5 (9 e^x + x e^x) \\
& - 6547290750 \sin(x e^x) (2 e^x + x e^x)^4 (8 e^x + x e^x) (4 e^x + x e^x) \\
& - 10475665200 \sin(x e^x) (2 e^x + x e^x)^4 (7 e^x + x e^x) (5 e^x + x e^x) \\
& - 20951330400 \cos(x e^x) (2 e^x + x e^x)^5 (7 e^x + x e^x) (3 e^x + x e^x)
\end{aligned}$$

$$\begin{aligned}
& + 7856748900 \sin(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^5 (8 e^x + x e^x) \\
& - 38798760 \cos(x e^x) (4 e^x + x e^x) (10 e^x + x e^x) (6 e^x + x e^x) \\
& - 55426800 \cos(x e^x) (4 e^x + x e^x) (9 e^x + x e^x) (7 e^x + x e^x) \\
& + 969969000 \sin(x e^x) (3 e^x + x e^x) (4 e^x + x e^x)^2 (9 e^x + x e^x) \\
& + 290990700 \sin(x e^x) (2 e^x + x e^x) (4 e^x + x e^x)^2 (10 e^x + x e^x) \\
& + 4888643760 \sin(x e^x) (4 e^x + x e^x) (5 e^x + x e^x)^2 (6 e^x + x e^x) \\
& + 9777287520 \cos(x e^x) (e^x + x e^x) (4 e^x + x e^x) (5 e^x + x e^x)^3 \\
& + 775975200 \sin(x e^x) (3 e^x + x e^x)^2 (9 e^x + x e^x) (5 e^x + x e^x) \\
& + 2586584000 \cos(x e^x) (2 e^x + x e^x) (3 e^x + x e^x)^3 (9 e^x + x e^x) \\
& - 2586584000 \sin(x e^x) (e^x + x e^x)^2 (3 e^x + x e^x)^3 (9 e^x + x e^x) \\
& - 73329656400 \sin(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x)^6 (5 e^x + x e^x) \\
& - 38192529375 \sin(x e^x) (2 e^x + x e^x)^2 (4 e^x + x e^x)^4 \\
& - 6110804700 \sin(x e^x) (2 e^x + x e^x)^4 (6 e^x + x e^x)^2 - 3259095840 \sin(x e^x) (e^x \\
& + x e^x)^3 (5 e^x + x e^x) (6 e^x + x e^x)^2 + 997682400 \cos(x e^x) (2 e^x + x e^x)^3 (7 e^x \\
& + x e^x)^2 + 1745944200 \cos(x e^x) (2 e^x + x e^x)^3 (6 e^x + x e^x) (8 e^x + x e^x) \\
& + 3491888400 \sin(x e^x) (e^x + x e^x)^5 (4 e^x + x e^x)^2 (7 e^x + x e^x) \\
& + 775975200 \sin(x e^x) (e^x + x e^x)^5 (3 e^x + x e^x)^2 (9 e^x + x e^x) \\
& - 46558512000 \sin(x e^x) (2 e^x + x e^x)^2 (3 e^x + x e^x)^3 (7 e^x + x e^x) \\
& + 325909584000 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x)^2 (3 e^x + x e^x)^5 \\
& + 15519504000 \sin(x e^x) (e^x + x e^x)^4 (3 e^x + x e^x)^3 (7 e^x + x e^x) \\
& - 21727305600 \sin(x e^x) (e^x + x e^x)^6 (3 e^x + x e^x)^3 (5 e^x + x e^x) \\
& + 6547290750 \sin(x e^x) (e^x + x e^x)^8 (2 e^x + x e^x)^2 (4 e^x + x e^x)^2 \\
& + 48886437600 \sin(x e^x) (e^x + x e^x)^4 (3 e^x + x e^x)^2 (5 e^x + x e^x)^2 \\
& - 76385058750 \cos(x e^x) (2 e^x + x e^x)^4 (4 e^x + x e^x)^3 \\
& - 61108047000 \sin(x e^x) (2 e^x + x e^x)^3 (4 e^x + x e^x)^2 (6 e^x + x e^x) \\
& - 1330243200 \sin(x e^x) (e^x + x e^x)^7 (3 e^x + x e^x)^2 (7 e^x + x e^x) \\
& + 45831035250 \sin(x e^x) (2 e^x + x e^x)^6 (4 e^x + x e^x)^2 \\
& - 21998896920 \cos(x e^x) (2 e^x + x e^x)^5 (5 e^x + x e^x)^2 \\
& - 36664828200 \cos(x e^x) (2 e^x + x e^x)^5 (4 e^x + x e^x) (6 e^x + x e^x) \\
& + 109994484600 \sin(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^4 (5 e^x + x e^x)^2 \\
& - 2793510720 \sin(x e^x) (e^x + x e^x)^3 (5 e^x + x e^x)^2 (7 e^x + x e^x)
\end{aligned}$$

$$\begin{aligned}
& + 2909907000 \sin(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x)^4 (9 e^x + x e^x) \\
& - 969969000 \sin(x e^x) (e^x + x e^x)^3 (4 e^x + x e^x)^2 (9 e^x + x e^x) \\
& - 2182430250 \cos(x e^x) (e^x + x e^x)^4 (4 e^x + x e^x)^2 (8 e^x + x e^x) \\
& + 3259095840 \sin(x e^x) (e^x + x e^x)^5 (3 e^x + x e^x) (6 e^x + x e^x)^2 \\
& + 4888643760 \cos(x e^x) (e^x + x e^x)^6 (5 e^x + x e^x)^2 (4 e^x + x e^x) \\
& - 2793510720 \sin(x e^x) (e^x + x e^x)^7 (5 e^x + x e^x)^2 (3 e^x + x e^x) \\
& - 14665931280 \sin(x e^x) (e^x + x e^x)^6 (5 e^x + x e^x)^2 (2 e^x + x e^x)^2 \\
& + 1955457504 \sin(x e^x) (e^x + x e^x)^5 (5 e^x + x e^x)^3 + 969969000 \sin(x e^x) (e^x \\
& + x e^x)^9 (3 e^x + x e^x) (4 e^x + x e^x)^2 - 407386980000 \sin(x e^x) (e^x + x e^x)^4 (2 e^x \\
& + x e^x)^2 (3 e^x + x e^x)^4 + 543182640 \cos(x e^x) (e^x + x e^x)^2 (6 e^x + x e^x)^3 \\
& + 77597520 \sin(x e^x) (e^x + x e^x)^6 (9 e^x + x e^x) (5 e^x + x e^x) \\
& + 543182640 \sin(x e^x) (2 e^x + x e^x) (6 e^x + x e^x)^3 - 21727305600 \sin(x e^x) (e^x \\
& + x e^x)^5 (3 e^x + x e^x)^5 - 211629600 \cos(x e^x) (e^x + x e^x)^{11} (3 e^x + x e^x) (2 e^x + x e^x)^3 \\
& - 581981400 \sin(x e^x) (e^x + x e^x)^{10} (4 e^x + x e^x) (2 e^x + x e^x)^3 \\
& - 52907400 \sin(x e^x) (e^x + x e^x)^2 (12 e^x + x e^x) (2 e^x + x e^x)^3 \\
& - 26453700 \cos(x e^x) (e^x + x e^x)^4 (12 e^x + x e^x) (2 e^x + x e^x)^2 \\
& + 581981400 \sin(x e^x) (e^x + x e^x)^4 (10 e^x + x e^x) (2 e^x + x e^x)^3 \\
& + 116396280 \cos(x e^x) (e^x + x e^x)^6 (10 e^x + x e^x) (2 e^x + x e^x)^2 \\
& - 1995364800 \cos(x e^x) (e^x + x e^x)^7 (7 e^x + x e^x) (2 e^x + x e^x)^3 \\
& - 1745944200 \sin(x e^x) (e^x + x e^x)^6 (8 e^x + x e^x) (2 e^x + x e^x)^3 \\
& - 11639628000 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x)^2 (9 e^x + x e^x) (3 e^x + x e^x)^2 \\
& - 814773960000 \sin(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x)^4 (3 e^x + x e^x)^3 \\
& - 366648282000 \cos(x e^x) (e^x + x e^x)^4 (2 e^x + x e^x)^5 (3 e^x + x e^x)^2 \\
& - 52378326000 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^2 (3 e^x + x e^x)^2 (8 e^x + x e^x) \\
& + 139675536000 \sin(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x)^2 (3 e^x + x e^x)^2 (7 e^x + x e^x) \\
& + 1496523600 \cos(x e^x) (e^x + x e^x) (7 e^x + x e^x) (2 e^x + x e^x)^2 (8 e^x + x e^x) \\
& + 332560800 \cos(x e^x) (e^x + x e^x)^2 (7 e^x + x e^x) (2 e^x + x e^x) (9 e^x + x e^x) \\
& + 1629547920 \cos(x e^x) (e^x + x e^x)^6 (6 e^x + x e^x)^2 (2 e^x + x e^x) \\
& + 6518191680 \cos(x e^x) (e^x + x e^x)^6 (5 e^x + x e^x) (3 e^x + x e^x) (6 e^x + x e^x) \\
& - 2793510720 \sin(x e^x) (e^x + x e^x)^7 (5 e^x + x e^x) (2 e^x + x e^x) (6 e^x + x e^x) \\
& - 4655851200 \sin(x e^x) (e^x + x e^x)^7 (4 e^x + x e^x) (3 e^x + x e^x) (6 e^x + x e^x)
\end{aligned}$$

$$\begin{aligned}
& + 183324141000 \sin(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^4 (4 e^x + x e^x) (6 e^x + x e^x) \\
& + 3491888400 \sin(x e^x) (3 e^x + x e^x) (8 e^x + x e^x) (5 e^x + x e^x) (4 e^x + x e^x) \\
& - 23279256000 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x) (3 e^x + x e^x)^3 (8 e^x + x e^x) \\
& - 7759752000 \cos(x e^x) (e^x + x e^x)^3 (3 e^x + x e^x)^3 (8 e^x + x e^x) \\
& - 91662070500 \cos(x e^x) (e^x + x e^x)^4 (2 e^x + x e^x)^6 (4 e^x + x e^x) \\
& + 34918884000 \cos(x e^x) (2 e^x + x e^x) (4 e^x + x e^x)^2 (7 e^x + x e^x) (3 e^x + x e^x) \\
& - 203693490000 \sin(x e^x) (2 e^x + x e^x) (4 e^x + x e^x)^3 (3 e^x + x e^x)^2 \\
& + 40738698000 \cos(x e^x) (e^x + x e^x)^5 (4 e^x + x e^x)^3 (3 e^x + x e^x) \\
& - 73329656400 \cos(x e^x) (e^x + x e^x) (2 e^x + x e^x)^4 (5 e^x + x e^x) (6 e^x + x e^x) \\
& - 4655851200 \sin(x e^x) (e^x + x e^x)^3 (4 e^x + x e^x) (6 e^x + x e^x) (7 e^x + x e^x) \\
& - 4073869800 \cos(x e^x) (e^x + x e^x)^4 (4 e^x + x e^x) (6 e^x + x e^x)^2 \\
& - 13967553600 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x)^3 (6 e^x + x e^x) (7 e^x + x e^x) \\
& - 24443218800 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^3 (6 e^x + x e^x)^2 \\
& + 9777287520 \sin(x e^x) (e^x + x e^x)^5 (4 e^x + x e^x) (6 e^x + x e^x) (5 e^x + x e^x) \\
& + 4073869800 \cos(x e^x) (e^x + x e^x)^6 (4 e^x + x e^x)^2 (6 e^x + x e^x) \\
& + 17459442000 \sin(x e^x) (e^x + x e^x)^4 (3 e^x + x e^x)^2 (8 e^x + x e^x) (2 e^x + x e^x) \\
& + 3491888400 \sin(x e^x) (e^x + x e^x)^5 (3 e^x + x e^x) (8 e^x + x e^x) (4 e^x + x e^x) \\
& + 1163962800 \cos(x e^x) (e^x + x e^x)^6 (3 e^x + x e^x)^2 (8 e^x + x e^x) \\
& - 54318264000 \sin(x e^x) (2 e^x + x e^x) (3 e^x + x e^x)^4 (6 e^x + x e^x) \\
& + 1629547920000 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x)^3 (3 e^x + x e^x)^3 (4 e^x + x e^x) \\
& + 814773960000 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^3 (3 e^x + x e^x)^4 \\
& + 10475665200 \cos(x e^x) (e^x + x e^x)^5 (3 e^x + x e^x) (8 e^x + x e^x) (2 e^x + x e^x)^2 \\
& - 13967553600 \sin(x e^x) (e^x + x e^x)^6 (3 e^x + x e^x) (7 e^x + x e^x) (2 e^x + x e^x)^2 \\
& - 229155176250 \sin(x e^x) (e^x + x e^x)^4 (2 e^x + x e^x)^4 (4 e^x + x e^x)^2 \\
& - 40738698000 \sin(x e^x) (e^x + x e^x)^6 (3 e^x + x e^x)^2 (4 e^x + x e^x)^2 \\
& - 20951330400 \cos(x e^x) (e^x + x e^x)^7 (2 e^x + x e^x)^2 (5 e^x + x e^x) (4 e^x + x e^x) \\
& + 10475665200 \sin(x e^x) (e^x + x e^x)^8 (2 e^x + x e^x)^2 (5 e^x + x e^x) (3 e^x + x e^x) \\
& + 916620705000 \sin(x e^x) (e^x + x e^x) (2 e^x + x e^x)^4 (3 e^x + x e^x) (4 e^x + x e^x)^2 \\
& + 36664828200 \cos(x e^x) (2 e^x + x e^x) (4 e^x + x e^x)^2 (5 e^x + x e^x)^2 \\
& - 73329656400 \sin(x e^x) (2 e^x + x e^x)^3 (4 e^x + x e^x) (5 e^x + x e^x)^2 \\
& + 4655851200 \cos(x e^x) (e^x + x e^x)^6 (3 e^x + x e^x) (7 e^x + x e^x) (4 e^x + x e^x)
\end{aligned}$$

$$\begin{aligned}
& + 1745944200 \sin(x e^x) (e^x + x e^x)^8 (6 e^x + x e^x) (2 e^x + x e^x)^3 \\
& + 116396280 \cos(x e^x) (e^x + x e^x)^{10} (6 e^x + x e^x) (2 e^x + x e^x)^2 \\
& - 997682400 \cos(x e^x) (e^x + x e^x)^8 (3 e^x + x e^x) (7 e^x + x e^x) (2 e^x + x e^x) \\
& + 2793510720 \cos(x e^x) (e^x + x e^x)^2 (5 e^x + x e^x) (7 e^x + x e^x) (6 e^x + x e^x) \\
& - 11639628000 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x)^3 (9 e^x + x e^x) (3 e^x + x e^x) \\
& + 1163962800 \cos(x e^x) (e^x + x e^x)^2 (4 e^x + x e^x) (9 e^x + x e^x) (5 e^x + x e^x) \\
& - 1745944200 \cos(x e^x) (e^x + x e^x)^8 (4 e^x + x e^x) (2 e^x + x e^x) (6 e^x + x e^x) \\
& - 3491888400 \cos(x e^x) (e^x + x e^x)^8 (4 e^x + x e^x) (3 e^x + x e^x) (5 e^x + x e^x) \\
& + 105814800 \cos(x e^x) (e^x + x e^x) (2 e^x + x e^x)^2 (12 e^x + x e^x) (3 e^x + x e^x) \\
& - 13967553600 \cos(x e^x) (e^x + x e^x)^3 (6 e^x + x e^x) (2 e^x + x e^x)^2 (7 e^x + x e^x) \\
& + 465585120 \cos(x e^x) (e^x + x e^x)^{10} (5 e^x + x e^x) (3 e^x + x e^x) (2 e^x + x e^x) \\
& - 6983776800 \cos(x e^x) (e^x + x e^x)^4 (4 e^x + x e^x) (7 e^x + x e^x) (5 e^x + x e^x) \\
& - 1939938000 \cos(x e^x) (e^x + x e^x)^4 (3 e^x + x e^x) (9 e^x + x e^x) (4 e^x + x e^x) \\
& - 3491888400 \cos(x e^x) (e^x + x e^x)^4 (3 e^x + x e^x) (8 e^x + x e^x) (5 e^x + x e^x) \\
& - 4655851200 \cos(x e^x) (e^x + x e^x)^4 (3 e^x + x e^x) (7 e^x + x e^x) (6 e^x + x e^x) \\
& + 5587021440 \sin(x e^x) (e^x + x e^x)^5 (3 e^x + x e^x) (7 e^x + x e^x) (5 e^x + x e^x) \\
& - 4888643760 \cos(x e^x) (e^x + x e^x)^4 (5 e^x + x e^x)^2 (6 e^x + x e^x) \\
& - 41902660800 \cos(x e^x) (e^x + x e^x)^2 (5 e^x + x e^x) (2 e^x + x e^x)^3 (7 e^x + x e^x) \\
& - 26189163000 \cos(x e^x) (e^x + x e^x)^2 (4 e^x + x e^x) (2 e^x + x e^x)^3 (8 e^x + x e^x) \\
& + 69837768000 \sin(x e^x) (e^x + x e^x)^3 (4 e^x + x e^x) (2 e^x + x e^x)^3 (7 e^x + x e^x) \\
& - 7759752000 \cos(x e^x) (e^x + x e^x)^3 (3 e^x + x e^x)^2 (9 e^x + x e^x) (2 e^x + x e^x) \\
& + 34918884000 \sin(x e^x) (e^x + x e^x)^3 (3 e^x + x e^x) (8 e^x + x e^x) (2 e^x + x e^x)^3 \\
& - 1163962800 \cos(x e^x) (e^x + x e^x)^8 (3 e^x + x e^x)^2 (6 e^x + x e^x) \\
& - 1047566520 \cos(x e^x) (e^x + x e^x)^8 (2 e^x + x e^x) (5 e^x + x e^x)^2 \\
& + 35271600 \cos(x e^x) (e^x + x e^x)^2 (3 e^x + x e^x)^2 (12 e^x + x e^x) \\
& + 52907400 \cos(x e^x) (e^x + x e^x)^2 (2 e^x + x e^x) (12 e^x + x e^x) (4 e^x + x e^x) \\
& - 2327925600 \sin(x e^x) (e^x + x e^x)^3 (3 e^x + x e^x) (6 e^x + x e^x) (8 e^x + x e^x) \\
& - 5237832600 \sin(x e^x) (e^x + x e^x)^2 (6 e^x + x e^x) (2 e^x + x e^x)^2 (8 e^x + x e^x) \\
& + 217273056000 \cos(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x) (3 e^x + x e^x)^5 \\
& + 1745944200 \sin(x e^x) (2 e^x + x e^x) (4 e^x + x e^x) (8 e^x + x e^x) (6 e^x + x e^x) \\
& + 775975200 \sin(x e^x) (e^x + x e^x)^9 (5 e^x + x e^x) (3 e^x + x e^x)^2
\end{aligned}$$

$$\begin{aligned}
& -10475665200 \sin(x e^x) (e^x + x e^x) (5 e^x + x e^x) (2 e^x + x e^x)^3 (8 e^x + x e^x) \\
& -10475665200 \cos(x e^x) (e^x + x e^x)^3 (5 e^x + x e^x) (2 e^x + x e^x)^2 (8 e^x + x e^x) \\
& -5819814000 \cos(x e^x) (e^x + x e^x)^3 (4 e^x + x e^x) (2 e^x + x e^x)^2 (9 e^x + x e^x) \\
& +13094581500 \sin(x e^x) (e^x + x e^x)^4 (4 e^x + x e^x) (2 e^x + x e^x)^2 (8 e^x + x e^x) \\
& +423259200 \cos(x e^x) (e^x + x e^x) (3 e^x + x e^x)^2 (11 e^x + x e^x) (2 e^x + x e^x) \\
& -2327925600 \sin(x e^x) (e^x + x e^x)^2 (3 e^x + x e^x)^2 (10 e^x + x e^x) (2 e^x + x e^x) \\
& -2327925600 \cos(x e^x) (e^x + x e^x)^3 (3 e^x + x e^x) (10 e^x + x e^x) (2 e^x + x e^x)^2 \\
& +5819814000 \sin(x e^x) (e^x + x e^x)^4 (3 e^x + x e^x) (9 e^x + x e^x) (2 e^x + x e^x)^2 \\
& +1745944200 \cos(x e^x) (e^x + x e^x)^2 (4 e^x + x e^x) (8 e^x + x e^x) (6 e^x + x e^x) \\
& -3491888400 \sin(x e^x) (e^x + x e^x)^3 (4 e^x + x e^x) (8 e^x + x e^x) (5 e^x + x e^x) \\
& +211629600 \cos(x e^x) (e^x + x e^x)^2 (3 e^x + x e^x) (11 e^x + x e^x) (4 e^x + x e^x) \\
& +465585120 \cos(x e^x) (e^x + x e^x)^2 (3 e^x + x e^x) (10 e^x + x e^x) (5 e^x + x e^x) \\
& -775975200 \sin(x e^x) (e^x + x e^x)^3 (3 e^x + x e^x) (10 e^x + x e^x) (4 e^x + x e^x) \\
& +775975200 \cos(x e^x) (e^x + x e^x)^2 (3 e^x + x e^x) (9 e^x + x e^x) (6 e^x + x e^x) \\
& -1551950400 \sin(x e^x) (e^x + x e^x)^3 (3 e^x + x e^x) (9 e^x + x e^x) (5 e^x + x e^x) \\
& +1163962800 \cos(x e^x) (e^x + x e^x) (6 e^x + x e^x) (2 e^x + x e^x)^2 (9 e^x + x e^x) \\
& +698377680 \cos(x e^x) (e^x + x e^x) (5 e^x + x e^x) (2 e^x + x e^x)^2 (10 e^x + x e^x) \\
& -3491888400 \sin(x e^x) (e^x + x e^x)^2 (5 e^x + x e^x) (2 e^x + x e^x)^2 (9 e^x + x e^x) \\
& +317444400 \cos(x e^x) (e^x + x e^x) (4 e^x + x e^x) (2 e^x + x e^x)^2 (11 e^x + x e^x) \\
& -1745944200 \sin(x e^x) (e^x + x e^x)^2 (4 e^x + x e^x) (2 e^x + x e^x)^2 (10 e^x + x e^x) \\
& -1745944200 \cos(x e^x) (e^x + x e^x)^4 (6 e^x + x e^x) (2 e^x + x e^x) (8 e^x + x e^x) \\
& +2793510720 \sin(x e^x) (e^x + x e^x)^5 (6 e^x + x e^x) (2 e^x + x e^x) (7 e^x + x e^x) \\
& -1163962800 \cos(x e^x) (e^x + x e^x)^4 (5 e^x + x e^x) (2 e^x + x e^x) (9 e^x + x e^x) \\
& +2095133040 \sin(x e^x) (e^x + x e^x)^5 (5 e^x + x e^x) (2 e^x + x e^x) (8 e^x + x e^x) \\
& -634888800 \sin(x e^x) (e^x + x e^x)^2 (3 e^x + x e^x) (11 e^x + x e^x) (2 e^x + x e^x)^2 \\
& -211629600 \cos(x e^x) (e^x + x e^x)^4 (3 e^x + x e^x) (11 e^x + x e^x) (2 e^x + x e^x) \\
& -387987600 \cos(x e^x) (e^x + x e^x)^4 (3 e^x + x e^x)^2 (10 e^x + x e^x) \\
& +997682400 \sin(x e^x) (2 e^x + x e^x) (4 e^x + x e^x) (7 e^x + x e^x)^2 \\
& +155195040 \sin(x e^x) (e^x + x e^x) (3 e^x + x e^x) (6 e^x + x e^x) (10 e^x + x e^x) \\
& -325909584000 \cos(x e^x) (e^x + x e^x)^5 (2 e^x + x e^x)^3 (3 e^x + x e^x)^3 \\
& -54318264000 \cos(x e^x) (e^x + x e^x)^6 (3 e^x + x e^x)^4 (2 e^x + x e^x)
\end{aligned}$$

$$\begin{aligned}
& -77597520 \cos(x e^x) (e^x + x e^x)^9 (5 e^x + x e^x) (6 e^x + x e^x) \\
& -99768240 \cos(x e^x) (e^x + x e^x)^5 (7 e^x + x e^x) (8 e^x + x e^x) \\
& +46558512000 \sin(x e^x) (e^x + x e^x)^7 (3 e^x + x e^x)^3 (2 e^x + x e^x)^2 \\
& +2586584000 \cos(x e^x) (e^x + x e^x)^9 (3 e^x + x e^x)^3 (2 e^x + x e^x) \\
& +387987600 \cos(x e^x) (e^x + x e^x)^{10} (3 e^x + x e^x)^2 (4 e^x + x e^x) \\
& +290990700 \cos(x e^x) (e^x + x e^x)^{10} (4 e^x + x e^x)^2 (2 e^x + x e^x) \\
& +6547290750 \cos(x e^x) (e^x + x e^x)^4 (2 e^x + x e^x)^4 (8 e^x + x e^x) \\
& -775975200 \sin(x e^x) (e^x + x e^x)^3 (6 e^x + x e^x) (9 e^x + x e^x) (2 e^x + x e^x) \\
& -77597520 \cos(x e^x) (e^x + x e^x)^5 (6 e^x + x e^x) (9 e^x + x e^x) \\
& +775975200 \sin(x e^x) (2 e^x + x e^x) (6 e^x + x e^x) (9 e^x + x e^x) (3 e^x + x e^x) \\
& +465585120 \sin(x e^x) (2 e^x + x e^x) (5 e^x + x e^x) (10 e^x + x e^x) (3 e^x + x e^x) \\
& +211629600 \sin(x e^x) (2 e^x + x e^x) (4 e^x + x e^x) (11 e^x + x e^x) (3 e^x + x e^x) \\
& -36664828200 \sin(x e^x) (e^x + x e^x)^4 (2 e^x + x e^x)^5 (6 e^x + x e^x) \\
& -12221609400 \cos(x e^x) (e^x + x e^x)^6 (2 e^x + x e^x)^4 (6 e^x + x e^x) \\
& +498841200 \sin(x e^x) (e^x + x e^x) (4 e^x + x e^x) (7 e^x + x e^x) (8 e^x + x e^x) \\
& +221707200 \sin(x e^x) (e^x + x e^x) (3 e^x + x e^x) (7 e^x + x e^x) (9 e^x + x e^x) \\
& +232792560 \cos(x e^x) (e^x + x e^x)^2 (6 e^x + x e^x) (10 e^x + x e^x) (2 e^x + x e^x) \\
& +126977760 \cos(x e^x) (e^x + x e^x)^2 (5 e^x + x e^x) (11 e^x + x e^x) (2 e^x + x e^x) \\
& -465585120 \sin(x e^x) (e^x + x e^x)^3 (5 e^x + x e^x) (10 e^x + x e^x) (2 e^x + x e^x) \\
& -46558512 \cos(x e^x) (e^x + x e^x)^5 (5 e^x + x e^x) (10 e^x + x e^x) \\
& -211629600 \sin(x e^x) (e^x + x e^x)^3 (4 e^x + x e^x) (11 e^x + x e^x) (2 e^x + x e^x) \\
& +35271600 \sin(x e^x) (e^x + x e^x) (3 e^x + x e^x) (4 e^x + x e^x) (12 e^x + x e^x) \\
& +84651840 \sin(x e^x) (e^x + x e^x) (3 e^x + x e^x) (5 e^x + x e^x) (11 e^x + x e^x) \\
& +997682400 \sin(x e^x) (2 e^x + x e^x) (3 e^x + x e^x) (8 e^x + x e^x) (7 e^x + x e^x) \\
& +10475665200 \sin(x e^x) (e^x + x e^x)^7 (5 e^x + x e^x) (2 e^x + x e^x)^4 \\
& +1163962800 \cos(x e^x) (e^x + x e^x)^9 (5 e^x + x e^x) (2 e^x + x e^x)^3 \\
& -1163962800 \sin(x e^x) (e^x + x e^x)^{10} (3 e^x + x e^x)^2 (2 e^x + x e^x)^2 \\
& +35271600 \sin(x e^x) (2 e^x + x e^x) (12 e^x + x e^x) (3 e^x + x e^x)^2 \\
& +1163962800 \cos(x e^x) (e^x + x e^x)^5 (9 e^x + x e^x) (2 e^x + x e^x)^3 \\
& -43997793840 \cos(x e^x) (e^x + x e^x)^5 (2 e^x + x e^x)^5 (5 e^x + x e^x) \\
& +6547290750 \cos(x e^x) (e^x + x e^x)^8 (2 e^x + x e^x)^4 (4 e^x + x e^x) \\
& +17459442000 \cos(x e^x) (e^x + x e^x)^8 (2 e^x + x e^x)^3 (3 e^x + x e^x)^2
\end{aligned}$$

$$\begin{aligned}
& -21162960 \cos(x e^x) (e^x + x e^x)^5 (11 e^x + x e^x) (4 e^x + x e^x) \\
& + 116396280 \sin(x e^x) (e^x + x e^x)^6 (6 e^x + x e^x) (8 e^x + x e^x) \\
& - 38798760 \sin(x e^x) (e^x + x e^x)^4 (6 e^x + x e^x) (10 e^x + x e^x) \\
& - 141086400 \sin(x e^x) (e^x + x e^x)^3 (3 e^x + x e^x)^2 (11 e^x + x e^x) \\
& + 166280400 \sin(x e^x) (2 e^x + x e^x)^2 (7 e^x + x e^x) (9 e^x + x e^x) \\
& + 116396280 \sin(x e^x) (2 e^x + x e^x)^2 (6 e^x + x e^x) (10 e^x + x e^x) \\
& + 63488880 \sin(x e^x) (2 e^x + x e^x)^2 (5 e^x + x e^x) (11 e^x + x e^x) \\
& + 26453700 \sin(x e^x) (2 e^x + x e^x)^2 (4 e^x + x e^x) (12 e^x + x e^x) \\
& - 10475665200 \sin(x e^x) (e^x + x e^x)^5 (2 e^x + x e^x)^4 (7 e^x + x e^x) \\
& - 211629600 \cos(x e^x) (e^x + x e^x)^3 (2 e^x + x e^x)^3 (11 e^x + x e^x) \\
& - 1309458150 \sin(x e^x) (e^x + x e^x)^8 (2 e^x + x e^x)^6 - 2909907000 \sin(x e^x) (e^x \\
& + x e^x)^9 (2 e^x + x e^x)^4 (3 e^x + x e^x) - 174594420 \cos(x e^x) (e^x + x e^x)^{10} (2 e^x + x e^x)^5 \\
& - 21162960 \sin(x e^x) (e^x + x e^x)^4 (5 e^x + x e^x) (11 e^x + x e^x)
\end{aligned}$$

Um sistema pioneiro foi desenvolvido pelo Prêmio Nobel de Física de 1963, Martin Veltman, que construiu o programa *Schoonship* para cálculos em Física de Altas Energias. Os CAS's começaram a ser desenvolvidos e difundidos a partir da década de 1970. Inicialmente um ramo da pesquisa em inteligência artificial, atualmente é um campo de pesquisa independente desta.

Os primeiros sistemas de uso geral de maior difusão foram o Reduce, Derive, e Macsyma, que ainda hoje estão disponíveis. Atualmente, os líderes de mercado são o Maple e o Mathematica, seguidos pelos MuPAD e MathCad; são utilizados por matemáticos, físicos, engenheiros e outros profissionais. Há sistemas de uso mais específico, acadêmicos, geralmente gratuitos.

II. Operações básicas e comandos elementares

$$\begin{array}{lcl}
> 1+1; & 2 & (2.1) \\
\end{array}$$

$$\begin{array}{lcl}
> 3-4; & -1 & (2.2) \\
\end{array}$$

$$\begin{array}{lcl}
> 4/2; & 2 & (2.3) \\
\end{array}$$

$$\begin{array}{lcl}
> \text{sqrt}(16); & 4 & (2.4) \\
\end{array}$$

$$\begin{array}{lcl}
> 8*7; & 56 & (2.5) \\
\end{array}$$

$$\begin{array}{lcl}
> a+b; & a + b & (2.6) \\
\end{array}$$

$$> 2/3; \quad \frac{2}{3} \quad (2.7)$$

Números inteiros versus números não-inteiros

$$> 2./3; \quad 0.66666666667 \quad (2.8)$$

```
> evalf(2/3);
```

Número de casas decimais padrão 10.

```
> Digits:=50;  
Digits := 50  
(2.10)
```

```
> evalf(Pi);  
3.1415926535897932384626433832795028841971693993751 (2.12)
```

```
> evalf(exp(1));  
2.7182818284590452353602874712526624977572470027000  
(2.12)
```

```
> restart:
```

III. Manipulando expressões algébricas

Examinando os comandos SUBS, EXPAND, SIMPLIFY, COLLECT

$$> \textcolor{red}{f := x^3 + 2*x^2 - 5*x + 4; } \quad f := x^3 + 2\,x^2 - 5\,x + 4 \quad (3.1)$$

```
> subs(x=4, f);
```

```
> g:=sin(a+b);
```

```
> expand(g);

$$g = \frac{1}{2}x^2 - \frac{1}{2}y^2 + \frac{1}{2}z^2 + \frac{1}{2}w^2$$
 (2.4)
```

```
> sin(a)^2+cos(a)^2;
```

```
> simplify(sin(a)^2+cos(a)^2);
```

= > h:=a*ln(x)-ln(x)*x-x;

$= \text{collect}(h, \ln(x)):$

$$= \sigma := x^2 \exp(x) - 2x \exp(x) + 2 \exp(x) - x^2 / \exp(x) - 2x / \exp(x)$$

$$\begin{aligned} & -2/\exp(x); \\ & g := x^2 e^x - 2 x e^x + 2 e^x - \frac{x^2}{e^x} - \frac{2 x}{e^x} - \frac{2}{e^x} \end{aligned} \quad (3.9)$$

$$\begin{aligned} > \text{collect}(g, \exp(x)); \\ & (2 + x^2 - 2 x) e^x + \frac{-2 x - 2 - x^2}{e^x} \end{aligned} \quad (3.10)$$

> restart:

IV. Gráfico de funções de uma ou mais variáveis

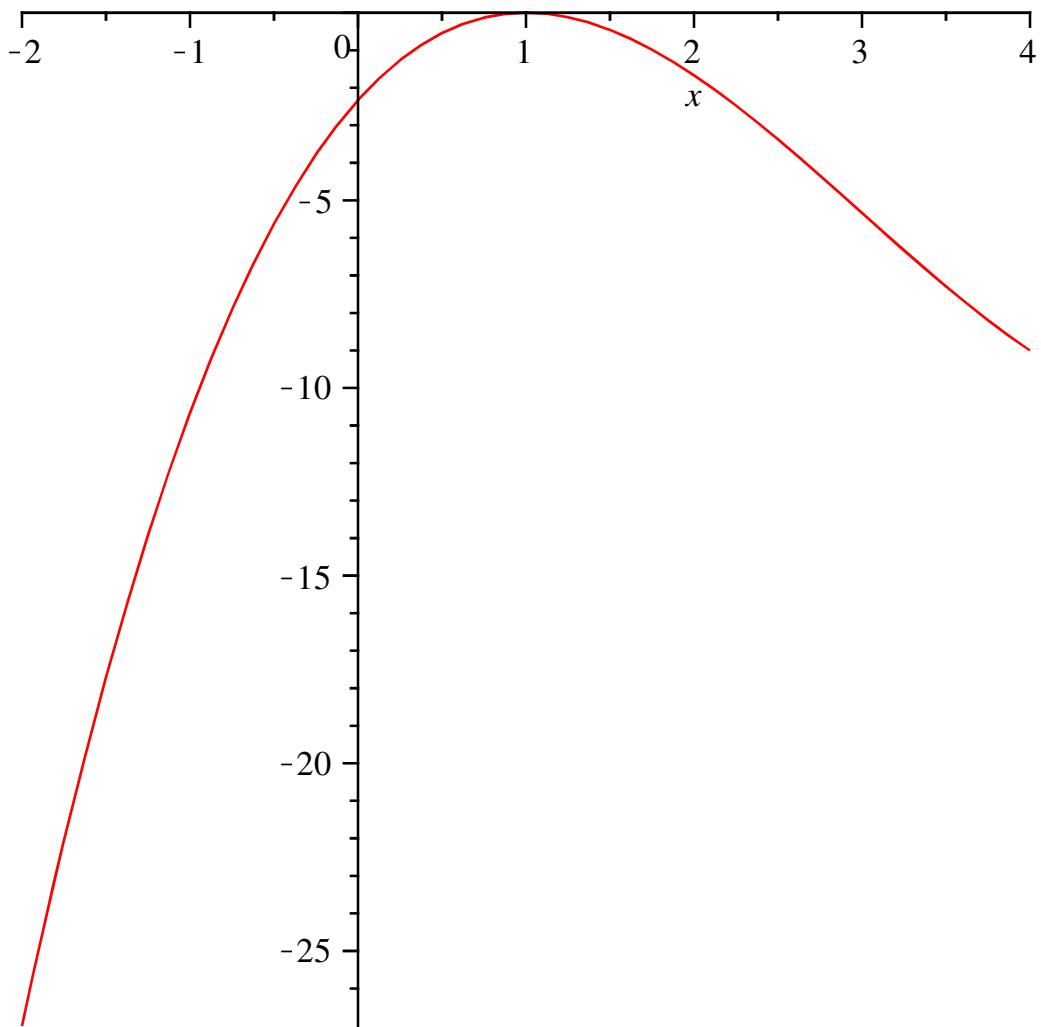
O Maple possui um pacote denominado PLOTS que contém um conjunto de ferramentas para construção de gráficos de funções em uma ou mais variáveis. Vamos conhecê-lo.

```
> with(plots);
[animate, animate3d, animatecurve, arrow, changecoords, complexplot, complexplot3d,
conformal, conformal3d, contourplot, contourplot3d, coordplot, coordplot3d,
densityplot, display, dualaxisplot, fieldplot, fieldplot3d, gradplot, gradplot3d,
graphplot3d, implicitplot, implicitplot3d, inequal, interactive, interactiveparams,
intersectplot, listcontplot, listcontplot3d, listdensityplot, listplot, listplot3d, loglogplot,
logplot, matrixplot, multiple, odeplot, pareto, plotcompare, pointplot, pointplot3d,
polarplot, polygonplot, polygonplot3d, polyhedra_supported, polyhedraplot, rootlocus,
semilogplot, setcolors, setoptions, setoptions3d, spacecurve, sparsematrixplot, surldata,
textplot, textplot3d, tubeplot]
```

$$\begin{aligned} > f := 1/3*x^3 - 6/2*x^2 + 5*x - 7/3; \\ & f := \frac{1}{3} x^3 - 3 x^2 + 5 x - \frac{7}{3} \end{aligned} \quad (4.2)$$

O Maple pode facilmente plotar o gráfico desta função polinomial

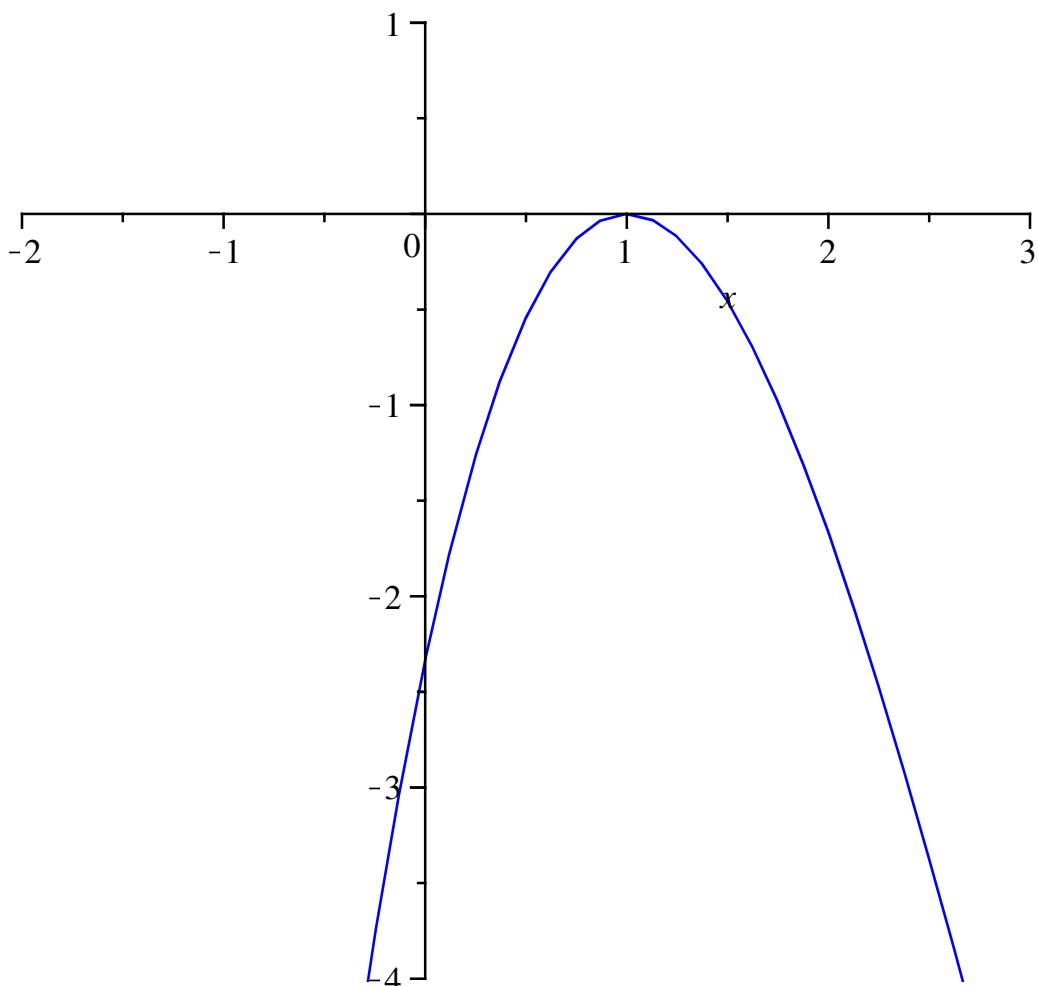
> plot(f, x=-2..4);



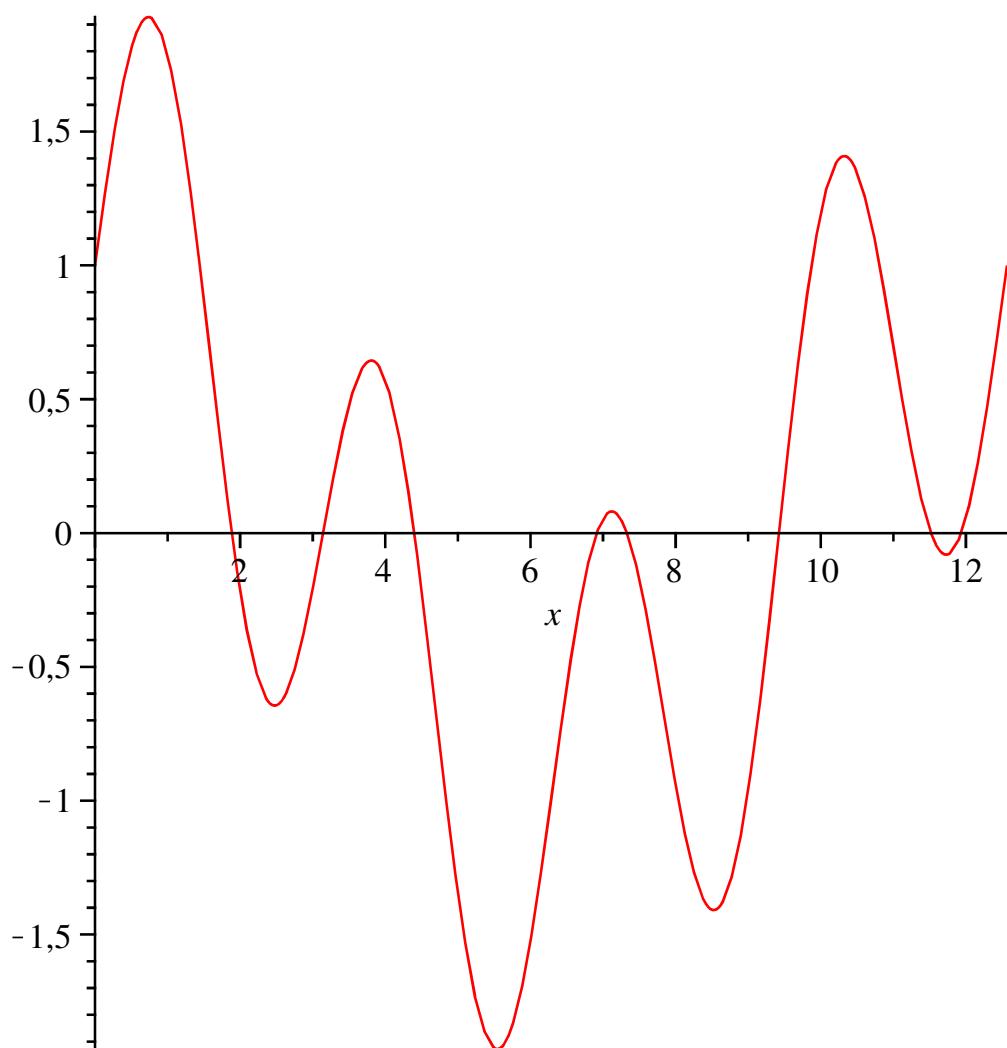
Mas como saber se o comportamento da função constitui uma curva com concavidade voltada para baixo? A resposta a essa pergunta será respondida mais adiante. Ainda nesta função.

```
> plot(f,x=-2..4,view=[-2..3,-4..1],color=blue,title=
`Polinômio`);
```

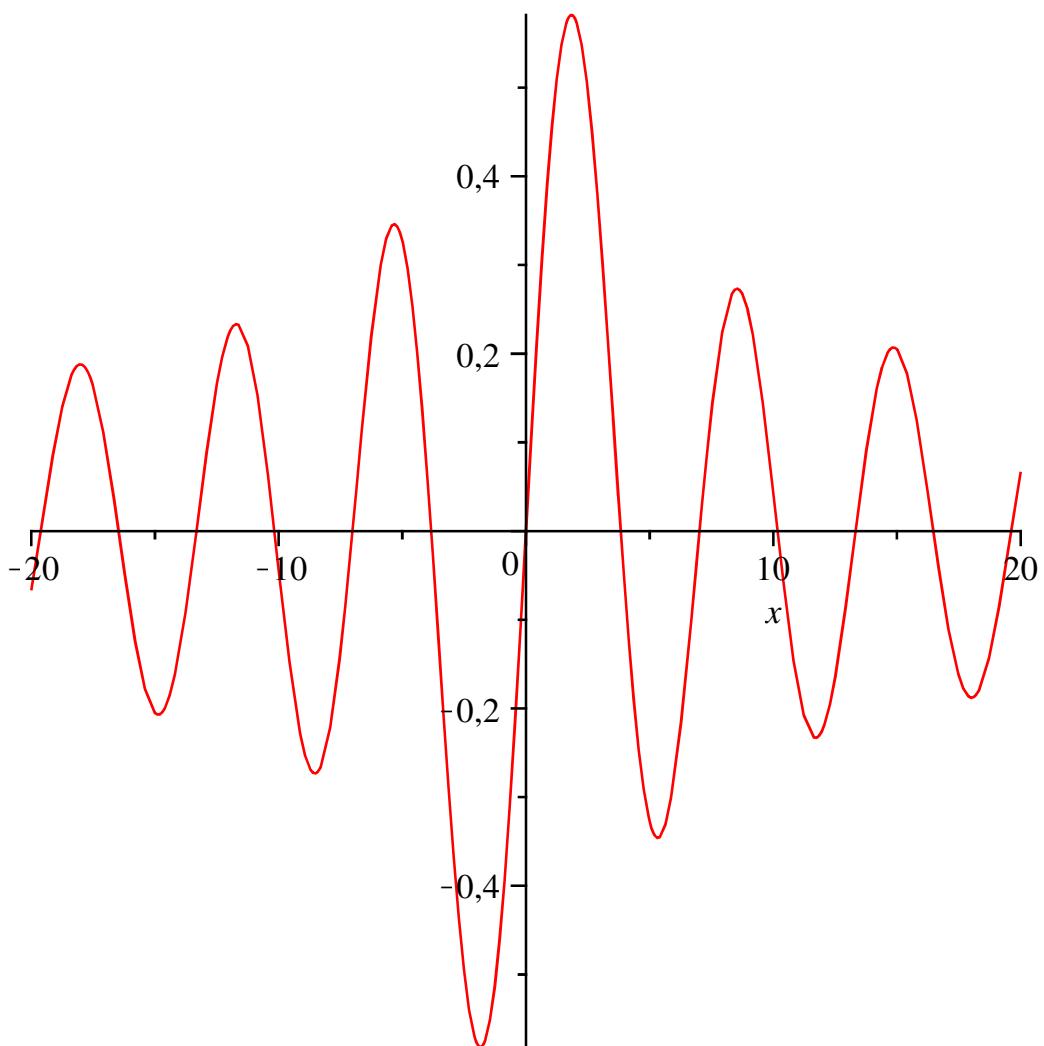
Polinômio



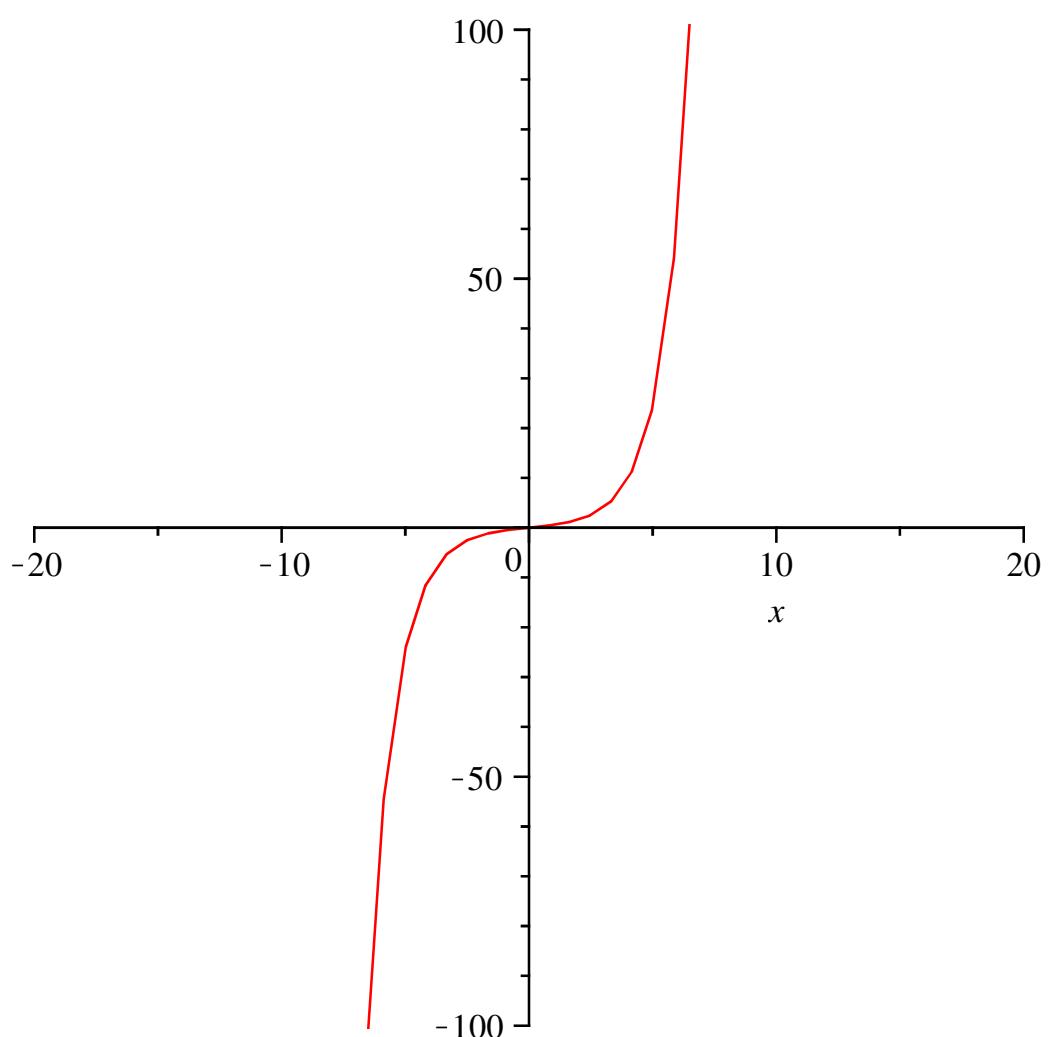
```
> plot(cos((1/2)*x)+sin(2*x),x = 0 .. 4*pi);
```



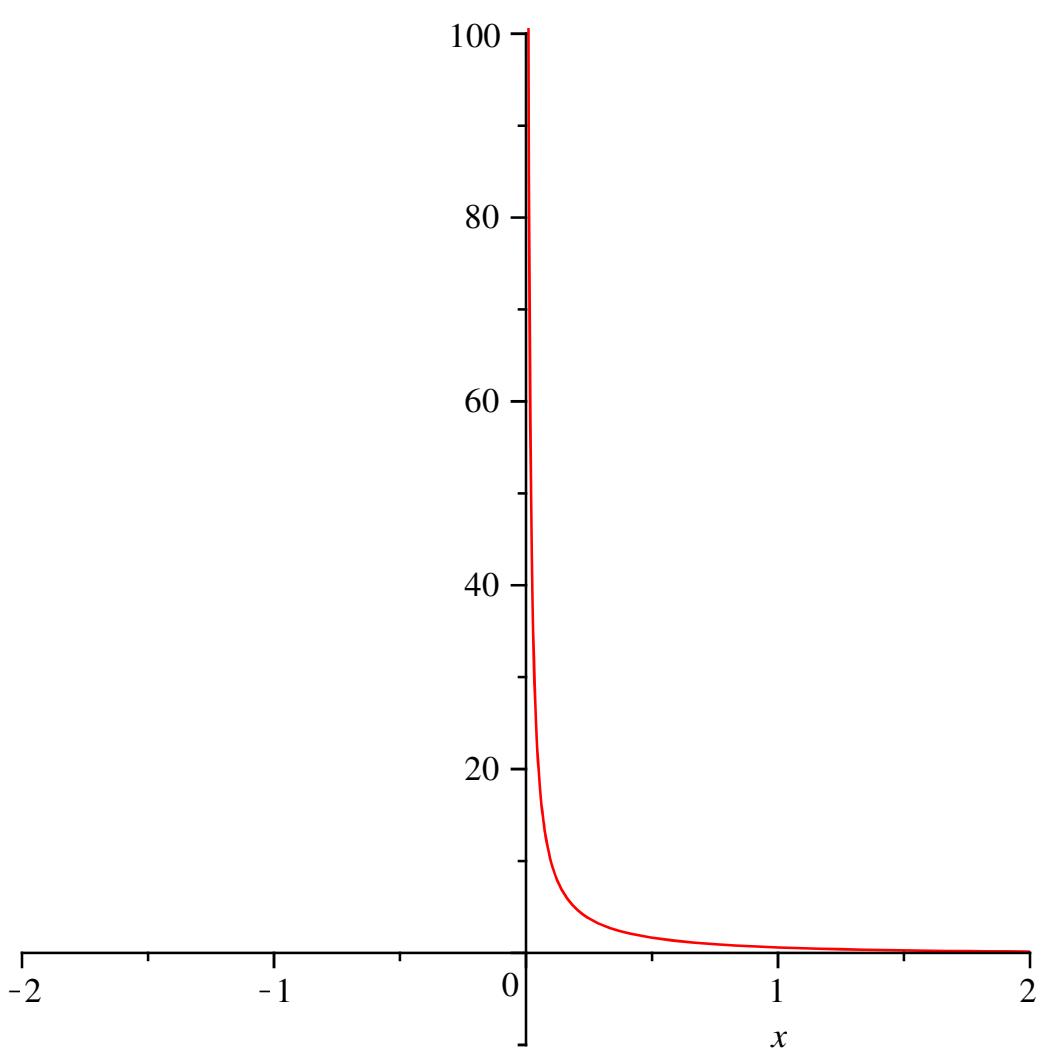
```
> plot(BesselJ(1, x), x = -20 .. 20);
```



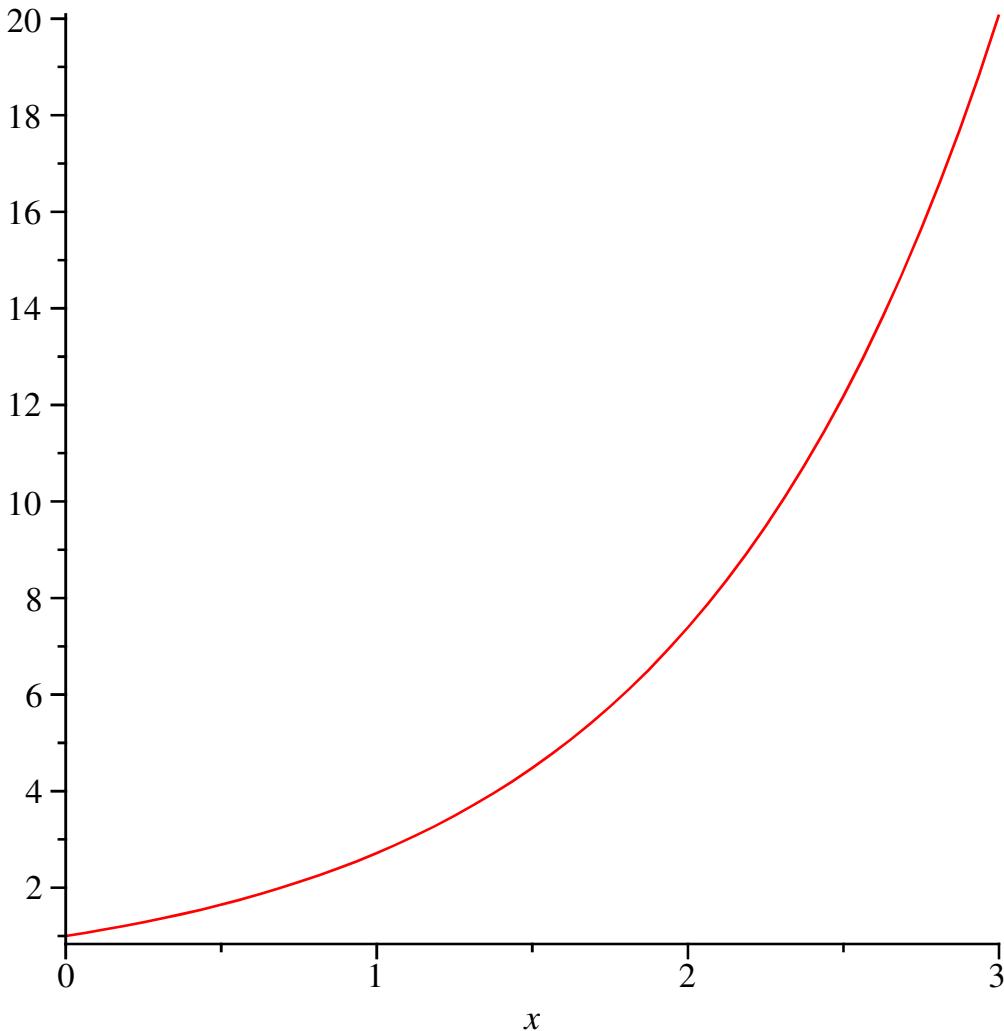
```
> plot(BesselI(1, x), x = -20 .. 20, -100..100);
```



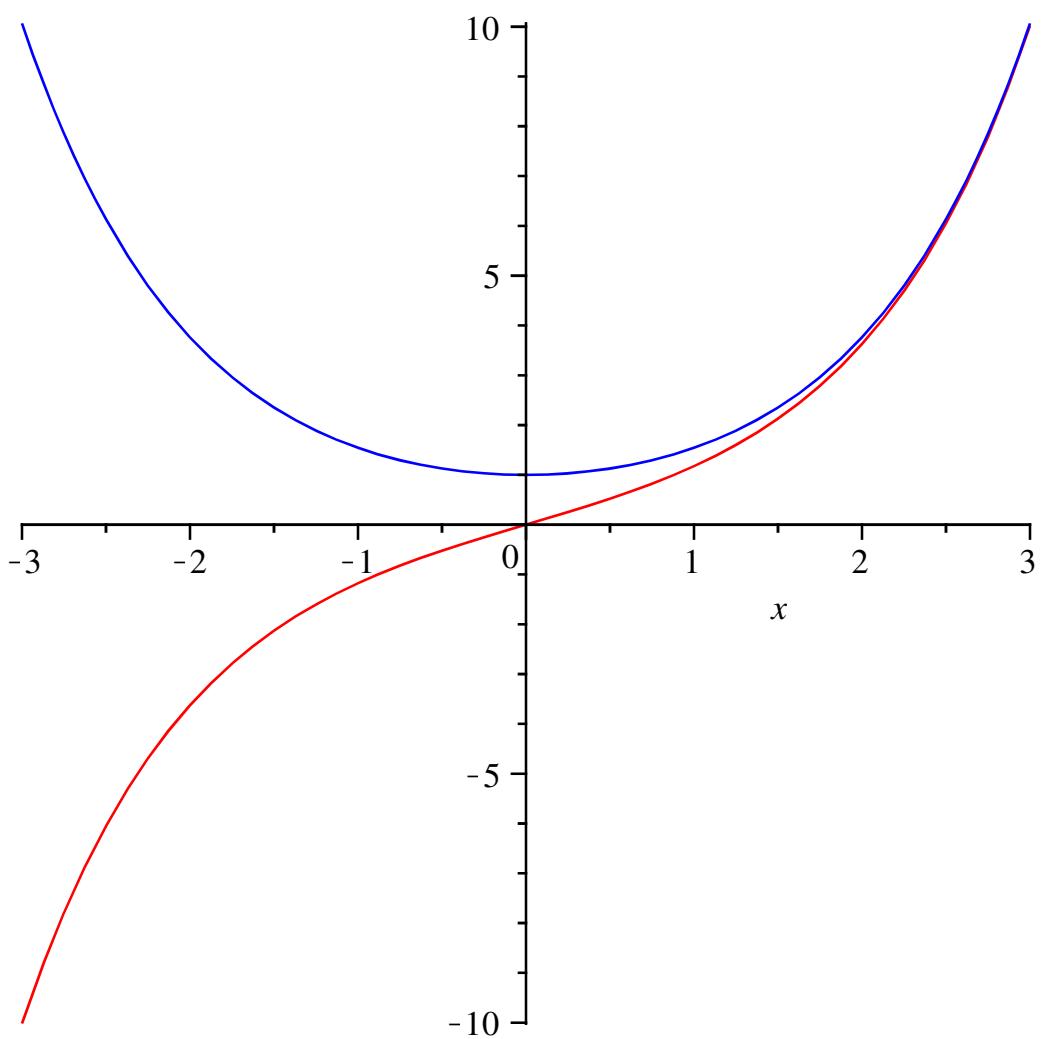
```
> plot(BesselK(1, x), x = -2 .. 2, -10..100);
```



```
> plot(exp(x), x=0..3);
```

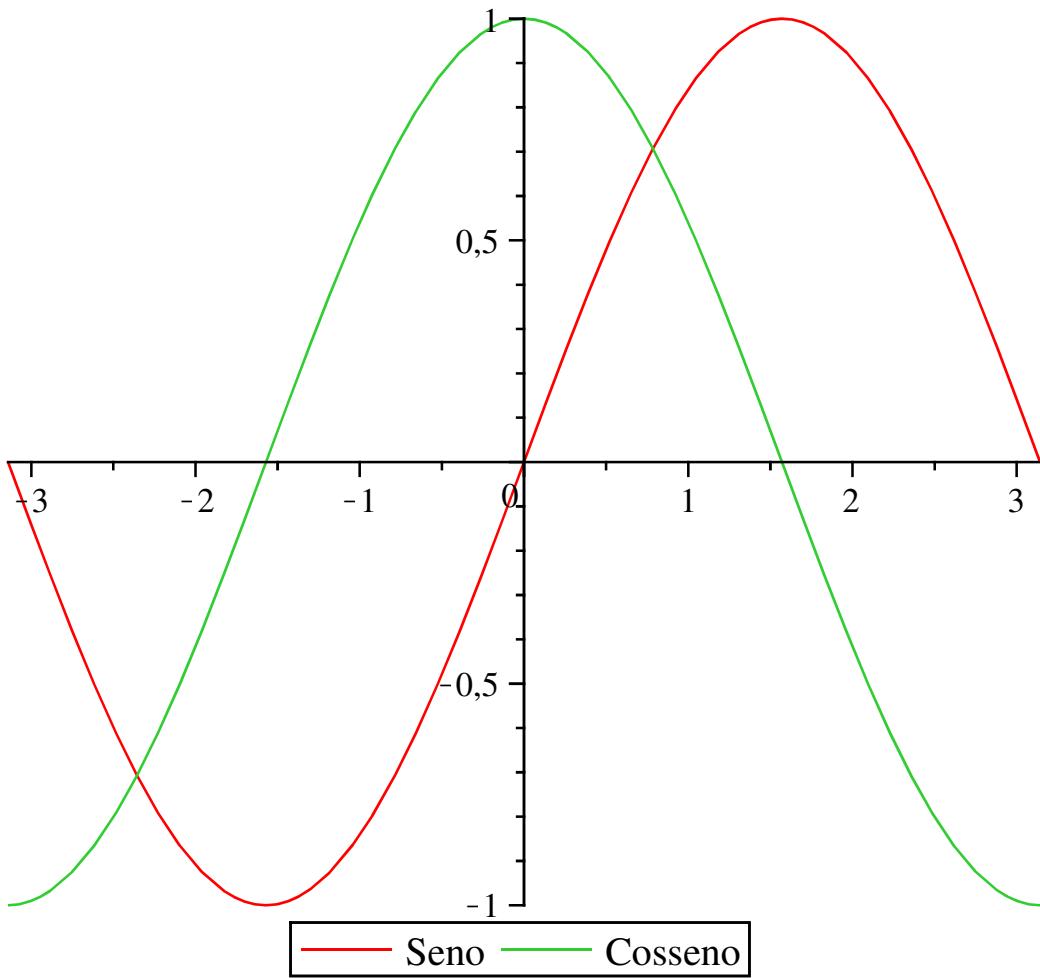


```
> plot([sinh(x),cosh(x)],x=-3..3,color=[red,blue]);
```

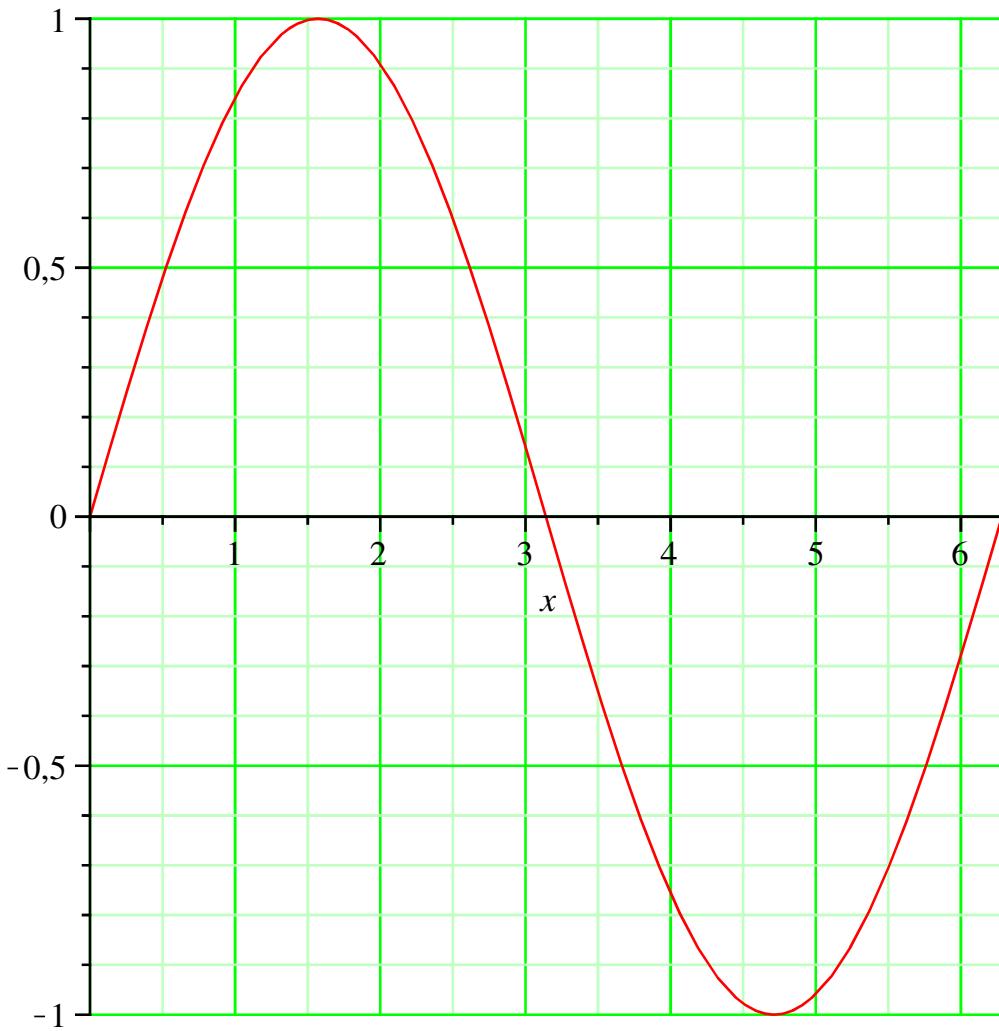


```
> plot([sin, cos], -Pi .. Pi, title = "Simple Trig Functions",
       legend = ["Seno", "Coseno"]);
```

Simple Trig Functions



```
> plot(sin(x), x = 0 .. 2*Pi, axis = [gridlines = [colour = green, majorlines = 2]]);
```



Construindo o gráfico a partir de um arquivo numéricico.

```
> #currentdir("C:\\\\Users\\\\User\\\\Desktop\\\\minicurso_maple");
> currentdir("C:\\\\Users\\\\Windows 7\\\\Desktop\\\\minicurso-maple"
              "C:\\Users\\Windows 7\\Desktop\\minicurso-maple" (4.3)
```

```
> currentdir();
              "C:\\Users\\Windows 7\\Desktop\\minicurso-maple" (4.4)
```

```
> readdata(`pacoteE135alpha04.dat` , 2);
[[0.009090909091, 0.01369802986], [0.01818181818, 0.04401990255], [0.0272727272727,
 0.06732435948], [0.03636363636, 0.06606643078], [0.04545454545,
 0.04261968046], [0.05454545455, 0.01714993141], [0.06363636364,
 0.01214356194], [0.07272727273, 0.03653000287], [0.08181818182,
 0.08118816174], [0.09090909091, 0.1271274502], [0.1000000000, 0.1577395508],
[0.1090909091, 0.1656222794], [0.1181818182, 0.1514969739], [0.1272727273,
0.1201353027], [0.1363636364, 0.07860610456], [0.1454545455, 0.03709149476],
[0.1545454545, 0.007936609415], [0.1636363636, 0.0003986456945], (4.5)
```

[0.1727272727, 0.01411466393], [0.1818181818, 0.03765667366], [0.1909090909, 0.05508922920], [0.2000000000, 0.05631286365], [0.2090909091, 0.04311364625], [0.2181818182, 0.02625134511], [0.2272727273, 0.01646527838], [0.2363636364, 0.01707158045], [0.2454545455, 0.02347441370], [0.2545454545, 0.02853483287], [0.2636363636, 0.02828374277], [0.2727272727, 0.02357750669], [0.2818181818, 0.01790182680], [0.2909090909, 0.01438473712], [0.3000000000, 0.01428896418], [0.3090909091, 0.01685671051], [0.3181818182, 0.01961107319], [0.3272727273, 0.01961338750], [0.3363636364, 0.01662362551], [0.3454545455, 0.01681126035], [0.3545454545, 0.03291357847], [0.3636363636, 0.07750767637], [0.3727272727, 0.1517535023], [0.3818181818, 0.2379320733], [0.3909090909, 0.3038572446], [0.4000000000, 0.3190277290], [0.4090909091, 0.2729906837], [0.4181818182, 0.1830885851], [0.4272727273, 0.08595920830], [0.4363636364, 0.01864168915], [0.4454545455, 0.001189173370], [0.4545454545, 0.03038713829], [0.4636363636, 0.08551713273], [0.4727272727, 0.1407069739], [0.4818181818, 0.1771053538], [0.4909090909, 0.1903668434], [0.5000000000, 0.1910962271], [0.5090909091, 0.1970807916], [0.5181818182, 0.2200373178], [0.5272727273, 0.2542388088], [0.5363636364, 0.2766269911], [0.5454545455, 0.2620952094], [0.5545454545, 0.2047775390], [0.5636363636, 0.1287244950], [0.5727272727, 0.07614882634], [0.5818181818, 0.07902900913], [0.5909090909, 0.1352393956], [0.6000000000, 0.2084490300], [0.6090909091, 0.2530911582], [0.6181818182, 0.2447425094], [0.6272727273, 0.1927378439], [0.6363636364, 0.1274899034], [0.6454545455, 0.07576091180], [0.6545454545, 0.04532702606], [0.6636363636, 0.02840541285], [0.6727272727, 0.01571841295], [0.6818181818, 0.005758616202], [0.6909090909, 0.002106666951], [0.7000000000, 0.005444542038], [0.7090909091, 0.01081144125], [0.7181818182, 0.01284888490], [0.7272727273, 0.01182169646], [0.7363636364, 0.01270658018], [0.7454545455, 0.01843901933], [0.7545454545, 0.02557672429], [0.7636363636, 0.02787164178], [0.7727272727, 0.02370407653], [0.7818181818, 0.01840233051], [0.7909090909, 0.01812424154], [0.8000000000, 0.02218005879], [0.8090909091, 0.02335052436], [0.8181818182, 0.01709541717], [0.8272727273, 0.009735334539], [0.8363636364, 0.01515205066], [0.8454545455, 0.04111373408], [0.8545454545, 0.07817180715], [0.8636363636, 0.1035263677], [0.8727272727, 0.09846351719], [0.8818181818, 0.06455502827], [0.8909090909, 0.02408675266], [0.9000000000, 0.003727913144], [0.9090909091, 0.01518003320], [0.9181818182, 0.04822379880], [0.9272727273, 0.08000971980], [0.9363636364, 0.09160642642], [0.9454545455, 0.07879486442], [0.9545454545, 0.05119014231], [0.9636363636, 0.02340373169], [0.9727272727, 0.005753673664], [0.9818181818,

0.0001233984460], [0.9909090909, 0.001936641785], [1.000000000,
0.005695281962], [1.009090909, 0.01012807000], [1.018181818, 0.01892956726],
[1.027272727, 0.03570873517], [1.036363636, 0.05689568646], [1.045454545,
0.07008991561], [1.054545455, 0.06242997698], [1.063636364, 0.03425334254],
[1.072727273, 0.005627475127], [1.081818182, 0.006063000551], [1.090909091,
0.05185001246], [1.100000000, 0.1287715936], [1.109090909, 0.1964479772],
[1.118181818, 0.2141874961], [1.127272727, 0.1698370971], [1.136363636,
0.08938136023], [1.145454545, 0.02025516798], [1.154545455, 0.001056312873],
[1.163636364, 0.03870290234], [1.172727273, 0.1067860087], [1.181818182,
0.1633589720], [1.190909091, 0.1756285071], [1.200000000, 0.1379891980],
[1.209090909, 0.07437820336], [1.218181818, 0.02329268915], [1.227272727,
0.01303633465], [1.236363636, 0.04222071155], [1.245454545, 0.08059939542],
[1.254545455, 0.09293014551], [1.263636364, 0.06879627149], [1.272727273,
0.03258817376], [1.281818182, 0.02230463799], [1.290909091, 0.05363226692],
[1.300000000, 0.1023738984], [1.309090909, 0.1242616436], [1.318181818,
0.09589751468], [1.327272727, 0.03868565878], [1.336363636, 0.001660938448],
[1.345454545, 0.01743907659], [1.354545455, 0.07229980804], [1.363636364,
0.1185715635], [1.372727273, 0.1172507691], [1.381818182, 0.07117899331],
[1.390909091, 0.01938791333], [1.400000000, 0.0006432172019], [1.409090909,
0.02163576409], [1.418181818, 0.05668142412], [1.427272727, 0.07412922441],
[1.436363636, 0.06232178568], [1.445454545, 0.03362684705], [1.454545455,
0.009119824732], [1.463636364, 0.002000803057], [1.472727273, 0.01244584055],
[1.481818182, 0.03230512390], [1.490909091, 0.05101093575], [1.500000000,
0.05886451724], [1.509090909, 0.05053349648], [1.518181818, 0.02953308379],
[1.527272727, 0.008706094048], [1.536363636, 0.002621803157], [1.545454545,
0.01594476750], [1.554545455, 0.03846528364], [1.563636364, 0.05293648814],
[1.572727273, 0.04909332027], [1.581818182, 0.03096041154], [1.590909091,
0.01153209002], [1.600000000, 0.001143914930], [1.609090909, 0.0008845117647],
[1.618181818, 0.005453802295], [1.627272727, 0.009790499617], [1.636363636,
0.01210481388], [1.645454545, 0.01238540994], [1.654545455, 0.01071442564],
[1.663636364, 0.007970776179], [1.672727273, 0.006608394532], [1.681818182,
0.008684144552], [1.690909091, 0.01281193320], [1.700000000, 0.01461844208],
[1.709090909, 0.01159012212], [1.718181818, 0.006907554776], [1.727272727,
0.006931338118], [1.736363636, 0.01430732127], [1.745454545, 0.02420412005],
[1.754545455, 0.02832504640], [1.763636364, 0.02285128199], [1.772727273,
0.01185390739], [1.781818182, 0.002922049455], [1.790909091, 0.0003641245438],

[1.800000000, 0.002877521761], [1.809090909, 0.006567801791], [1.818181818,
0.008694577531], [1.827272727, 0.008503063486], [1.836363636, 0.006378546109],
[1.845454545, 0.003965689815], [1.854545455, 0.004376808737], [1.863636364,
0.009691801651], [1.872727273, 0.01702256357], [1.881818182, 0.01910620261],
[1.890909091, 0.01188421710], [1.900000000, 0.001793127943], [1.909090909,
0.002448437864], [1.918181818, 0.02070408318], [1.927272727, 0.04604650406],
[1.936363636, 0.05762041342], [1.945454545, 0.04497835909], [1.954545455,
0.02096136372], [1.963636364, 0.01073833722], [1.972727273, 0.02622524533],
[1.981818182, 0.05268845913], [1.990909091, 0.06336221851], [2.000000000,
0.04757021506], [2.009090909, 0.02194061876], [2.018181818, 0.01244105101],
[2.027272727, 0.02683224007], [2.036363636, 0.04730113559], [2.045454545,
0.05054066072], [2.054545455, 0.03220946989], [2.063636364, 0.009247393836],
[2.072727273, 0.000002531882026], [2.081818182, 0.006021812347], [2.090909091,
0.01453320472], [2.100000000, 0.01547509626], [2.109090909, 0.01129745903],
[2.118181818, 0.009579379764], [2.127272727, 0.01112887738], [2.136363636,
0.009942417734], [2.145454545, 0.003859091735], [2.154545455,
0.0001553185167], [2.163636364, 0.006899861741], [2.172727273, 0.02064652061],
[2.181818182, 0.02784035145], [2.190909091, 0.02031395036], [2.200000000,
0.006420195042], [2.209090909, 0.003207022411], [2.218181818, 0.01717189016],
[2.227272727, 0.03576522472], [2.236363636, 0.04039559495], [2.245454545,
0.02637909839], [2.254545455, 0.007373347858], [2.263636364, 0.0002875766190],
[2.272727273, 0.008148477035], [2.281818182, 0.01930263220], [2.290909091,
0.02191076606], [2.300000000, 0.01570221015], [2.309090909, 0.008788054825],
[2.318181818, 0.006520584883], [2.327272727, 0.006672407386], [2.336363636,
0.004872033492], [2.345454545, 0.001474156579], [2.354545455,
0.0006092872972], [2.363636364, 0.003684499036], [2.372727273,
0.007114615849], [2.381818182, 0.007222099679], [2.390909091, 0.005092155952],
[2.400000000, 0.004762967287], [2.409090909, 0.007323293696], [2.418181818,
0.009103742110], [2.427272727, 0.006727004328], [2.436363636, 0.002246540771],
[2.445454545, 0.001352415160], [2.454545455, 0.006662219289], [2.463636364,
0.01414504562], [2.472727273, 0.01703293156], [2.481818182, 0.01278832520],
[2.490909091, 0.005277490856], [2.500000000, 0.0006641152967], [2.509090909,
0.002355215282], [2.518181818, 0.009187395581], [2.527272727, 0.01674668306],
[2.536363636, 0.02007926618], [2.545454545, 0.01647852554], [2.554545455,
0.007785776197], [2.563636364, 0.0006960203593], [2.572727273,
0.002602394102], [2.581818182, 0.01474967215], [2.590909091, 0.02973143347],

[2.600000000, 0.03711981384], [2.609090909, 0.03231453457], [2.618181818,
0.02045577510], [2.627272727, 0.01239008402], [2.636363636, 0.01704890393],
[2.645454545, 0.03628855959], [2.654545455, 0.06356451252], [2.663636364,
0.08514964185], [2.672727273, 0.08584096430], [2.681818182, 0.06133910170],
[2.690909091, 0.02947070304], [2.700000000, 0.02364689889], [2.709090909,
0.06411099240], [2.718181818, 0.1305911863], [2.727272727, 0.1697159359],
[2.736363636, 0.1413483921], [2.745454545, 0.06379232966], [2.754545455,
0.006863887496], [2.763636364, 0.02839557929], [2.772727273, 0.1141035812],
[2.781818182, 0.1863240375], [2.790909091, 0.1776756979], [2.800000000,
0.09668407460], [2.809090909, 0.01859648146], [2.818181818, 0.009929177979],
[2.827272727, 0.06481323173], [2.836363636, 0.1185909437], [2.845454545,
0.1183557469], [2.854545455, 0.07153450509], [2.863636364, 0.02708956806],
[2.872727273, 0.01933614321], [2.881818182, 0.03730182454], [2.890909091,
0.04720845575], [2.900000000, 0.03446173402], [2.909090909, 0.01448847942],
[2.918181818, 0.007050744459], [2.927272727, 0.01237037907], [2.936363636,
0.01607038203], [2.945454545, 0.01039441773], [2.954545455, 0.002812638790],
[2.963636364, 0.003001125310], [2.972727273, 0.008383616750], [2.981818182,
0.008877492165], [2.990909091, 0.002783749077], [3.000000000,
0.0006190056560], [3.009090909, 0.01159025304], [3.018181818, 0.03013192662],
[3.027272727, 0.04013497691], [3.036363636, 0.03329255554], [3.045454545,
0.01922352731], [3.054545455, 0.01468282505], [3.063636364, 0.02589286781],
[3.072727273, 0.04386472481], [3.081818182, 0.05445785299], [3.090909091,
0.05116034790], [3.100000000, 0.03912204155], [3.109090909, 0.02820866488],
[3.118181818, 0.02425306080], [3.127272727, 0.02757674884], [3.136363636,
0.03581461966], [3.145454545, 0.04465330445], [3.154545455, 0.04819197283],
[3.163636364, 0.04224928873], [3.172727273, 0.02818225127], [3.181818182,
0.01376315898], [3.190909091, 0.01005268311], [3.200000000, 0.02403493810],
[3.209090909, 0.05037175419], [3.218181818, 0.07110273071], [3.227272727,
0.06832633865], [3.236363636, 0.04114171304], [3.245454545, 0.01060435508],
[3.254545455, 0.004918022926], [3.263636364, 0.03400503270], [3.272727273,
0.07598886231], [3.281818182, 0.09375093196], [3.290909091, 0.07040468204],
[3.300000000, 0.02680698548], [3.309090909, 0.0008472115593], [3.318181818,
0.01066023193], [3.327272727, 0.03954679746], [3.336363636, 0.05573213745],
[3.345454545, 0.04484542798], [3.354545455, 0.02069093802], [3.363636364,
0.005170147682], [3.372727273, 0.004420264834], [3.381818182, 0.008384644350],
[3.390909091, 0.007841222379], [3.400000000, 0.004553072428], [3.409090909,

[0.004785701125], [3.418181818, 0.008573241226], [3.427272727, 0.01034591241],
[3.436363636, 0.008357862459], [3.445454545, 0.006898552116], [3.454545455,
0.008434600149], [3.463636364, 0.009879344222], [3.472727273, 0.009036385624],
[3.481818182, 0.01033459472], [3.490909091, 0.01967240406], [3.500000000,
0.03317284457], [3.509090909, 0.03655788622], [3.518181818, 0.02235283273],
[3.527272727, 0.004332705180], [3.536363636, 0.004833824185], [3.545454545,
0.02718471943], [3.554545455, 0.04905889240], [3.563636364, 0.04664513777],
[3.572727273, 0.02211792070], [3.581818182, 0.002547080123], [3.590909091,
0.009307519935], [3.600000000, 0.03308763012], [3.609090909, 0.04589494485],
[3.618181818, 0.03461684227], [3.627272727, 0.01388529570], [3.636363636,
0.005977572793], [3.645454545, 0.01552552979], [3.654545455, 0.02752095911],
[3.663636364, 0.02720511385], [3.672727273, 0.01608676095], [3.681818182,
0.006058268795], [3.690909091, 0.003424605744], [3.700000000, 0.004674231207],
[3.709090909, 0.004759804777], [3.718181818, 0.003179741682], [3.727272727,
0.002003071498], [3.736363636, 0.002401351454], [3.745454545, 0.005158304282],
[3.754545455, 0.01124748813], [3.763636364, 0.01769757872], [3.772727273,
0.01651984427], [3.781818182, 0.005965038620], [3.790909091, 0.001517371212],
[3.800000000, 0.02473992428], [3.809090909, 0.07486287171], [3.818181818,
0.1163446889], [3.827272727, 0.1071979602], [3.836363636, 0.04935193307],
[3.845454545, 0.003292919081], [3.854545455, 0.03346369946], [3.863636364,
0.1343185390], [3.872727273, 0.2238621946], [3.881818182, 0.2200405840],
[3.890909091, 0.1233772108], [3.900000000, 0.02234938101], [3.909090909,
0.01228544537], [3.918181818, 0.1035251056], [3.927272727, 0.2118510165],
[3.936363636, 0.2412596832], [3.945454545, 0.1709440726], [3.954545455,
0.06379039919], [3.963636364, 0.003367058754], [3.972727273, 0.02539003971],
[3.981818182, 0.09733246491], [3.990909091, 0.1539921478], [4.000000000,
0.1527187045], [4.009090909, 0.1001743818], [4.018181818, 0.03644719241],
[4.027272727, 0.001771409369], [4.036363636, 0.01275041518], [4.045454545,
0.05560229932], [4.054545455, 0.09623356144], [4.063636364, 0.1038333200],
[4.072727273, 0.07315686057], [4.081818182, 0.02758549349], [4.090909091,
0.001129949416], [4.100000000, 0.01288150704], [4.109090909, 0.05046952103],
[4.118181818, 0.07793090204], [4.127272727, 0.06874767499], [4.136363636,
0.03338733591], [4.145454545, 0.007372887920], [4.154545455, 0.01213860919],
[4.163636364, 0.03445199898], [4.172727273, 0.04479080559], [4.181818182,
0.03178362955], [4.190909091, 0.01511775574], [4.200000000, 0.01966998477],
[4.209090909, 0.03982708361], [4.218181818, 0.04478889995], [4.227272727,

[0.02307123364], [4.236363636, 0.003195827699], [4.245454545, 0.01832494467],
[4.254545455, 0.06101225019], [4.263636364, 0.08648499555], [4.272727273,
0.06379164653], [4.281818182, 0.01742454986], [4.290909091, 0.004559804470],
[4.300000000, 0.04641043730], [4.309090909, 0.09908197658], [4.318181818,
0.1053827168], [4.327272727, 0.06205893002], [4.336363636, 0.01986532086],
[4.345454545, 0.02252735210], [4.354545455, 0.05919186363], [4.363636364,
0.08222016240], [4.372727273, 0.06571655533], [4.381818182, 0.03262522698],
[4.390909091, 0.01961216382], [4.400000000, 0.03114757359], [4.409090909,
0.04158273047], [4.418181818, 0.03258999473], [4.427272727, 0.01339069664],
[4.436363636, 0.004388377451], [4.445454545, 0.01060777697], [4.454545455,
0.01843477685], [4.463636364, 0.01648363865], [4.472727273, 0.008871428957],
[4.481818182, 0.004167501105], [4.490909091, 0.002668726766], [4.500000000,
0.001403381555], [4.509090909, 0.002457828798], [4.518181818, 0.008898988229],
[4.527272727, 0.01693460832], [4.536363636, 0.01801022592], [4.545454545,
0.01003719686], [4.554545455, 0.003348845382], [4.563636364, 0.009043782814],
[4.572727273, 0.02211089974], [4.581818182, 0.02608459010], [4.590909091,
0.01604355361], [4.600000000, 0.006339598259], [4.609090909, 0.01158011857],
[4.618181818, 0.02723955851], [4.627272727, 0.03433298331], [4.636363636,
0.02255639824], [4.645454545, 0.004619317369], [4.654545455, 0.001849933997],
[4.663636364, 0.01705590434], [4.672727273, 0.03122038307], [4.681818182,
0.02828056059], [4.690909091, 0.01329987290], [4.700000000, 0.003377029816],
[4.709090909, 0.007850154537], [4.718181818, 0.02014691779], [4.727272727,
0.02594204859], [4.736363636, 0.01857150515], [4.745454545, 0.006695132713],
[4.754545455, 0.005187073451], [4.763636364, 0.01867928017], [4.772727273,
0.03633234309], [4.781818182, 0.04271909472], [4.790909091, 0.03214080878],
[4.800000000, 0.01377362582], [4.809090909, 0.005836446874], [4.818181818,
0.02166056410], [4.827272727, 0.05465292702], [4.836363636, 0.07894447756],
[4.845454545, 0.07335176988], [4.854545455, 0.04402809102], [4.863636364,
0.01798123637], [4.872727273, 0.01844625169], [4.881818182, 0.04881357391],
[4.890909091, 0.08938717542], [4.900000000, 0.1069440779], [4.909090909,
0.08250992293], [4.918181818, 0.03517046417], [4.927272727, 0.007722765672],
[4.936363636, 0.02555984291], [4.945454545, 0.07260549615], [4.954545455,
0.1041167367], [4.963636364, 0.08642504706], [4.972727273, 0.03416008777],
[4.981818182, 0.0008541741514], [4.990909091, 0.01938293151], [5.000000000,
0.06247094609], [5.009090909, 0.07739870041], [5.018181818, 0.04924580069],
[5.027272727, 0.01397489257], [5.036363636, 0.01237577063], [5.045454545,

[0.04189871277], [5.054545455, 0.06127198204], [5.063636364, 0.04400147884],
[5.072727273, 0.01366947549], [5.081818182, 0.01133904351], [5.090909091,
0.03952526418], [5.100000000, 0.06068392361], [5.109090909, 0.04769364323],
[5.118181818, 0.01648888011], [5.127272727, 0.004352943761], [5.136363636,
0.02509255831], [5.145454545, 0.05376578407], [5.154545455, 0.05783902281],
[5.163636364, 0.03557545554], [5.172727273, 0.01351392995], [5.181818182,
0.01174179130], [5.190909091, 0.02572525248], [5.200000000, 0.04025591298],
[5.209090909, 0.04705794854], [5.218181818, 0.04535823540], [5.227272727,
0.03520819589], [5.236363636, 0.01920397606], [5.245454545, 0.008715069311],
[5.254545455, 0.01760891272], [5.263636364, 0.04459856576], [5.272727273,
0.06903324835], [5.281818182, 0.06956972767], [5.290909091, 0.04384384107],
[5.300000000, 0.01125385523], [5.309090909, 0.0008954302476], [5.318181818,
0.02943980323], [5.327272727, 0.08178991357], [5.336363636, 0.1182519546],
[5.345454545, 0.1078437010], [5.354545455, 0.05642381757], [5.363636364,
0.007404831410], [5.372727273, 0.01278892853], [5.381818182, 0.08454174740],
[5.390909091, 0.1683336160], [5.400000000, 0.1871481425], [5.409090909,
0.1232079305], [5.418181818, 0.04174648738], [5.427272727, 0.02467375021],
[5.436363636, 0.08979602661], [5.445454545, 0.1777884762], [5.454545455,
0.2113176019], [5.463636364, 0.1665613955], [5.472727273, 0.09080902687],
[5.481818182, 0.05195816308], [5.490909091, 0.07513994964], [5.500000000,
0.1295570997], [5.509090909, 0.1657523809], [5.518181818, 0.1561520361],
[5.527272727, 0.1082445819], [5.536363636, 0.05441976858], [5.545454545,
0.03040817473], [5.554545455, 0.04987160355], [5.563636364, 0.09059696410],
[5.572727273, 0.1113320402], [5.581818182, 0.09016570890], [5.590909091,
0.04392682403], [5.600000000, 0.007783584999], [5.609090909, 0.002679763764],
[5.618181818, 0.02366742832], [5.627272727, 0.04946537443], [5.636363636,
0.05950107224], [5.645454545, 0.04828068478], [5.654545455, 0.02614346186],
[5.663636364, 0.007050968094], [5.672727273, 0.00005023140828], [5.681818182,
0.008583817295], [5.690909091, 0.02729468409], [5.700000000, 0.04174445364],
[5.709090909, 0.04126039994], [5.718181818, 0.02970379209], [5.727272727,
0.01769997003], [5.736363636, 0.009980164383], [5.745454545, 0.006086609224],
[5.754545455, 0.008670433813], [5.763636364, 0.02367977378], [5.772727273,
0.04879807290], [5.781818182, 0.06569640602], [5.790909091, 0.05564360241],
[5.800000000, 0.02565333732], [5.809090909, 0.006360833706], [5.818181818,
0.02029813609], [5.827272727, 0.06232565889], [5.836363636, 0.1071905613],
[5.845454545, 0.1250746498], [5.854545455, 0.1020730132], [5.863636364,

[0.06015403386], [5.872727273, 0.04341923227], [5.881818182, 0.07305457954],
[5.890909091, 0.1270873767], [5.900000000, 0.1642855801], [5.909090909,
0.1556698771], [5.918181818, 0.1058867849], [5.927272727, 0.05934897938],
[5.936363636, 0.06363285416], [5.945454545, 0.1106889681], [5.954545455,
0.1407356099], [5.963636364, 0.1174225093], [5.972727273, 0.06922934846],
[5.981818182, 0.04482720711], [5.990909091, 0.05537577388], [6.000000000,
0.07249972572], [6.009090909, 0.06584320116], [6.018181818, 0.03572298070],
[6.027272727, 0.01299950827], [6.036363636, 0.02304354673], [6.045454545,
0.05245745636], [6.054545455, 0.06439460547], [6.063636364, 0.04421123147],
[6.072727273, 0.01448853588], [6.081818182, 0.005956824718], [6.090909091,
0.02715245707], [6.100000000, 0.06243955850], [6.109090909, 0.08809591605],
[6.118181818, 0.08850064693], [6.127272727, 0.06686423379], [6.136363636,
0.04605286717], [6.145454545, 0.05169054735], [6.154545455, 0.08568726618],
[6.163636364, 0.1201281794], [6.172727273, 0.1256576957], [6.181818182,
0.1030610312], [6.190909091, 0.07915992344], [6.200000000, 0.07461127871],
[6.209090909, 0.08458523666], [6.218181818, 0.09189697511], [6.227272727,
0.09116772405], [6.236363636, 0.09131471128], [6.245454545, 0.09467254550],
[6.254545455, 0.08748131506], [6.263636364, 0.06148136107], [6.272727273,
0.03405368844], [6.281818182, 0.03114807767], [6.290909091, 0.05401243133],
[6.300000000, 0.07495459217], [6.309090909, 0.06683778454], [6.318181818,
0.03267345688], [6.327272727, 0.004023352552], [6.336363636, 0.006733096698],
[6.345454545, 0.03136849667], [6.354545455, 0.04724400890], [6.363636364,
0.04034148965], [6.372727273, 0.02200979953], [6.381818182, 0.007168731667],
[6.390909091, 0.002709333372], [6.400000000, 0.01053113148], [6.409090909,
0.02434950522], [6.418181818, 0.02989576320], [6.427272727, 0.02059785163],
[6.436363636, 0.006203350503], [6.445454545, 0.0001628891978], [6.454545455,
0.005711809766], [6.463636364, 0.01489235459], [6.472727273, 0.01634985292],
[6.481818182, 0.007903530494], [6.490909091, 0.001187901510], [6.500000000,
0.005433040443], [6.509090909, 0.01234050067], [6.518181818, 0.009767682195],
[6.527272727, 0.001869080029], [6.536363636, 0.001171342272], [6.545454545,
0.008658136096], [6.554545455, 0.01390466476], [6.563636364, 0.009977531069],
[6.572727273, 0.002069946296], [6.581818182, 0.002261867813], [6.590909091,
0.01360033899], [6.600000000, 0.02226764681], [6.609090909, 0.01575289332],
[6.618181818, 0.003328616719], [6.627272727, 0.002761773515], [6.636363636,
0.01347397304], [6.645454545, 0.02018434119], [6.654545455, 0.01601611565],
[6.663636364, 0.007157717817], [6.672727273, 0.001688126415], [6.681818182,

[0.003292421369], [6.690909091, 0.009448836652], [6.700000000, 0.01271847473],
[6.709090909, 0.009275186457], [6.718181818, 0.003423002325], [6.727272727,
0.0002743135704], [6.736363636, 0.0008454382396], [6.745454545,
0.004858105200], [6.754545455, 0.009652733494], [6.763636364, 0.009580345261],
[6.772727273, 0.005171057311], [6.781818182, 0.005748545383], [6.790909091,
0.01482955186], [6.800000000, 0.02231192205], [6.809090909, 0.01879783982],
[6.818181818, 0.009825424011], [6.827272727, 0.009718716076], [6.836363636,
0.02387786053], [6.845454545, 0.03963175056], [6.854545455, 0.03882673875],
[6.863636364, 0.02255574272], [6.872727273, 0.01371240507], [6.881818182,
0.02627206260], [6.890909091, 0.04427695024], [6.900000000, 0.04398269350],
[6.909090909, 0.02570968833], [6.918181818, 0.01053197731], [6.927272727,
0.01275287825], [6.936363636, 0.02560761026], [6.945454545, 0.03155453799],
[6.954545455, 0.02257312119], [6.963636364, 0.008739035056], [6.972727273,
0.004228285513], [6.981818182, 0.008996222900], [6.990909091, 0.01228894066],
[7.000000000, 0.009511021087], [7.009090909, 0.004989700254], [7.018181818,
0.002082079008], [7.027272727, 0.0005640420291], [7.036363636,
0.0008563766583], [7.045454545, 0.003699813792], [7.054545455,
0.007766191821], [7.063636364, 0.01112609873], [7.072727273, 0.01310791211],
[7.081818182, 0.01329352969], [7.090909091, 0.01075900151], [7.100000000,
0.007169196747], [7.109090909, 0.01038521628], [7.118181818, 0.02773308963],
[7.127272727, 0.05019671270], [7.136363636, 0.05384995445], [7.145454545,
0.03003399752], [7.154545455, 0.004911398498], [7.163636364, 0.01214048759],
[7.172727273, 0.05046443080], [7.181818182, 0.08188182149], [7.190909091,
0.07207190876], [7.200000000, 0.02915340154], [7.209090909, 0.0007152702733],
[7.218181818, 0.02265914890], [7.227272727, 0.07073610365], [7.236363636,
0.08576718786], [7.245454545, 0.05162034781], [7.254545455, 0.01473883741],
[7.263636364, 0.01531611465], [7.272727273, 0.03731558144], [7.281818182,
0.04449692310], [7.290909091, 0.03172769793], [7.300000000, 0.01974389399],
[7.309090909, 0.02123345238], [7.318181818, 0.02809267073], [7.327272727,
0.02461874763], [7.336363636, 0.009510651949], [7.345454545, 0.001711346626],
[7.354545455, 0.01426905099], [7.363636364, 0.03062063541], [7.372727273,
0.02741818375], [7.381818182, 0.01132518368], [7.390909091, 0.007295673665],
[7.400000000, 0.01886154364], [7.409090909, 0.02632149149], [7.418181818,
0.01940322800], [7.427272727, 0.01040819455], [7.436363636, 0.01483628018],
[7.445454545, 0.03004707361], [7.454545455, 0.03696379451], [7.463636364,
0.02453258184], [7.472727273, 0.007953908034], [7.481818182, 0.01016836342],

[7.490909091, 0.02833887683], [7.500000000, 0.03747453732], [7.509090909,
0.02595016059], [7.518181818, 0.007728757814], [7.527272727, 0.0004679773367],
[7.536363636, 0.007974326628], [7.545454545, 0.02147368819], [7.554545455,
0.02710249907], [7.563636364, 0.01789914106], [7.572727273, 0.003739225575],
[7.581818182, 0.0008545072116], [7.590909091, 0.01134906705], [7.600000000,
0.02312137106], [7.609090909, 0.02598055434], [7.618181818, 0.01830149724],
[7.627272727, 0.005621585166], [7.636363636, 0.0005293958806], [7.645454545,
0.01274394644], [7.654545455, 0.03291506933], [7.663636364, 0.03913468851],
[7.672727273, 0.02461467059], [7.681818182, 0.006232428251], [7.690909091,
0.002078298653], [7.700000000, 0.01243288498], [7.709090909, 0.02565326362],
[7.718181818, 0.03186258218], [7.727272727, 0.02763559497], [7.736363636,
0.01670587922], [7.745454545, 0.009962782276], [7.754545455, 0.01622721538],
[7.763636364, 0.02913696770], [7.772727273, 0.03345734593], [7.781818182,
0.02892128249], [7.790909091, 0.03232380321], [7.800000000, 0.04738145489],
[7.809090909, 0.05317940757], [7.818181818, 0.03824773486], [7.827272727,
0.02489712515], [7.836363636, 0.03874715731], [7.845454545, 0.07055259512],
[7.854545455, 0.08722035036], [7.863636364, 0.07012604833], [7.872727273,
0.03400123309], [7.881818182, 0.01655956680], [7.890909091, 0.04301244797],
[7.900000000, 0.08823422233], [7.909090909, 0.09456673400], [7.918181818,
0.04767203536], [7.927272727, 0.004599735955], [7.936363636, 0.01682261737],
[7.945454545, 0.05844841455], [7.954545455, 0.06822067953], [7.963636364,
0.03513621465], [7.972727273, 0.003255810166], [7.981818182, 0.006981236425],
[7.990909091, 0.03266618309], [8.000000000, 0.04256809481], [8.009090909,
0.02322098727], [8.018181818, 0.003230194965], [8.027272727, 0.01472758590],
[8.036363636, 0.04412164430], [8.045454545, 0.04841993793], [8.054545455,
0.02058040075], [8.063636364, 0.001512189758], [8.072727273, 0.01799160228],
[8.081818182, 0.04532483655], [8.090909091, 0.04697882108], [8.100000000,
0.02284211880], [8.109090909, 0.002124474207], [8.118181818, 0.00507771263],
[8.127272727, 0.02339723792], [8.136363636, 0.03329424183], [8.145454545,
0.02366585456], [8.154545455, 0.007659973335], [8.163636364, 0.002679790772],
[8.172727273, 0.007792216642], [8.181818182, 0.01108903342], [8.190909091,
0.009336824117], [8.200000000, 0.007135660159], [8.209090909, 0.005240966858],
[8.218181818, 0.002122200291], [8.227272727, 0.0008334196774], [8.236363636,
0.005116072764], [8.245454545, 0.01217565614], [8.254545455, 0.01445647801],
[8.263636364, 0.008546219374], [8.272727273, 0.001677780853], [8.281818182,
0.005644442317], [8.290909091, 0.02038872720], [8.300000000, 0.03060011407],

[8.309090909, 0.02607268912], [8.318181818, 0.01611093971], [8.327272727, 0.01400634623], [8.336363636, 0.01793455012], [8.345454545, 0.01859004941], [8.354545455, 0.01652847698], [8.363636364, 0.02084265124], [8.372727273, 0.03438245617], [8.381818182, 0.04588063084], [8.390909091, 0.03911443052], [8.400000000, 0.01540668248], [8.409090909, 0.003379960897], [8.418181818, 0.02977517414], [8.427272727, 0.07979561197], [8.436363636, 0.1065706046], [8.445454545, 0.08395285368], [8.454545455, 0.03368163052], [8.463636364, 0.001588223825], [8.472727273, 0.02113318104], [8.481818182, 0.08893173756], [8.490909091, 0.1563030698], [8.500000000, 0.1604995875], [8.509090909, 0.09101280113], [8.518181818, 0.01441874843], [8.527272727, 0.008993457850], [8.536363636, 0.08132454564], [8.545454545, 0.1642864288], [8.554545455, 0.1873490038], [8.563636364, 0.1348256645], [8.572727273, 0.04969045504], [8.581818182, 0.0006875049439], [8.590909091, 0.03505919431], [8.600000000, 0.1352835650], [8.609090909, 0.2183276694], [8.618181818, 0.2039560602], [8.627272727, 0.1014159133], [8.636363636, 0.01220452663], [8.645454545, 0.02657069369], [8.654545455, 0.1274551907], [8.663636364, 0.2140428818], [8.672727273, 0.2085969083], [8.681818182, 0.1248202139], [8.690909091, 0.04603676601], [8.700000000, 0.04891965663], [8.709090909, 0.1300107007], [8.718181818, 0.2010672191], [8.727272727, 0.1834985509], [8.736363636, 0.1053420219], [8.745454545, 0.06295727499], [8.754545455, 0.09085353773], [8.763636364, 0.1286587557], [8.772727273, 0.1222143037], [8.781818182, 0.09070791388], [8.790909091, 0.07454541933], [8.800000000, 0.07562491274], [8.809090909, 0.07488876274], [8.818181818, 0.06637621964], [8.827272727, 0.05369927292], [8.836363636, 0.04113121113], [8.845454545, 0.03599213519], [8.854545455, 0.03930709449], [8.863636364, 0.03820009543], [8.872727273, 0.02494637300], [8.881818182, 0.01156725865], [8.890909091, 0.009851461466], [8.900000000, 0.01279514411], [8.909090909, 0.009849830178], [8.918181818, 0.004182113653], [8.927272727, 0.003017300802], [8.936363636, 0.004965697710], [8.945454545, 0.005364330023], [8.954545455, 0.003692065959], [8.963636364, 0.001532062377], [8.972727273, 0.0005540162343], [8.981818182, 0.003149062263], [8.990909091, 0.009943562362], [9.000000000, 0.01705846871], [9.009090909, 0.01825890910], [9.018181818, 0.01104352697], [9.027272727, 0.002964118999], [9.036363636, 0.008601284984], [9.045454545, 0.03126108981], [9.054545455, 0.05105275364], [9.063636364, 0.04606185344], [9.072727273, 0.02407037510], [9.081818182, 0.01534930721], [9.090909091, 0.03255731231], [9.100000000, 0.05559070530], [9.109090909, 0.06000149749], [9.118181818,

[0.04537150464], [9.127272727, 0.03013972619], [9.136363636, 0.02877660787],
[9.145454545, 0.04021481017], [9.154545455, 0.05421849313], [9.163636364,
0.06298297814], [9.172727273, 0.06422771095], [9.181818182, 0.05747681127],
[9.190909091, 0.04584474011], [9.200000000, 0.04025850617], [9.209090909,
0.04981169169], [9.218181818, 0.06563928483], [9.227272727, 0.06658555885],
[9.236363636, 0.04539649120], [9.245454545, 0.02022094798], [9.254545455,
0.01593718565], [9.263636364, 0.03755165223], [9.272727273, 0.06229918108],
[9.281818182, 0.06031868503], [9.290909091, 0.02967596066], [9.300000000,
0.004457769978], [9.309090909, 0.01407129859], [9.318181818, 0.04335424633],
[9.327272727, 0.05396907323], [9.336363636, 0.03593304842], [9.345454545,
0.01252176049], [9.354545455, 0.003366021418], [9.363636364, 0.009748218837],
[9.372727273, 0.02701643933], [9.381818182, 0.04512360172], [9.390909091,
0.04662358777], [9.400000000, 0.02734759441], [9.409090909, 0.008198940177],
[9.418181818, 0.008902573934], [9.427272727, 0.02424657547], [9.436363636,
0.03815908608], [9.445454545, 0.04246004998], [9.454545455, 0.03383792082],
[9.463636364, 0.01475557712], [9.472727273, 0.002352551530], [9.481818182,
0.01262217104], [9.490909091, 0.03394025098], [9.500000000, 0.03973015144],
[9.509090909, 0.02509443098], [9.518181818, 0.008104478181], [9.527272727,
0.001178931945], [9.536363636, 0.003741242496], [9.545454545, 0.01434348975],
[9.554545455, 0.02818157712], [9.563636364, 0.03177426267], [9.572727273,
0.01938474775], [9.581818182, 0.006069474208], [9.590909091, 0.009336639357],
[9.600000000, 0.02625886402], [9.609090909, 0.03978931819], [9.618181818,
0.04004099530], [9.627272727, 0.03169013166], [9.636363636, 0.02595072893],
[9.645454545, 0.02958251730], [9.654545455, 0.04007757258], [9.663636364,
0.05189932360], [9.672727273, 0.06468356401], [9.681818182, 0.07782453033],
[9.690909091, 0.08097321242], [9.700000000, 0.06444972955], [9.709090909,
0.03922769709], [9.718181818, 0.03137382888], [9.727272727, 0.05224629053],
[9.736363636, 0.08332936420], [9.745454545, 0.09352248854], [9.754545455,
0.06888396888], [9.763636364, 0.02827470629], [9.772727273, 0.009158877773],
[9.781818182, 0.02942312711], [9.790909091, 0.06461631768], [9.800000000,
0.07477657100], [9.809090909, 0.05072678180], [9.818181818, 0.01849994727],
[9.827272727, 0.001928058088], [9.836363636, 0.0006358034399], [9.845454545,
0.004749200367], [9.854545455, 0.01134656095], [9.863636364, 0.02084193273],
[9.872727273, 0.02988127606], [9.881818182, 0.03345787608], [9.890909091,
0.02899619768], [9.900000000, 0.01776490686], [9.909090909, 0.006090678689],
[9.918181818, 0.005166356461], [9.927272727, 0.02598121644], [9.936363636,

[0.06777589859], [9.945454545, 0.1065110257], [9.954545455, 0.1055764291],
[9.963636364, 0.05793893778], [9.972727273, 0.01309951876], [9.981818182,
0.03232615401], [9.990909091, 0.1100592260], [10.00000000, 0.1691847861],
[10.00909091, 0.1487967483], [10.01818182, 0.07278842335], [10.02727273,
0.01607307217], [10.03636364, 0.02238041175], [10.04545455, 0.07044142892],
[10.05454545, 0.1071949658], [10.06363636, 0.1005863178], [10.07272727,
0.06423900624], [10.08181818, 0.03543106448], [10.09090909, 0.03145176894],
[10.10000000, 0.03745910984], [10.10909091, 0.03765360604], [10.11818182,
0.03740489531], [10.12727273, 0.04428792825], [10.13636364, 0.04811587767],
[10.14545455, 0.03606588630], [10.15454545, 0.01401604268], [10.16363636,
0.0004015521974], [10.17272727, 0.007785935963], [10.18181818, 0.03386979017],
[10.19090909, 0.05995541595], [10.20000000, 0.06150618130], [10.20909091,
0.03494263326], [10.21818182, 0.008195366188], [10.22727273, 0.008858571038],
[10.23636364, 0.03051835101], [10.24545455, 0.04655530178], [10.25454545,
0.04481010616], [10.26363636, 0.03121281515], [10.27272727, 0.01372342290],
[10.28181818, 0.001461237622], [10.29090909, 0.005473524139], [10.30000000,
0.02260494182], [10.30909091, 0.03219493852], [10.31818182, 0.02331472841],
[10.32727273, 0.01045279261], [10.33636364, 0.009782656482], [10.34545455,
0.01601894249], [10.35454545, 0.01532095782], [10.36363636, 0.007238652702],
[10.37272727, 0.002715897711], [10.38181818, 0.009421489299], [10.39090909,
0.02442551680], [10.40000000, 0.03490811978], [10.40909091, 0.02826345200],
[10.41818182, 0.009301001297], [10.42727273, 0.0001046380839], [10.43636364,
0.01254975737], [10.44545455, 0.03088146785], [10.45454545, 0.03372097955],
[10.46363636, 0.02202410337], [10.47272727, 0.01114061159], [10.48181818,
0.006472812842], [10.49090909, 0.003415333708], [10.50000000, 0.003112935398],
[10.50909091, 0.01128010769], [10.51818182, 0.02434128022], [10.52727273,
0.03012379848], [10.53636364, 0.02282355306], [10.54545455, 0.009345291350],
[10.55454545, 0.0007689789199], [10.56363636, 0.003320316095], [10.57272727,
0.01727488282], [10.58181818, 0.03727499268], [10.59090909, 0.05034134393],
[10.60000000, 0.04215089043], [10.60909091, 0.01638919009], [10.61818182,
0.002680107905], [10.62727273, 0.02712155213], [10.63636364, 0.07298972892],
[10.64545455, 0.09168674104], [10.65454545, 0.06158996111], [10.66363636,
0.01638274274], [10.67272727, 0.003151239011], [10.68181818, 0.03053476694],
[10.69090909, 0.07014085816], [10.70000000, 0.09065666660], [10.70909091,
0.07896673516], [10.71818182, 0.04654597719], [10.72727273, 0.02534008903],
[10.73636364, 0.03831850316], [10.74545455, 0.06842105618], [10.75454545,

[0.07954096159], [10.76363636, 0.06874679914], [10.77272727, 0.06469283036],
[10.78181818, 0.07229866022], [10.79090909, 0.06289675320], [10.80000000,
0.03190770106], [10.80909091, 0.01999049484], [10.81818182, 0.05149730175],
[10.82727273, 0.09001197006], [10.83636364, 0.08614750210], [10.84545455,
0.04309285494], [10.85454545, 0.005960740738], [10.86363636, 0.003978512340],
[10.87272727, 0.02681968349], [10.88181818, 0.04632977020], [10.89090909,
0.04421895361], [10.90000000, 0.02505372206], [10.90909091, 0.01046348305],
[10.91818182, 0.01484084743], [10.92727273, 0.02740852695], [10.93636364,
0.02833421304], [10.94545455, 0.01750884597], [10.95454545, 0.01163332481],
[10.96363636, 0.01654180111], [10.97272727, 0.02049247937], [10.98181818,
0.01484253241], [10.99090909, 0.005334994589], [11.00000000, 0.0005530420319],
[11.00909091, 0.001125315700], [11.01818182, 0.003075419304], [11.02727273,
0.004001337011], [11.03636364, 0.003720090212], [11.04545455, 0.002743364925],
[11.05454545, 0.001391611751], [11.06363636, 0.0002471567985], [11.07272727,
0.001503274275], [11.08181818, 0.006467307198], [11.09090909, 0.01032202106],
[11.10000000, 0.006642665323], [11.10909091, 0.0007809774311], [11.11818182,
0.007614115970], [11.12727273, 0.02804720800], [11.13636364, 0.04046827229],
[11.14545455, 0.02844473028], [11.15454545, 0.006295764328], [11.16363636,
0.001922480123], [11.17272727, 0.02129027327], [11.18181818, 0.04402550335],
[11.19090909, 0.04930461954], [11.20000000, 0.03452870619], [11.20909091,
0.01284827273], [11.21818182, 0.001766632240], [11.22727273, 0.01039019810],
[11.23636364, 0.03119633037], [11.24545455, 0.04755621436], [11.25454545,
0.05107681901], [11.26363636, 0.04543069686], [11.27272727, 0.03485701506],
[11.28181818, 0.02074985298], [11.29090909, 0.01021742817], [11.30000000,
0.01454940112], [11.30909091, 0.03473119261], [11.31818182, 0.05710883738],
[11.32727273, 0.06544948729], [11.33636364, 0.05234757770], [11.34545455,
0.02393112483], [11.35454545, 0.001515308338], [11.36363636, 0.009655101719],
[11.37272727, 0.04856013912], [11.38181818, 0.08477610308], [11.39090909,
0.08408756306], [11.40000000, 0.04937899173], [11.40909091, 0.01335325356],
[11.41818182, 0.00002341613458], [11.42727273, 0.007215822370], [11.43636364,
0.02119912353], [11.44545455, 0.03271001078], [11.45454545, 0.03874223663],
[11.46363636, 0.03891683049], [11.47272727, 0.03220500050], [11.48181818,
0.01733227768], [11.49090909, 0.001949772088], [11.50000000, 0.006736796871],
[11.50909091, 0.04337977469], [11.51818182, 0.08771221138], [11.52727273,
0.09667238979], [11.53636364, 0.06097360224], [11.54545455, 0.02307983381],
[11.55454545, 0.03205312847], [11.56363636, 0.09230841344], [11.57272727,

[0.1611304726], [11.58181818, 0.1839731640], [11.59090909, 0.1365230781],
[11.60000000, 0.05630831612], [11.60909091, 0.02994653216], [11.61818182,
0.1121412785], [11.62727273, 0.2461127848], [11.63636364, 0.3014599797],
[11.64545455, 0.2155518373], [11.65454545, 0.07079342154], [11.66363636,
0.004822830024], [11.67272727, 0.06388997507], [11.68181818, 0.1719016077],
[11.69090909, 0.2268329851], [11.70000000, 0.1938719492], [11.70909091,
0.1097792376], [11.71818182, 0.03250669450], [11.72727273, 0.0008434084076],
[11.73636364, 0.02161654855], [11.74545455, 0.07211004885], [11.75454545,
0.1131858683], [11.76363636, 0.1138458613], [11.77272727, 0.07493692433],
[11.78181818, 0.02932058036], [11.79090909, 0.01115684776], [11.80000000,
0.02210797395], [11.80909091, 0.03419789229], [11.81818182, 0.02793483570],
[11.82727273, 0.01628026109], [11.83636364, 0.02290401918], [11.84545455,
0.04741623987], [11.85454545, 0.06583723318], [11.86363636, 0.06075971588],
[11.87272727, 0.03810480279], [11.88181818, 0.01537907701], [11.89090909,
0.004498577882], [11.90000000, 0.007853669205], [11.90909091, 0.02377959528],
[11.91818182, 0.05128812236], [11.92727273, 0.08745665216], [11.93636364,
0.1184353881], [11.94545455, 0.1200171802], [11.95454545, 0.08105667196],
[11.96363636, 0.02703062558], [11.97272727, 0.004257599732], [11.98181818,
0.03313129088], [11.99090909, 0.08777572974], [12.00000000, 0.1263993344],
[12.00909091, 0.1285230632], [12.01818182, 0.09845617345], [12.02727273,
0.05180426686], [12.03636364, 0.01147545535], [12.04545455, 0.001142249886],
[12.05454545, 0.02454303608], [12.06363636, 0.05738908809], [12.07272727,
0.07168924505], [12.08181818, 0.06303350568], [12.09090909, 0.04696420359],
[12.10000000, 0.03711601974], [12.10909091, 0.03465573424], [12.11818182,
0.03151605325], [12.12727273, 0.01925831545], [12.13636364, 0.004104075648],
[12.14545455, 0.01331269210], [12.15454545, 0.06781437378], [12.16363636,
0.1426926504], [12.17272727, 0.1777208280], [12.18181818, 0.1423435293],
[12.19090909, 0.07296701486], [12.20000000, 0.03050351959], [12.20909091,
0.03790723931], [12.21818182, 0.07615320390], [12.22727273, 0.1212916090],
[12.23636364, 0.1580038222], [12.24545455, 0.1687698457], [12.25454545,
0.1420035878], [12.26363636, 0.09299059199], [12.27272727, 0.05395622623],
[12.28181818, 0.03991323719], [12.29090909, 0.04148092191], [12.30000000,
0.05098564592], [12.30909091, 0.07349065418], [12.31818182, 0.1051228000],
[12.32727273, 0.1205071149], [12.33636364, 0.09755931334], [12.34545455,
0.04744271434], [12.35454545, 0.007801978479], [12.36363636, 0.007059816169],
[12.37272727, 0.04062712074], [12.38181818, 0.07984546856], [12.39090909,

[0.09817561424], [12.40000000, 0.08812216532], [12.40909091, 0.05909938353],
[12.41818182, 0.02710628917], [12.42727273, 0.008488503486], [12.43636364,
0.01481733809], [12.44545455, 0.04261680723], [12.45454545, 0.06938746689],
[12.46363636, 0.07124304867], [12.47272727, 0.04798684120], [12.48181818,
0.02295722756], [12.49090909, 0.01630438698], [12.50000000, 0.02706935529],
[12.50909091, 0.04209298817], [12.51818182, 0.04998851965], [12.52727273,
0.04364216873], [12.53636364, 0.02497513829], [12.54545455, 0.01498905224],
[12.55454545, 0.04178606284], [12.56363636, 0.1030348538], [12.57272727,
0.1523924614], [12.58181818, 0.1429871260], [12.59090909, 0.08166067082],
[12.60000000, 0.02548985056], [12.60909091, 0.02524279189], [12.61818182,
0.08144687448], [12.62727273, 0.1505503488], [12.63636364, 0.1816678895],
[12.64545455, 0.1526818535], [12.65454545, 0.08763445941], [12.66363636,
0.04054116000], [12.67272727, 0.04873593055], [12.68181818, 0.09779593576],
[12.69090909, 0.1391924225], [12.70000000, 0.1406247944], [12.70909091,
0.1094176600], [12.71818182, 0.07065066028], [12.72727273, 0.03945939384],
[12.73636364, 0.01921920039], [12.74545455, 0.01219012490], [12.75454545,
0.02041306401], [12.76363636, 0.03953523494], [12.77272727, 0.05741466571],
[12.78181818, 0.05976036191], [12.79090909, 0.04132008089], [12.80000000,
0.01639768015], [12.80909091, 0.01128745675], [12.81818182, 0.03469220012],
[12.82727273, 0.06079665846], [12.83636364, 0.05793306736], [12.84545455,
0.03230957113], [12.85454545, 0.02296734813], [12.86363636, 0.04856212190],
[12.87272727, 0.08028352943], [12.88181818, 0.08015322463], [12.89090909,
0.04909183174], [12.90000000, 0.01946971909], [12.90909091, 0.01140928682],
[12.91818182, 0.01659118583], [12.92727273, 0.02063042610], [12.93636364,
0.02133858220], [12.94545455, 0.02191323009], [12.95454545, 0.02110270445],
[12.96363636, 0.01673674403], [12.97272727, 0.01086999399], [12.98181818,
0.006630025245], [12.99090909, 0.004527764251], [13.00000000, 0.003616608708],
[13.00909091, 0.002586489199], [13.01818182, 0.0007594679978], [13.02727273,
0.002833943170], [13.03636364, 0.01944551838], [13.04545455, 0.05409149443],
[13.05454545, 0.09001148391], [13.06363636, 0.1005083729], [13.07272727,
0.07666744254], [13.08181818, 0.03859065477], [13.09090909, 0.01563207048],
[13.10000000, 0.02047633228], [13.10909091, 0.04489469444], [13.11818182,
0.07385847665], [13.12727273, 0.09701860291], [13.13636364, 0.1087038477],
[13.14545455, 0.1038852362], [13.15454545, 0.07952003037], [13.16363636,
0.04244543412], [13.17272727, 0.01402667459], [13.18181818, 0.01857384133],
[13.19090909, 0.05949093487], [13.20000000, 0.1096995089], [13.20909091,

[0.1335319088], [13.21818182, 0.1178268483], [13.22727273, 0.07680531212],
[13.23636364, 0.03266164420], [13.24545455, 0.003672994072], [13.25454545,
0.006295031667], [13.26363636, 0.04631207517], [13.27272727, 0.09923747905],
[13.28181818, 0.1188978047], [13.29090909, 0.08390816825], [13.30000000,
0.02696114544], [13.30909091, 0.001011657829], [13.31818182, 0.02078023865],
[13.32727273, 0.05304511158], [13.33636364, 0.06113690774], [13.34545455,
0.04141961993], [13.35454545, 0.01549151318], [13.36363636, 0.004639814513],
[13.37272727, 0.01733371650], [13.38181818, 0.04565329791], [13.39090909,
0.06545604943], [13.40000000, 0.05425029747], [13.40909091, 0.02035382393],
[13.41818182, 0.002595212012], [13.42727273, 0.02678620951], [13.43636364,
0.07051018626], [13.44545455, 0.08713043454], [13.45454545, 0.06103175993],
[13.46363636, 0.02262822051], [13.47272727, 0.008052698238], [13.48181818,
0.02019948106], [13.49090909, 0.03573591921], [13.50000000, 0.03757629750],
[13.50909091, 0.02966226657], [13.51818182, 0.02574073017], [13.52727273,
0.03341408337], [13.53636364, 0.04819911844], [13.54545455, 0.05746483144],
[13.55454545, 0.05092515287], [13.56363636, 0.03150528725], [13.57272727,
0.01563677604], [13.58181818, 0.01986014802], [13.59090909, 0.04635065518],
[13.60000000, 0.08102100803], [13.60909091, 0.1033807126], [13.61818182,
0.09896256355], [13.62727273, 0.06843058177], [13.63636364, 0.02907369567],
[13.64545455, 0.004505895715], [13.65454545, 0.008303611498], [13.66363636,
0.03702442806], [13.67272727, 0.07758268247], [13.68181818, 0.1155670067],
[13.69090909, 0.1356448979], [13.70000000, 0.1250915368], [13.70909091,
0.08773786767], [13.71818182, 0.04961314225], [13.72727273, 0.03787380633],
[13.73636364, 0.05243015722], [13.74545455, 0.06761669960], [13.75454545,
0.06379326773], [13.76363636, 0.04787063201], [13.77272727, 0.03902036243],
[13.78181818, 0.04397580455], [13.79090909, 0.05378776398], [13.80000000,
0.05775984524], [13.80909091, 0.05163020337], [13.81818182, 0.03654062261],
[13.82727273, 0.01958284441], [13.83636364, 0.01358616423], [13.84545455,
0.02709176714], [13.85454545, 0.05364921793], [13.86363636, 0.07768305697],
[13.87272727, 0.09073429885], [13.88181818, 0.09482240573], [13.89090909,
0.09093098410], [13.90000000, 0.07532685818], [13.90909091, 0.05111154778],
[13.91818182, 0.03299695928], [13.92727273, 0.03217819789], [13.93636364,
0.04208551644], [13.94545455, 0.04687912867], [13.95454545, 0.04006790682],
[13.96363636, 0.02766829537], [13.97272727, 0.01754361781], [13.98181818,
0.01487700403], [13.99090909, 0.02479458033], [14.00000000, 0.04725878004],
[14.00909091, 0.06867478764], [14.01818182, 0.07160774522], [14.02727273,

[0.05883590560], [14.03636364, 0.05731315762], [14.04545455, 0.08863756832],
[14.05454545, 0.1413029764], [14.06363636, 0.1813452828], [14.07272727,
0.1864649593], [14.08181818, 0.1604234203], [14.09090909, 0.1182392408],
[14.10000000, 0.07230712050], [14.10909091, 0.03692819979], [14.11818182,
0.03222969969], [14.12727273, 0.06927537200], [14.13636364, 0.1320118113],
[14.14545455, 0.1827642798], [14.15454545, 0.1898260358], [14.16363636,
0.1500449188], [14.17272727, 0.08746919999], [14.18181818, 0.03357800562],
[14.19090909, 0.006852837147], [14.20000000, 0.005874677357], [14.20909091,
0.01902549701], [14.21818182, 0.03961798315], [14.22727273, 0.06870143743],
[14.23636364, 0.1022361235], [14.24545455, 0.1222851304], [14.25454545,
0.1100041796], [14.26363636, 0.06798552291], [14.27272727, 0.02262854559],
[14.28181818, 0.001219372652], [14.29090909, 0.01067827526], [14.30000000,
0.03953350870], [14.30909091, 0.07252045835], [14.31818182, 0.09703314498],
[14.32727273, 0.1019514844], [14.33636364, 0.08233657855], [14.34545455,
0.04806737231], [14.35454545, 0.02094981764], [14.36363636, 0.01864194999],
[14.37272727, 0.04249742828], [14.38181818, 0.08010569903], [14.39090909,
0.1144309288], [14.40000000, 0.1299762144], [14.40909091, 0.1181909721],
[14.41818182, 0.08401449581], [14.42727273, 0.04544079742], [14.43636364,
0.02230167303], [14.44545455, 0.02581132283], [14.45454545, 0.05851092158],
[14.46363636, 0.1158145417], [14.47272727, 0.1799104458], [14.48181818,
0.2196483712], [14.49090909, 0.2131503997], [14.50000000, 0.1745658018],
[14.50909091, 0.1447596611], [14.51818182, 0.1454620834], [14.52727273,
0.1521123027], [14.53636364, 0.1264641190], [14.54545455, 0.07219044196],
[14.55454545, 0.04015864339], [14.56363636, 0.07152258257], [14.57272727,
0.1473265903], [14.58181818, 0.2054239495], [14.59090909, 0.2021888764],
[14.60000000, 0.1481231382], [14.60909091, 0.08688321200], [14.61818182,
0.05247052293], [14.62727273, 0.04952602581], [14.63636364, 0.06314327114],
[14.64545455, 0.07703170049], [14.65454545, 0.08472661248], [14.66363636,
0.09162637551], [14.67272727, 0.1081060508], [14.68181818, 0.1368154755],
[14.69090909, 0.1655409375], [14.70000000, 0.1752899234], [14.70909091,
0.1567276808], [14.71818182, 0.1176493176], [14.72727273, 0.07503215719],
[14.73636364, 0.04233323771], [14.74545455, 0.02423241861], [14.75454545,
0.01957322983], [14.76363636, 0.02616507337], [14.77272727, 0.04284735342],
[14.78181818, 0.06724871422], [14.79090909, 0.09083355588], [14.80000000,
0.09840230924], [14.80909091, 0.07883129750], [14.81818182, 0.03993759344],
[14.82727273, 0.008276205319], [14.83636364, 0.007332298396], [14.84545455,

[0.03534172473], [14.85454545, 0.06850437534], [14.86363636, 0.08525363566],
[14.87272727, 0.08193298984], [14.88181818, 0.06545433019], [14.89090909,
0.04119792526], [14.90000000, 0.01563623885], [14.90909091, 0.003394064446],
[14.91818182, 0.01753166649], [14.92727273, 0.05002222768], [14.93636364,
0.07255596036], [14.94545455, 0.06490786255], [14.95454545, 0.03821840253],
[14.96363636, 0.02279657186], [14.97272727, 0.03468544434], [14.98181818,
0.06115045037], [14.99090909, 0.07852331142], [15.00000000, 0.07620323988],
[15.00909091, 0.06026865570], [15.01818182, 0.04115604560], [15.02727273,
0.02516658066], [15.03636364, 0.01505531307], [15.04545455, 0.01101092911],
[15.05454545, 0.009585019458], [15.06363636, 0.006493957175], [15.07272727,
0.002142526568], [15.08181818, 0.0006811742349], [15.09090909,
0.002547677253], [15.10000000, 0.003032522895], [15.10909091, 0.001529242404],
[15.11818182, 0.007193944217], [15.12727273, 0.02849557896], [15.13636364,
0.05834837735], [15.14545455, 0.07705989226], [15.15454545, 0.07286470377],
[15.16363636, 0.05472842323], [15.17272727, 0.04118513435], [15.18181818,
0.04010298642], [15.19090909, 0.04398991152], [15.20000000, 0.04264538503],
[15.20909091, 0.03438412797], [15.21818182, 0.02526204743], [15.22727273,
0.02438264282], [15.23636364, 0.04287699689], [15.24545455, 0.09030837577],
[15.25454545, 0.1628974285], [15.26363636, 0.2349716182], [15.27272727,
0.2699216770], [15.28181818, 0.2465585421], [15.29090909, 0.1763490210],
[15.30000000, 0.09452463431], [15.30909091, 0.03449514700], [15.31818182,
0.008584165909], [15.32727273, 0.007335993941], [15.33636364, 0.01233255581],
[15.34545455, 0.01098002858], [15.35454545, 0.004432612358], [15.36363636,
0.004527577799], [15.37272727, 0.02254166345], [15.38181818, 0.06014209440],
[15.39090909, 0.1110836024], [15.40000000, 0.1687627905], [15.40909091,
0.2266869537], [15.41818182, 0.2706732589], [15.42727273, 0.2784641653],
[15.43636364, 0.2367663391], [15.44545455, 0.1599260230], [15.45454545,
0.08463658700], [15.46363636, 0.04072781661], [15.47272727, 0.02875207399],
[15.48181818, 0.02857539380], [15.49090909, 0.02575295415], [15.50000000,
0.02305396932], [15.50909091, 0.02754994739], [15.51818182, 0.03573563968],
[15.52727273, 0.03717069252], [15.53636364, 0.02828531933], [15.54545455,
0.01548967969], [15.55454545, 0.005681080213], [15.56363636, 0.0008445684440],
[15.57272727, 0.003846273842], [15.58181818, 0.02222484558], [15.59090909,
0.05926795601], [15.60000000, 0.1036165700], [15.60909091, 0.1350456432],
[15.61818182, 0.1426113855], [15.62727273, 0.1326841617], [15.63636364,
0.1169302059], [15.64545455, 0.09733251184], [15.65454545, 0.06857549914],

[15.66363636, 0.03309626924], [15.67272727, 0.006262838386], [15.68181818, 0.002912638717], [15.69090909, 0.02180834804], [15.70000000, 0.04697961363], [15.70909091, 0.06319453014], [15.71818182, 0.06718643808], [15.72727273, 0.06487274480], [15.73636364, 0.06228459122], [15.74545455, 0.06151982299], [15.75454545, 0.06298209181], [15.76363636, 0.06807864242], [15.77272727, 0.07916517003], [15.78181818, 0.09772508893], [15.79090909, 0.1218381249], [15.80000000, 0.1440815936], [15.80909091, 0.1532698524], [15.81818182, 0.1417942971], [15.82727273, 0.1127983632], [15.83636364, 0.07835097003], [15.84545455, 0.04921042614], [15.85454545, 0.02814409136], [15.86363636, 0.01479895862], [15.87272727, 0.01369268277], [15.88181818, 0.03110458751], [15.89090909, 0.06232730500], [15.90000000, 0.08748037422], [15.90909091, 0.08647136048], [15.91818182, 0.05876599189], [15.92727273, 0.02456829617], [15.93636364, 0.005022111939], [15.94545455, 0.004005387048], [15.95454545, 0.01078344507], [15.96363636, 0.01641223847], [15.97272727, 0.02225622914], [15.98181818, 0.03317357173], [15.99090909, 0.04859232106], [16.00000000, 0.06389383289], [16.00909091, 0.07707341064], [16.01818182, 0.08891178955], [16.02727273, 0.09745047955], [16.03636364, 0.09810049601], [16.04545455, 0.09173446218], [16.05454545, 0.08814675223], [16.06363636, 0.09579048378], [16.07272727, 0.1084824439], [16.08181818, 0.1078178209], [16.09090909, 0.08230094372], [16.10000000, 0.04229701547], [16.10909091, 0.01293131375], [16.11818182, 0.01209487605], [16.12727273, 0.03664346337], [16.13636364, 0.06848808188], [16.14545455, 0.09025145498], [16.15454545, 0.09434653721], [16.16363636, 0.08205094373], [16.17272727, 0.06002980780], [16.18181818, 0.03850343185], [16.19090909, 0.02791282889], [16.20000000, 0.03278883648], [16.20909091, 0.04855088349], [16.21818182, 0.06599327791], [16.22727273, 0.07890826300], [16.23636364, 0.08625482773], [16.24545455, 0.08805783026], [16.25454545, 0.08269411552], [16.26363636, 0.06995958971], [16.27272727, 0.05440529313], [16.28181818, 0.04220312085], [16.29090909, 0.03474512951], [16.30000000, 0.02849364254], [16.30909091, 0.02273892927], [16.31818182, 0.02497508917], [16.32727273, 0.04491224083], [16.33636364, 0.08247120111], [16.34545455, 0.1238716239], [16.35454545, 0.1512337057], [16.36363636, 0.1558727514], [16.37272727, 0.1424542830], [16.38181818, 0.1223984943], [16.39090909, 0.1049814528], [16.40000000, 0.09287390030], [16.40909091, 0.08207252016], [16.41818182, 0.06499165129], [16.42727273, 0.03776090342], [16.43636364, 0.009214236919], [16.44545455, 0.001639776240], [16.45454545, 0.03590410071], [16.46363636, 0.1100922342], [16.47272727, 0.1934927088],

[16.48181818, 0.2468951872], [16.49090909, 0.2528872485], [16.50000000,
0.2267756604], [16.50909091, 0.1976192198], [16.51818182, 0.1800913870],
[16.52727273, 0.1660407601], [16.53636364, 0.1409228035], [16.54545455,
0.1032287684], [16.55454545, 0.06540015466], [16.56363636, 0.03897743834],
[16.57272727, 0.02395887251], [16.58181818, 0.01357104221], [16.59090909,
0.005213441764], [16.60000000, 0.002593135679], [16.60909091, 0.007812763313],
[16.61818182, 0.01554183390], [16.62727273, 0.01763205180], [16.63636364,
0.01243586242], [16.64545455, 0.007451669492], [16.65454545, 0.01256947315],
[16.66363636, 0.03172754491], [16.67272727, 0.06077742479], [16.68181818,
0.09136262271], [16.69090909, 0.1157158400], [16.70000000, 0.1293793594],
[16.70909091, 0.1320772549], [16.71818182, 0.1267697695], [16.72727273,
0.1164158808], [16.73636364, 0.1007091871], [16.74545455, 0.07725751662],
[16.75454545, 0.04756921006], [16.76363636, 0.02089368574], [16.77272727,
0.008874599221], [16.78181818, 0.01426542066], [16.79090909, 0.02616617676],
[16.80000000, 0.02925723782], [16.80909091, 0.01880487181], [16.81818182,
0.005175584543], [16.82727273, 0.002304326869], [16.83636364, 0.01261286544],
[16.84545455, 0.02498493126], [16.85454545, 0.02740202647], [16.86363636,
0.01944489639], [16.87272727, 0.01116610295], [16.88181818, 0.01124758856],
[16.89090909, 0.01866381317], [16.90000000, 0.02582893999], [16.90909091,
0.02707810925], [16.91818182, 0.02220153498], [16.92727273, 0.01377759408],
[16.93636364, 0.005298851661], [16.94545455, 0.003379496889], [16.95454545,
0.01816664265], [16.96363636, 0.05598148413], [16.97272727, 0.1091031041],
[16.98181818, 0.1551520410], [16.99090909, 0.1708655626], [17.00000000,
0.1493397301], [17.00909091, 0.1045472365], [17.01818182, 0.05920108602],
[17.02727273, 0.02834430896], [17.03636364, 0.01342524857], [17.04545455,
0.008761047285], [17.05454545, 0.009991892664], [17.06363636, 0.01553668300],
[17.07272727, 0.02285781727], [17.08181818, 0.02715024702], [17.09090909,
0.02495901009], [17.10000000, 0.01764856946], [17.10909091, 0.009881015908],
[17.11818182, 0.005105898592], [17.12727273, 0.003695541531], [17.13636364,
0.005142330908], [17.14545455, 0.01003352558], [17.15454545, 0.01837456934],
[17.16363636, 0.02682333914], [17.17272727, 0.02981403223], [17.18181818,
0.02458769736], [17.19090909, 0.01437322039], [17.20000000, 0.005525285029],
[17.20909091, 0.001810460082], [17.21818182, 0.002640894565], [17.22727273,
0.006857209021], [17.23636364, 0.01622498159], [17.24545455, 0.03304816690],
[17.25454545, 0.05437134498], [17.26363636, 0.07078603032], [17.27272727,
0.07314179132], [17.28181818, 0.06072865526], [17.29090909, 0.04188622683],

[17.30000000, 0.02627003591], [17.30909091, 0.01738078019], [17.31818182, 0.01301032019], [17.32727273, 0.01124981877], [17.33636364, 0.01324522583], [17.34545455, 0.01916731604], [17.35454545, 0.02409742053], [17.36363636, 0.02209464979], [17.37272727, 0.01638988972], [17.38181818, 0.02358485814], [17.39090909, 0.06328662177], [17.40000000, 0.1397538655], [17.40909091, 0.2325641109], [17.41818182, 0.3066752708], [17.42727273, 0.3344941448], [17.43636364, 0.3117292041], [17.44545455, 0.2554460694], [17.45454545, 0.1891095264], [17.46363636, 0.1288630657], [17.47272727, 0.08031762315], [17.48181818, 0.04352788218], [17.49090909, 0.01815133274], [17.50000000, 0.004478552788], [17.50909091, 0.002098712910], [17.51818182, 0.009223750516], [17.52727273, 0.02284353919], [17.53636364, 0.03845476465], [17.54545455, 0.05000944502], [17.55454545, 0.05209604929], [17.56363636, 0.04388286744], [17.57272727, 0.03077336735], [17.58181818, 0.02060812102], [17.59090909, 0.01702161746], [17.60000000, 0.01671371797], [17.60909091, 0.01409088895], [17.61818182, 0.008702516804], [17.62727273, 0.007224911098], [17.63636364, 0.01730516743], [17.64545455, 0.03964120226], [17.65454545, 0.06693250490], [17.66363636, 0.09084852460], [17.67272727, 0.1091981305], [17.68181818, 0.1253039494], [17.69090909, 0.1405716309], [17.70000000, 0.1492269134], [17.70909091, 0.1419890194], [17.71818182, 0.1154078145], [17.72727273, 0.07699063046], [17.73636364, 0.04049157819], [17.74545455, 0.01605011171], [17.75454545, 0.004835678685], [17.76363636, 0.002345035366], [17.77272727, 0.005140106231], [17.78181818, 0.01310851612], [17.79090909, 0.02571793956], [17.80000000, 0.03826471601], [17.80909091, 0.04396690988], [17.81818182, 0.04036178451], [17.82727273, 0.03271374514], [17.83636364, 0.02988100558], [17.84545455, 0.03631289150], [17.85454545, 0.04826444814], [17.86363636, 0.05797882665], [17.87272727, 0.06133830973], [17.88181818, 0.06126979004], [17.89090909, 0.06409136128], [17.90000000, 0.07322421915], [17.90909091, 0.08653143276], [17.91818182, 0.09881075741], [17.92727273, 0.1056487150], [17.93636364, 0.1047132738], [17.94545455, 0.09477521977], [17.95454545, 0.07556733096], [17.96363636, 0.04964162727], [17.97272727, 0.02357593143], [17.98181818, 0.005513826581], [17.99090909, 0.00005127524956], [18.00000000, 0.005155711494], [18.00909091, 0.01436069699], [18.01818182, 0.02209537083], [18.02727273, 0.02675132954], [18.03636364, 0.02889249108], [18.04545455, 0.02782432868], [18.05454545, 0.02173883708], [18.06363636, 0.01213446306], [18.07272727, 0.007103530289], [18.08181818, 0.01774286801], [18.09090909, 0.04874864638], [18.10000000, 0.09141515658], [18.10909091, 0.1267352268],

[18.11818182, 0.1376138648], [18.12727273, 0.1205176453], [18.13636364, 0.08688265660], [18.14545455, 0.05357002857], [18.15454545, 0.03104945168], [18.16363636, 0.01902229130], [18.17272727, 0.01148104283], [18.18181818, 0.004696672139], [18.19090909, 0.0003082508282], [18.20000000, 0.001813810168], [18.20909091, 0.009408560926], [18.21818182, 0.01880857289], [18.22727273, 0.02474682650], [18.23636364, 0.02510839245], [18.24545455, 0.02187605311], [18.25454545, 0.01902893740], [18.26363636, 0.02034028474], [18.27272727, 0.02882763230], [18.28181818, 0.04660453688], [18.29090909, 0.07322239092], [18.30000000, 0.1032505988], [18.30909091, 0.1264028263], [18.31818182, 0.1322383161], [18.32727273, 0.1169410606], [18.33636364, 0.08661512080], [18.34545455, 0.05370807738], [18.35454545, 0.02904366532], [18.36363636, 0.01587583020], [18.37272727, 0.01039898640], [18.38181818, 0.007169584802], [18.39090909, 0.003827161424], [18.40000000, 0.001199615846], [18.40909091, 0.0002047436013], [18.41818182, 0.0001457905005], [18.42727273, 0.0007550844220], [18.43636364, 0.005311877502], [18.44545455, 0.02007340488], [18.45454545, 0.04876359871], [18.46363636, 0.08656430148], [18.47272727, 0.1198812664], [18.48181818, 0.1336735463], [18.49090909, 0.1212585914], [18.50000000, 0.08880140553], [18.50909091, 0.05091850707], [18.51818182, 0.02117835605], [18.52727273, 0.005081601817], [18.53636364, 0.0001810916140], [18.54545455, 0.001495289365], [18.55454545, 0.006416904644], [18.56363636, 0.01510507371], [18.57272727, 0.02740695877], [18.58181818, 0.04047819278], [18.59090909, 0.04978548086], [18.60000000, 0.05223106679], [18.60909091, 0.04804911315], [18.61818182, 0.03980016576], [18.62727273, 0.03003180311], [18.63636364, 0.02032723028], [18.64545455, 0.01241110743], [18.65454545, 0.009222911133], [18.66363636, 0.01367147016], [18.67272727, 0.02554691345], [18.68181818, 0.03978813013], [18.69090909, 0.04876222946], [18.70000000, 0.04750828817], [18.70909091, 0.03760816506], [18.71818182, 0.02599482392], [18.72727273, 0.01937799780], [18.73636364, 0.01906009271], [18.74545455, 0.02073662940], [18.75454545, 0.01938276285], [18.76363636, 0.01462921127], [18.77272727, 0.01154768141], [18.78181818, 0.01601357929], [18.79090909, 0.02886961471], [18.80000000, 0.04428976369], [18.80909091, 0.05396982478], [18.81818182, 0.05355166695], [18.82727273, 0.04578021141], [18.83636364, 0.03790603885], [18.84545455, 0.03588420895], [18.85454545, 0.04040536231], [18.86363636, 0.04771327127], [18.87272727, 0.05373240930], [18.88181818, 0.05740230508], [18.89090909, 0.06045488464], [18.90000000, 0.06452845031], [18.90909091, 0.06886463594], [18.91818182, 0.07082465047], [18.92727273,

[0.06840448228], [18.93636364, 0.06199673832], [18.94545455, 0.05366845848],
[18.95454545, 0.04497443510], [18.96363636, 0.03588452368], [18.97272727,
0.02614158692], [18.98181818, 0.01757906417], [18.99090909, 0.01453105558],
[19.00000000, 0.02106994543], [19.00909091, 0.03702603521], [19.01818182,
0.05645320634], [19.02727273, 0.07053180172], [19.03636364, 0.07312120213],
[19.04545455, 0.06465954643], [19.05454545, 0.05124474581], [19.06363636,
0.03967461832], [19.07272727, 0.03257383864], [19.08181818, 0.02755464835],
[19.09090909, 0.02080401814], [19.10000000, 0.01167770775], [19.10909091,
0.004119223957], [19.11818182, 0.003604886152], [19.12727273, 0.01226228939],
[19.13636364, 0.02638606991], [19.14545455, 0.03850311243], [19.15454545,
0.04231966675], [19.16363636, 0.03662190142], [19.17272727, 0.02530257782],
[19.18181818, 0.01398951339], [19.19090909, 0.006317449240], [19.20000000,
0.002648137083], [19.20909091, 0.001528225369], [19.21818182, 0.001828343030],
[19.22727273, 0.003383664973], [19.23636364, 0.005906621453], [19.24545455,
0.007902419897], [19.25454545, 0.007332475136], [19.26363636, 0.003835694406],
[19.27272727, 0.0003580743395], [19.28181818, 0.002081839057], [19.29090909,
0.01277525633], [19.30000000, 0.03119721406], [19.30909091, 0.05065629634],
[19.31818182, 0.06260100119], [19.32727273, 0.06191679723], [19.33636364,
0.05008802540], [19.34545455, 0.03389075682], [19.35454545, 0.02066508167],
[19.36363636, 0.01376037468], [19.37272727, 0.01143239474], [19.38181818,
0.009622065248], [19.39090909, 0.006023657029], [19.40000000, 0.002068376941],
[19.40909091, 0.001407158062], [19.41818182, 0.006433389173], [19.42727273,
0.01588719534], [19.43636364, 0.02549957677], [19.44545455, 0.03101883730],
[19.45454545, 0.03105929497], [19.46363636, 0.02754352475], [19.47272727,
0.02365081335], [19.48181818, 0.02123052784], [19.49090909, 0.01987777650],
[19.50000000, 0.01821359916], [19.50909091, 0.01589883163], [19.51818182,
0.01432017670], [19.52727273, 0.01520470141], [19.53636364, 0.01844457260],
[19.54545455, 0.02132117975], [19.55454545, 0.02024087443], [19.56363636,
0.01388798185], [19.57272727, 0.005237474710], [19.58181818, 0.0004702722838],
[19.59090909, 0.005139482680], [19.60000000, 0.02015941018], [19.60909091,
0.04054320302], [19.61818182, 0.05795077778], [19.62727273, 0.06540758571],
[19.63636364, 0.06104754663], [19.64545455, 0.04852041832], [19.65454545,
0.03412897782], [19.66363636, 0.02296715302], [19.67272727, 0.01671932603],
[19.68181818, 0.01421750546], [19.69090909, 0.01368265254], [19.70000000,
0.01450316236], [19.70909091, 0.01714990727], [19.71818182, 0.02163301509],
[19.72727273, 0.02621601184], [19.73636364, 0.02785104015], [19.74545455,

[0.02424301709], [19.75454545, 0.01592235338], [19.76363636, 0.006504403179],
[19.77272727, 0.0006504138859], [19.78181818, 0.001074355966], [19.79090909,
0.006797124388], [19.80000000, 0.01401350626], [19.80909091, 0.01900739051],
[19.81818182, 0.02098875853], [19.82727273, 0.02273120151], [19.83636364,
0.02847907550], [19.84545455, 0.04059395862], [19.85454545, 0.05734348322],
[19.86363636, 0.07342726918], [19.87272727, 0.08289845058], [19.88181818,
0.08249604889], [19.89090909, 0.07321675342], [19.90000000, 0.05928982044],
[19.90909091, 0.04553901107], [19.91818182, 0.03508734056], [19.92727273,
0.02884347546], [19.93636364, 0.02669215209], [19.94545455, 0.02899781458],
[19.95454545, 0.03690985031], [19.96363636, 0.05107237990], [19.97272727,
0.06978721131], [19.98181818, 0.08831007656], [19.99090909, 0.1002607765],
[20.00000000, 0.1005926013], [20.00909091, 0.08832858325], [20.01818182,
0.06726207963], [20.02727273, 0.04408151635], [20.03636364, 0.02504251540],
[20.04545455, 0.01321918148], [20.05454545, 0.007904914417], [20.06363636,
0.006251808810], [20.07272727, 0.005783349141], [20.08181818, 0.005979267669],
[20.09090909, 0.007960053879], [20.10000000, 0.01274745358], [20.10909091,
0.01959636033], [20.11818182, 0.02577858408], [20.12727273, 0.02807410148],
[20.13636364, 0.02492741188], [20.14545455, 0.01769342864], [20.15454545,
0.01000408089], [20.16363636, 0.005595481843], [20.17272727, 0.006019647598],
[20.18181818, 0.009766155607], [20.19090909, 0.01337184666], [20.20000000,
0.01375961845], [20.20909091, 0.01023710181], [20.21818182, 0.004844221274],
[20.22727273, 0.0008712284978], [20.23636364, 0.0005946476015], [20.24545455,
0.003772001468], [20.25454545, 0.007884486931], [20.26363636, 0.009916585660],
[20.27272727, 0.008433464520], [20.28181818, 0.004544544353], [20.29090909,
0.001118952977], [20.30000000, 0.0008042546396], [20.30909091,
0.004194464019], [20.31818182, 0.009376930146], [20.32727273, 0.01315612373],
[20.33636364, 0.01313767957], [20.34545455, 0.009296239746], [20.35454545,
0.004002751933], [20.36363636, 0.0005033883820], [20.37272727,
0.0008481857488], [20.38181818, 0.004610128565], [20.39090909,
0.009206354120], [20.40000000, 0.01159123171], [20.40909091, 0.01021628064],
[20.41818182, 0.006000776392], [20.42727273, 0.001710098234], [20.43636364,
0.0001627758271], [20.44545455, 0.002423572320], [20.45454545,
0.007129099196], [20.46363636, 0.01135796898], [20.47272727, 0.01247782731],
[20.48181818, 0.009797038503], [20.49090909, 0.004989272108], [20.50000000,
0.001040645321], [20.50909091, 0.0003913997584], [20.51818182,
0.003432597874], [20.52727273, 0.008280860135], [20.53636364, 0.01195308611],

[20.54545455, 0.01220261672], [20.55454545, 0.008886072765], [20.56363636, 0.004034699656], [20.57272727, 0.0006045441563], [20.58181818, 0.0006800138942], [20.59090909, 0.00422218317], [20.60000000, 0.009107433802], [20.60909091, 0.01241496992], [20.61818182, 0.01217778101], [20.62727273, 0.008546895467], [20.63636364, 0.003686566167], [20.64545455, 0.0004796934679], [20.65454545, 0.0008232742199], [20.66363636, 0.004521174700], [20.67272727, 0.009414293164], [20.68181818, 0.01265479939], [20.69090909, 0.01236720538], [20.70000000, 0.008727968852], [20.70909091, 0.003848246768], [20.71818182, 0.0005443591621], [20.72727273, 0.0007172471053], [20.73636364, 0.004272991096], [20.74545455, 0.009191552669], [20.75454545, 0.01268805716], [20.76363636, 0.01279374085], [20.77272727, 0.009459195452], [20.78181818, 0.004567190854], [20.79090909, 0.0008639836618], [20.80000000, 0.0004212021191], [20.80909091, 0.003490120813], [20.81818182, 0.008376936155], [20.82727273, 0.01239255183], [20.83636364, 0.01333851766], [20.84545455, 0.01070703619], [20.85454545, 0.005944427192], [20.86363636, 0.001649062509], [20.87272727, 0.0001546449853], [20.88181818, 0.002273026328], [20.89090909, 0.006870208114], [20.90000000, 0.01148977723], [20.90909091, 0.01367466740], [20.91818182, 0.01227341121], [20.92727273, 0.008039081644], [20.93636364, 0.003215971763], [20.94545455, 0.0003473814871], [20.95454545, 0.0009413794303], [20.96363636, 0.004692992922], [20.97272727, 0.009658175089], [20.98181818, 0.01327411554], [20.99090909, 0.01368593538], [21.00000000, 0.01069317614], [21.00909091, 0.005837931987], [21.01818182, 0.001603800069], [21.02727273, 0.0001470427713], [21.03636364, 0.002209401755], [21.04545455, 0.006757174384], [21.05454545, 0.01151548359], [21.06363636, 0.01411572708], [21.07272727, 0.01327478695], [21.08181818, 0.009420957590], [21.09090909, 0.004467020344], [21.10000000, 0.0008566272625], [21.10909091, 0.0003634112877], [21.11818182, 0.003232672346], [21.12727273, 0.008076496660], [21.13636364, 0.01255989281], [21.14545455, 0.01453366322], [21.15454545, 0.01306287161], [21.16363636, 0.008861617511], [21.17272727, 0.003937920527], [21.18181818, 0.0006309637974], [21.19090909, 0.0005055219734], [21.20000000, 0.003625176707], [21.20909091, 0.008537192851], [21.21818182, 0.01296314398], [21.22727273, 0.01486234258], [21.23636364, 0.01337057551], [21.24545455, 0.009185228157], [21.25454545, 0.004230937906], [21.26363636, 0.0007714258485], [21.27272727, 0.0003804845888], [21.28181818,

[0.003239134301], [21.29090909, 0.008068521451], [21.30000000, 0.01271647655],
[21.30909091, 0.01512410468], [21.31818182, 0.01423674789], [21.32727273,
0.01045853349], [21.33636364, 0.005459769287], [21.34545455, 0.001433994565],
[21.35454545, 0.0001387008180], [21.36363636, 0.002139378103], [21.37272727,
0.006578672013], [21.38181818, 0.01155921855], [21.39090909, 0.01496442736],
[21.40000000, 0.01535964667], [21.40909091, 0.01259100594], [21.41818182,
0.007836065734], [21.42727273, 0.003096268297], [21.43636364,
0.0003541937657], [21.44545455, 0.0007520685667], [21.45454545,
0.004130120841], [21.46363636, 0.009106853800], [21.47272727, 0.01365705647],
[21.48181818, 0.01594202365], [21.49090909, 0.01505075188], [21.50000000,
0.01135565642], [21.50909091, 0.006348618226], [21.51818182, 0.002033902086],
[21.52727273, 0.0001282196611], [21.53636364, 0.001387625732], [21.54545455,
0.005322552655], [21.55454545, 0.01040364266], [21.56363636, 0.01466757064],
[21.57272727, 0.01647994800], [21.58181818, 0.01515868658], [21.59090909,
0.01122275706], [21.60000000, 0.006180292124], [21.60909091, 0.001946661403],
[21.61818182, 0.0001198310854], [21.62727273, 0.001387303143], [21.63636364,
0.005282156633], [21.64545455, 0.01037027013], [21.65454545, 0.01478971907],
[21.66363636, 0.01693670595], [21.67272727, 0.01604502394], [21.68181818,
0.01245200234], [21.69090909, 0.007462830740], [21.70000000, 0.002871512472],
[21.70909091, 0.0003171543696], [21.71818182, 0.0007072024867], [21.72727273,
0.003908695288], [21.73636364, 0.008808767626], [21.74545455, 0.01371416219],
[21.75454545, 0.01694325804], [21.76363636, 0.01740250631], [21.77272727,
0.01495096412], [21.78181818, 0.01043470701], [21.79090909, 0.005388029750],
[21.80000000, 0.001510209406], [21.80909091, 0.00009795556860], [21.81818182,
0.001622570455], [21.82727273, 0.005587081974], [21.83636364, 0.01070259555],
[21.84545455, 0.01531801909], [21.85454545, 0.01795760989], [21.86363636,
0.01779099968], [21.87272727, 0.01488775204], [21.88181818, 0.01018178293],
[21.89090909, 0.005164881497], [21.90000000, 0.001412678535], [21.90909091,
0.00009494979158], [21.91818182, 0.001621733407], [21.92727273,
0.005529811122], [21.93636364, 0.01063720077], [21.94545455, 0.01541121583],
[21.95454545, 0.01843337940], [21.96363636, 0.01881973553], [21.97272727,
0.01647341910], [21.98181818, 0.01210020554], [21.99090909, 0.006989600299],
[22.00000000, 0.002632014155], [22.00909091, 0.0002872161221], [22.01818182,
0.0006289041789], [22.02727273, 0.003563906201], [22.03636364,
0.008271516480], [22.04545455, 0.01344507188], [22.05454545, 0.01766232222],
[22.06363636, 0.01977844385], [22.07272727, 0.01923348482], [22.08181818,

0.01619355351], [22.09090909, 0.01149312941], [22.10000000, 0.006400442342],
[22.10909091, 0.002274007901], [22.11818182, 0.0002043503711], [22.12727273,
0.0007349760042], [22.13636364, 0.003732206947], [22.14545455,
0.008432250001], [22.15454545, 0.01364739598], [22.16363636, 0.01807367181],
[22.17272727, 0.02061921323], [22.18181818, 0.02067092298], [22.19090909,
0.01823581200], [22.20000000, 0.01392693686], [22.20909091, 0.008802973445],
[22.21818182, 0.004105370090], [22.22727273, 0.0009595515201], [22.23636364,
0.0001121680154], [22.24545455, 0.001764632197], [22.25454545,
0.005537980245], [22.26363636, 0.01057213635], [22.27272727, 0.01573174462],
[22.28181818, 0.01986786583], [22.29090909, 0.02207468879], [22.30000000,
0.02188444047], [22.30909091, 0.01936007810], [22.31818182, 0.01506968338],
[22.32727273, 0.009952907726], [22.33636364, 0.005112473982], [22.34545455,
0.001578012742], [22.35454545, 0.00009293495539], [22.36363636,
0.0009676363209], [22.37272727, 0.004026387220], [22.38181818,
0.008654673771], [22.39090909, 0.01393306190], [22.40000000, 0.01882705916],
[22.40909091, 0.02239298575], [22.41818182, 0.02395890059], [22.42727273,
0.02324672996], [22.43636364, 0.02041493499], [22.44545455, 0.01601733543],
[22.45454545, 0.01088973994], [22.46363636, 0.005988809500], [22.47272727,
0.002214962729], [22.48181818, 0.0002521744695], [22.49090909,
0.0004525270397], [22.50000000, 0.002783730352], [22.50909091,
0.006845630389], [22.51818182, 0.01194934256], [22.52727273, 0.01724226088],
[22.53636364, 0.02185543959], [22.54545455, 0.02504757370], [22.55454545,
0.02632202503], [22.56363636, 0.02549929462], [22.57272727, 0.02273572372],
[22.58181818, 0.01848843067], [22.59090909, 0.01343499368], [22.60000000,
0.008362877305], [22.60909091, 0.004047229452], [22.61818182, 0.001136143671],
[22.62727273, 0.00006000673829], [22.63636364, 0.0009767875673], [22.64545455,
0.003759002493], [22.65454545, 0.008021653046], [22.66363636, 0.01318465005],
[22.67272727, 0.01855888467], [22.68181818, 0.02344266298], [22.69090909,
0.02721483810], [22.70000000, 0.02941249612], [22.70909091, 0.02978407365],
[22.71818182, 0.02831273815], [22.72727273, 0.02520912098], [22.73636364,
0.02087646129], [22.74545455, 0.01585441113], [22.75454545, 0.01074984441],
[22.76363636, 0.006163860606], [22.77272727, 0.002623814647], [22.78181818,
0.0005278180758], [22.79090909, 0.0001070321712], [22.80000000,
0.001408552439], [22.80909091, 0.004299110938], [22.81818182, 0.008487504680],
[22.82727273, 0.01356182990], [22.83636364, 0.01903640976], [22.84545455,
0.02440280011], [22.85454545, 0.02917941160], [22.86363636, 0.03295499522],

[22.87272727, 0.03542235394], [22.88181818, 0.03639999301], [22.89090909, 0.03584083519], [22.90000000, 0.03382844975], [22.90909091, 0.03056235647], [22.91818182, 0.02633478487], [22.92727273, 0.02150175854], [22.93636364, 0.01645153258], [22.94545455, 0.01157327424], [22.95454545, 0.007228498471], [22.96363636, 0.003727223123], [22.97272727, 0.001310168109], [22.98181818, 0.0001376612872], [22.99090909, 0.0002852925347], [23.00000000, 0.001745824727], [23.00909091, 0.004436457339], [23.01818182, 0.008210260792], [23.02727273, 0.01287045824], [23.03636364, 0.01818621506], [23.04545455, 0.02390868519], [23.05454545, 0.02978623199], [23.06363636, 0.03557796293], [23.07272727, 0.04106496518], [23.08181818, 0.04605887886], [23.09090909, 0.05040767857], [23.10000000, 0.05399873509], [23.10909091, 0.05675939128], [23.11818182, 0.05865540264], [23.12727273, 0.05968766588], [23.13636364, 0.05988768982], [23.14545455, 0.05931225908], [23.15454545, 0.05803770876], [23.16363636, 0.05615417584], [23.17272727, 0.05376012778], [23.18181818, 0.05095739761], [23.19090909, 0.04784688407], [23.20000000, 0.04452500861], [23.20909091, 0.04108096301], [23.21818182, 0.03759473248], [23.22727273, 0.03413584184], [23.23636364, 0.03076274523], [23.24545455, 0.02752276321], [23.25454545, 0.02445246342], [23.26363636, 0.02157838017], [23.27272727, 0.01891797401], [23.28181818, 0.01648074138], [23.29090909, 0.01426939690], [23.30000000, 0.01228106377], [23.30909091, 0.01050842197], [23.31818182, 0.008940776676], [23.32727273, 0.007565021401], [23.33636364, 0.006366481005], [23.34545455, 0.005329628158], [23.35454545, 0.004438674034], [23.36363636, 0.003678039178], [23.37272727, 0.003032714221], [23.38181818, 0.002488522465], [23.39090909, 0.002032297564], [23.40000000, 0.001651989837], [23.40909091, 0.001336714358], [23.41818182, 0.001076753058], [23.42727273, 0.0008635219083], [23.43636364, 0.0006895128222], [23.44545455, 0.0005482184853], [23.45454545, 0.0004340468929], [23.46363636, 0.0003422310176], [23.47272727, 0.0002687378166], [23.48181818, 0.0002101797123], [23.49090909, 0.0001637307653], [23.50000000, 0.0001270489960], [23.50909091, 0.00009820570216], [23.51818182, 0.00007562213547], [23.52727273, 0.00005801354316], [23.53636364, 0.00004434031575], [23.54545455, 0.00003376580621], [23.55454545, 0.00002562027384], [23.56363636, 0.00001937034849], [23.57272727, 0.00001459339198], [23.58181818, 0.00001095614487], [23.59090909, 0.000008197076868], [23.60000000, 0.000006111903370], [23.60909091, 0.000004541781109], [23.61818182, 0.000003363750088], [23.62727273,

0.000002483042524], [23.63636364, 0.000001826931198], [23.64545455, 0.000001339837440], [23.65454545, 9.794624837 10^{-7}], [23.66363636, 7.137445548 10^{-7}], [23.67272727, 5.184779469 10^{-7}], [23.68181818, 3.754594865 10^{-7}], [23.69090909, 2.710526741 10^{-7}], [23.70000000, 1.950807107 10^{-7}], [23.70909091, 1.399770634 10^{-7}], [23.71818182, 1.001366260 10^{-7}], [23.72727273, 7.142230992 10^{-8}], [23.73636364, 5.079146740 10^{-8}], [23.74545455, 3.601424978 10^{-8}], [23.75454545, 2.546216314 10^{-8}], [23.76363636, 1.794997563 10^{-8}], [23.77272727, 1.261798992 10^{-8}], [23.78181818, 8.844720575 10^{-9}], [23.79090909, 6.182375190 10^{-9}], [23.80000000, 4.309365825 10^{-9}], [23.80909091, 2.995486748 10^{-9}], [23.81818182, 2.076474265 10^{-9}], [23.82727273, 1.435488466 10^{-9}], [23.83636364, 9.896817927 10^{-10}], [23.84545455, 6.804915153 10^{-10}], [23.85454545, 4.666480816 10^{-10}], [23.86363636, 3.191568022 10^{-10}], [23.87272727, 2.177081225 10^{-10}], [23.88181818, 1.481183867 10^{-10}], [23.89090909, 1.005112991 10^{-10}], [23.90000000, 6.802992436 10^{-11}], [23.90909091, 4.592738918 10^{-11}], [23.91818182, 3.092698191 10^{-11}], [23.92727273, 2.077325491 10^{-11}], [23.93636364, 1.391809758 10^{-11}], [23.94545455, 9.301874725 10^{-12}], [23.95454545, 6.201306913 10^{-12}], [23.96363636, 4.124058598 10^{-12}], [23.97272727, 2.735910655 10^{-12}], [23.98181818, 1.810593622 10^{-12}], [23.99090909, 1.195331756 10^{-12}], [24.00000000, 7.872462952 10^{-13}], [24.00909091, 5.172418907 10^{-13}], [24.01818182, 3.390343912 10^{-13}], [24.02727273, 2.217005778 10^{-13}], [24.03636364, 1.446334732 10^{-13}], [24.04545455, 9.413595859 10^{-14}], [24.05454545, 6.112695507 10^{-14}], [24.06363636, 3.960099562 10^{-14}], [24.07272727, 2.559653278 10^{-14}], [24.08181818, 1.650681774 10^{-14}], [24.09090909, 1.062082256 10^{-14}], [24.10000000, 6.818217633 10^{-15}], [24.10909091, 4.367236639 10^{-15}], [24.11818182, 2.791071268 10^{-15}], [24.12727273, 1.779789205 10^{-15}], [24.13636364, 1.132412584 10^{-15}], [24.14545455, 7.189260978 10^{-16}], [24.15454545, 4.554200601 10^{-16}], [24.16363636, 2.878679025 10^{-16}], [24.17272727, 1.815650616 10^{-16}], [24.18181818, 1.142704603 10^{-16}], [24.19090909, 7.176339465 10^{-17}], [24.20000000, 4.497217129 10^{-17}], [24.20909091, 2.812296772 10^{-17}], [24.21818182, 1.754928079 10^{-17}], [24.22727273, 1.092805325 10^{-17}], [24.23636364, 6.790722234 10^{-18}], [24.24545455, 4.210979737 10^{-18}], [24.25454545, 2.605845426 10^{-18}], [24.26363636, 1.609224760 10^{-18}], [24.27272727, 9.917255487 10^{-19}], [24.28181818,

$6.099260061 \cdot 10^{-19}$], [24.29090909, $3.743498771 \cdot 10^{-19}$], [24.30000000,
 $2.292963309 \cdot 10^{-19}$], [24.30909091, $1.401649144 \cdot 10^{-19}$], [24.31818182,
 $8.550829969 \cdot 10^{-20}$], [24.32727273, $5.206045937 \cdot 10^{-20}$], [24.33636364,
 $3.163316804 \cdot 10^{-20}$], [24.34545455, $1.918301175 \cdot 10^{-20}$], [24.35454545,
 $1.161007554 \cdot 10^{-20}$], [24.36363636, $7.012977536 \cdot 10^{-21}$], [24.37272727,
 $4.227894423 \cdot 10^{-21}$], [24.38181818, $2.543929723 \cdot 10^{-21}$], [24.39090909,
 $1.527741418 \cdot 10^{-21}$], [24.40000000, $9.157180802 \cdot 10^{-22}$], [24.40909091,
 $5.478260644 \cdot 10^{-22}$], [24.41818182, $3.271086858 \cdot 10^{-22}$], [24.42727273,
 $1.949425776 \cdot 10^{-22}$], [24.43636364, $1.159525506 \cdot 10^{-22}$], [24.44545455,
 $6.883410721 \cdot 10^{-23}$], [24.45454545, $4.078170032 \cdot 10^{-23}$], [24.46363636,
 $2.411308117 \cdot 10^{-23}$], [24.47272727, $1.422834290 \cdot 10^{-23}$], [24.48181818,
 $8.378428966 \cdot 10^{-24}$], [24.49090909, $4.923540103 \cdot 10^{-24}$], [24.50000000,
 $2.887424236 \cdot 10^{-24}$], [24.50909091, $1.690009834 \cdot 10^{-24}$], [24.51818182,
 $9.873233726 \cdot 10^{-25}$], [24.52727273, $5.758201541 \cdot 10^{-25}$], [24.53636364,
 $3.353160177 \cdot 10^{-25}$], [24.54545455, $1.950087081 \cdot 10^{-25}$], [24.55454545,
 $1.132855889 \cdot 10^{-25}$], [24.56363636, $6.574806828 \cdot 10^{-26}$], [24.57272727,
 $3.812430871 \cdot 10^{-26}$], [24.58181818, $2.208458621 \cdot 10^{-26}$], [24.59090909,
 $1.277675199 \cdot 10^{-26}$], [24.60000000, $7.378734044 \cdot 10^{-27}$], [24.60909091,
 $4.250849978 \cdot 10^{-27}$], [24.61818182, $2.440838309 \cdot 10^{-27}$], [24.62727273,
 $1.395633581 \cdot 10^{-27}$], [24.63636364, $7.939058201 \cdot 10^{-28}$], [24.64545455,
 $4.489035890 \cdot 10^{-28}$], [24.65454545, $2.521063193 \cdot 10^{-28}$], [24.66363636,
 $1.405198061 \cdot 10^{-28}$], [24.67272727, $7.766263045 \cdot 10^{-29}$], [24.68181818,
 $4.248946284 \cdot 10^{-29}$], [24.69090909, $2.292734917 \cdot 10^{-29}$], [24.70000000,
 $1.210198712 \cdot 10^{-29}$], [24.70909091, $6.137218001 \cdot 10^{-30}$], [24.71818182,
 $2.875702948 \cdot 10^{-30}$], [24.72727273, $1.138052443 \cdot 10^{-30}$], [24.73636364,
 $2.949861392 \cdot 10^{-31}$], [24.74545455, $1.988226608 \cdot 10^{-32}$], [24.75454545,
 $1.443601001 \cdot 10^{-31}$], [24.76363636, $5.727722194 \cdot 10^{-31}$], [24.77272727,
 $1.231495101 \cdot 10^{-30}$], [24.78181818, $2.040703339 \cdot 10^{-30}$], [24.79090909,
 $2.902730928 \cdot 10^{-30}$], [24.80000000, $3.703871331 \cdot 10^{-30}$], [24.80909091,
 $4.326783676 \cdot 10^{-30}$], [24.81818182, $4.669669736 \cdot 10^{-30}$], [24.82727273,
 $4.667138349 \cdot 10^{-30}$], [24.83636364, $4.307101507 \cdot 10^{-30}$], [24.84545455,
 $3.638725122 \cdot 10^{-30}$], [24.85454545, $2.768468146 \cdot 10^{-30}$], [24.86363636,
 $1.844158776 \cdot 10^{-30}$], [24.87272727, $1.030090895 \cdot 10^{-30}$], [24.88181818,
 $4.784082488 \cdot 10^{-31}$], [24.89090909, $3.029225859 \cdot 10^{-31}$], [24.90000000,
 $5.607629351 \cdot 10^{-31}$], [24.90909091, $1.245152109 \cdot 10^{-30}$], [24.91818182,
 $2.289820317 \cdot 10^{-30}$], [24.92727273, $3.582920258 \cdot 10^{-30}$], [24.93636364,

$4.986516926 \cdot 10^{-30}]$, [24.94545455, $6.357175937 \cdot 10^{-30}]$, [24.95454545, $7.563837652 \cdot 10^{-30}]$, [24.96363636, $8.500650844 \cdot 10^{-30}]$, [24.97272727, $9.094165289 \cdot 10^{-30}]$, [24.98181818, $9.305683152 \cdot 10^{-30}]$, [24.99090909, $9.130281067 \cdot 10^{-30}]$, [25.00000000, $8.593970218 \cdot 10^{-30}]$, [25.00909091, $7.749869561 \cdot 10^{-30}]$, [25.01818182, $6.673504090 \cdot 10^{-30}]$, [25.02727273, $5.456793810 \cdot 10^{-30}]$, [25.03636364, $4.200226557 \cdot 10^{-30}]$, [25.04545455, $3.003150483 \cdot 10^{-30}]$, [25.05454545, $1.952905526 \cdot 10^{-30}]$, [25.06363636, $1.114322015 \cdot 10^{-30}]$, [25.07272727, $5.216105108 \cdot 10^{-31}]$, [25.08181818, $1.746096627 \cdot 10^{-31}]$, [25.09090909, $4.068746111 \cdot 10^{-32}]$, [25.10000000, $6.244466589 \cdot 10^{-32}]$, [25.10909091, $1.700422024 \cdot 10^{-31}]$, [25.11818182, $2.958268630 \cdot 10^{-31}]$, [25.12727273, $3.882804274 \cdot 10^{-31}]$, [25.13636364, $4.223532923 \cdot 10^{-31}]$, [25.14545455, $4.039710601 \cdot 10^{-31}]$, [25.15454545, $3.677496796 \cdot 10^{-31}]$, [25.16363636, $3.684228625 \cdot 10^{-31}]$, [25.17272727, $4.678294719 \cdot 10^{-31}]$, [25.18181818, $7.202245531 \cdot 10^{-31}]$, [25.19090909, $1.158974265 \cdot 10^{-30}]$, [25.20000000, $1.787331788 \cdot 10^{-30}]$, [25.20909091, $2.575078092 \cdot 10^{-30}]$, [25.21818182, $3.461572382 \cdot 10^{-30}]$, [25.22727273, $4.364471345 \cdot 10^{-30}]$, [25.23636364, $5.192312642 \cdot 10^{-30}]$, [25.24545455, $5.858517119 \cdot 10^{-30}]$, [25.25454545, $6.294242286 \cdot 10^{-30}]$, [25.26363636, $6.457898743 \cdot 10^{-30}]$, [25.27272727, $6.339904079 \cdot 10^{-30}]$, [25.28181818, $5.962213067 \cdot 10^{-30}]$, [25.29090909, $5.373125195 \cdot 10^{-30}]$, [25.30000000, $4.638648842 \cdot 10^{-30}]$, [25.30909091, $3.832168739 \cdot 10^{-30}]$, [25.31818182, $3.024266328 \cdot 10^{-30}]$, [25.32727273, $2.274302912 \cdot 10^{-30}]$, [25.33636364, $1.624876668 \cdot 10^{-30}]$, [25.34545455, $1.099628930 \cdot 10^{-30}]$, [25.35454545, $7.042355437 \cdot 10^{-31}]$, [25.36363636, $4.298929828 \cdot 10^{-31}]$, [25.37272727, $2.582779146 \cdot 10^{-31}]$, [25.38181818, $1.668585021 \cdot 10^{-31}]$, [25.39090909, $1.335540816 \cdot 10^{-31}]$, [25.40000000, $1.400262398 \cdot 10^{-31}]$, [25.40909091, $1.732632801 \cdot 10^{-31}]$, [25.41818182, $2.255085224 \cdot 10^{-31}]$, [25.42727273, $2.929064389 \cdot 10^{-31}]$, [25.43636364, $3.734462258 \cdot 10^{-31}]$, [25.44545455, $4.648455610 \cdot 10^{-31}]$, [25.45454545, $5.629430981 \cdot 10^{-31}]$, [25.46363636, $6.609869774 \cdot 10^{-31}]$, [25.47272727, $7.499651823 \cdot 10^{-31}]$, [25.48181818, $8.198749672 \cdot 10^{-31}]$, [25.49090909, $8.616215445 \cdot 10^{-31}]$, [25.50000000, $8.691067849 \cdot 10^{-31}]$, [25.50909091, $8.410350002 \cdot 10^{-31}]$, [25.51818182, $7.820238365 \cdot 10^{-31}]$, [25.52727273, $7.027457154 \cdot 10^{-31}]$, [25.53636364, $6.190088136 \cdot 10^{-31}]$, [25.54545455, $5.498803708 \cdot 10^{-31}]$, [25.55454545, $5.151244510 \cdot 10^{-31}]$, [25.56363636, $5.323435049 \cdot 10^{-31}]$, [25.57272727, $6.142615500 \cdot 10^{-31}]$, [25.58181818, $7.665626502 \cdot 10^{-31}]$, [25.59090909,

$9.866099187 \cdot 10^{-31}]$, [25.60000000, $1.263235402 \cdot 10^{-30}$], [25.60909091, $1.577633655 \cdot 10^{-30}$], [25.61818182, $1.905236827 \cdot 10^{-30}$], [25.62727273, $2.218319240 \cdot 10^{-30}$], [25.63636364, $2.488991772 \cdot 10^{-30}$], [25.64545455, $2.692209874 \cdot 10^{-30}$], [25.65454545, $2.808434911 \cdot 10^{-30}$], [25.66363636, $2.825650076 \cdot 10^{-30}$], [25.67272727, $2.740527303 \cdot 10^{-30}$], [25.68181818, $2.558654800 \cdot 10^{-30}$], [25.69090909, $2.293849895 \cdot 10^{-30}$], [25.70000000, $1.966684001 \cdot 10^{-30}$], [25.70909091, $1.602424416 \cdot 10^{-30}$], [25.71818182, $1.228644425 \cdot 10^{-30}$], [25.72727273, $8.727665515 \cdot 10^{-31}$], [25.73636364, $5.597862081 \cdot 10^{-31}$], [25.74545455, $3.103799790 \cdot 10^{-31}$], [25.75454545, $1.395425595 \cdot 10^{-31}$], [25.76363636, $5.582784512 \cdot 10^{-32}$], [25.77272727, $6.120159263 \cdot 10^{-32}$], [25.78181818, $1.514528515 \cdot 10^{-31}$], [25.79090909, $3.170644222 \cdot 10^{-31}$], [25.80000000, $5.444120504 \cdot 10^{-31}$], [25.80909091, $8.171487238 \cdot 10^{-31}$], [25.81818182, $1.117633095 \cdot 10^{-30}$], [25.82727273, $1.428276955 \cdot 10^{-30}$], [25.83636364, $1.732712121 \cdot 10^{-30}$], [25.84545455, $2.016707960 \cdot 10^{-30}$], [25.85454545, $2.268803100 \cdot 10^{-30}$], [25.86363636, $2.480645267 \cdot 10^{-30}$], [25.87272727, $2.647058962 \cdot 10^{-30}$], [25.88181818, $2.765880296 \cdot 10^{-30}$], [25.89090909, $2.837610895 \cdot 10^{-30}$], [25.90000000, $2.864948520 \cdot 10^{-30}$], [25.90909091, $2.852251687 \cdot 10^{-30}$], [25.91818182, $2.804990298 \cdot 10^{-30}$], [25.92727273, $2.729225533 \cdot 10^{-30}$], [25.93636364, $2.631151556 \cdot 10^{-30}$], [25.94545455, $2.516720244 \cdot 10^{-30}$], [25.95454545, $2.391359292 \cdot 10^{-30}$], [25.96363636, $2.259784658 \cdot 10^{-30}$], [25.97272727, $2.125900733 \cdot 10^{-30}$], [25.98181818, $1.992776238 \cdot 10^{-30}$], [25.99090909, $1.862680677 \cdot 10^{-30}$], [26.00000000, $1.737164825 \cdot 10^{-30}$], [26.00909091, $1.617169163 \cdot 10^{-30}$], [26.01818182, $1.503145684 \cdot 10^{-30}$], [26.02727273, $1.395180933 \cdot 10^{-30}$], [26.03636364, $1.293110896 \cdot 10^{-30}$], [26.04545455, $1.196621300 \cdot 10^{-30}$], [26.05454545, $1.105329549 \cdot 10^{-30}$], [26.06363636, $1.018846902 \cdot 10^{-30}$], [26.07272727, $9.368213794 \cdot 10^{-31}$], [26.08181818, $8.589632585 \cdot 10^{-31}$], [26.09090909, $7.850559142 \cdot 10^{-31}$], [26.10000000, $7.149551932 \cdot 10^{-31}$], [26.10909091, $6.485805935 \cdot 10^{-31}$], [26.11818182, $5.859013150 \cdot 10^{-31}$], [26.12727273, $5.269198517 \cdot 10^{-31}$], [26.13636364, $4.716552945 \cdot 10^{-31}$], [26.14545455, $4.201279651 \cdot 10^{-31}$], [26.15454545, $3.723464736 \cdot 10^{-31}$], [26.16363636, $3.282978082 \cdot 10^{-31}$], [26.17272727, $2.879406705 \cdot 10^{-31}$], [26.18181818, $2.512019459 \cdot 10^{-31}$], [26.19090909, $2.179759840 \cdot 10^{-31}$], [26.20000000, $1.881262147 \cdot 10^{-31}$], [26.20909091, $1.614885607 \cdot 10^{-31}$], [26.21818182, $1.378760967 \cdot 10^{-31}$], [26.22727273, $1.170844360 \cdot 10^{-31}$], [26.23636364, $9.889739159 \cdot 10^{-32}$], [26.24545455,

$8.309253584 \cdot 10^{-32}]$, [26.25454545, $6.944637164 \cdot 10^{-32}]$, [26.26363636, $5.773891246 \cdot 10^{-32}]$, [26.27272727, $4.775754733 \cdot 10^{-32}]$, [26.28181818, $3.930013423 \cdot 10^{-32}]$, [26.29090909, $3.217732056 \cdot 10^{-32}]$, [26.30000000, $2.621413098 \cdot 10^{-32}]$, [26.30909091, $2.125089238 \cdot 10^{-32}]$, [26.31818182, $1.714358418 \cdot 10^{-32}]$, [26.32727273, $1.376371067 \cdot 10^{-32}]$, [26.33636364, $1.099779358 \cdot 10^{-32}]$, [26.34545455, $8.746578787 \cdot 10^{-33}]$, [26.35454545, $6.924042575 \cdot 10^{-33}]$, [26.36363636, $5.456272388 \cdot 10^{-33}]$, [26.37272727, $4.280285152 \cdot 10^{-33}]$, [26.38181818, $3.342834207 \cdot 10^{-33}]$, [26.39090909, $2.599244439 \cdot 10^{-33}]$, [26.40000000, $2.012304775 \cdot 10^{-33}]$, [26.40909091, $1.551238032 \cdot 10^{-33}]$, [26.41818182, $1.190760390 \cdot 10^{-33}]$, [26.42727273, $9.102365103 \cdot 10^{-34}]$, [26.43636364, $6.929313861 \cdot 10^{-34}]$, [26.44545455, $5.253563502 \cdot 10^{-34}]$, [26.45454545, $3.967040778 \cdot 10^{-34}]$, [26.46363636, $2.983657176 \cdot 10^{-34}]$, [26.47272727, $2.235223287 \cdot 10^{-34}]$, [26.48181818, $1.668024078 \cdot 10^{-34}]$, [26.49090909, $1.239973278 \cdot 10^{-34}]$, [26.50000000, $9.182684860 \cdot 10^{-35}]$, [26.50909091, $6.774740425 \cdot 10^{-35}]$, [26.51818182, $4.979653299 \cdot 10^{-35}]$, [26.52727273, $3.646753708 \cdot 10^{-35}]$, [26.53636364, $2.660918880 \cdot 10^{-35}]$, [26.54545455, $1.934600532 \cdot 10^{-35}]$, [26.55454545, $1.401527535 \cdot 10^{-35}]$, [26.56363636, $1.011762192 \cdot 10^{-35}]$, [26.57272727, $7.278421238 \cdot 10^{-36}]$, [26.58181818, $5.217866270 \cdot 10^{-36}]$, [26.59090909, $3.727867448 \cdot 10^{-36}]$, [26.60000000, $2.654325295 \cdot 10^{-36}]$, [26.60909091, $1.883597382 \cdot 10^{-36}]$, [26.61818182, $1.332220233 \cdot 10^{-36}]$, [26.62727273, $9.391424011 \cdot 10^{-37}]$, [26.63636364, $6.598838736 \cdot 10^{-37}]$, [26.64545455, $4.621650550 \cdot 10^{-37}]$, [26.65454545, $3.226508560 \cdot 10^{-37}]$, [26.66363636, $2.245365273 \cdot 10^{-37}]$, [26.67272727, $1.557656604 \cdot 10^{-37}]$, [26.68181818, $1.077206101 \cdot 10^{-37}]$, [26.69090909, $7.426425589 \cdot 10^{-38}]$, [26.70000000, $5.104182038 \cdot 10^{-38}]$, [26.70909091, $3.497428819 \cdot 10^{-38}]$, [26.71818182, $2.389235274 \cdot 10^{-38}]$, [26.72727273, $1.627297422 \cdot 10^{-38}]$, [26.73636364, $1.105053775 \cdot 10^{-38}]$, [26.74545455, $7.482015735 \cdot 10^{-39}]$, [26.75454545, $5.051061137 \cdot 10^{-39}]$, [26.76363636, $3.400050140 \cdot 10^{-39}]$, [26.77272727, $2.282109123 \cdot 10^{-39}]$, [26.78181818, $1.527374036 \cdot 10^{-39}]$, [26.79090909, $1.019346085 \cdot 10^{-39}]$, [26.80000000, $6.783820586 \cdot 10^{-40}]$, [26.80909091, $4.502072680 \cdot 10^{-40}]$, [26.81818182, $2.979510779 \cdot 10^{-40}]$, [26.82727273, $1.966438790 \cdot 10^{-40}]$, [26.83636364, $1.294277700 \cdot 10^{-40}]$, [26.84545455, $8.495608175 \cdot 10^{-41}]$, [26.85454545, $5.561471459 \cdot 10^{-41}]$, [26.86363636, $3.630958706 \cdot 10^{-41}]$, [26.87272727, $2.364271004 \cdot 10^{-41}]$, [26.88181818, $1.535413700 \cdot 10^{-41}]$, [26.89090909, $9.945199704 \cdot 10^{-42}]$, [26.90000000,

$6.424941180 \cdot 10^{-42}]$, $[26.90909091, 4.139995246 \cdot 10^{-42}]$, $[26.91818182, 2.660804327 \cdot 10^{-42}]$, $[26.92727273, 1.705751254 \cdot 10^{-42}]$, $[26.93636364, 1.090725007 \cdot 10^{-42}]$, $[26.94545455, 6.956946879 \cdot 10^{-43}]$, $[26.95454545, 4.426218818 \cdot 10^{-43}]$, $[26.96363636, 2.809083675 \cdot 10^{-43}]$, $[26.97272727, 1.778364582 \cdot 10^{-43}]$, $[26.98181818, 1.123072728 \cdot 10^{-43}]$, $[26.99090909, 7.075097859 \cdot 10^{-44}]$, $[27.00000000, 4.446322384 \cdot 10^{-44}]$, $[27.00909091, 2.787531094 \cdot 10^{-44}]$, $[27.01818182, 1.743391909 \cdot 10^{-44}]$, $[27.02727273, 1.087759881 \cdot 10^{-44}]$, $[27.03636364, 6.770797732 \cdot 10^{-45}]$, $[27.04545455, 4.204568568 \cdot 10^{-45}]$, $[27.05454545, 2.604856229 \cdot 10^{-45}]$, $[27.06363636, 1.610025079 \cdot 10^{-45}]$, $[27.07272727, 9.928276302 \cdot 10^{-46}]$, $[27.08181818, 6.108197799 \cdot 10^{-46}]$, $[27.09090909, 3.749349890 \cdot 10^{-46}]$, $[27.10000000, 2.296191142 \cdot 10^{-46}]$, $[27.10909091, 1.403055231 \cdot 10^{-46}]$, $[27.11818182, 8.553848788 \cdot 10^{-47}]$, $[27.12727273, 5.203239076 \cdot 10^{-47}]$, $[27.13636364, 3.158033111 \cdot 10^{-47}]$, $[27.14545455, 1.912473706 \cdot 10^{-47}]$, $[27.15454545, 1.155620692 \cdot 10^{-47}]$, $[27.16363636, 6.967568945 \cdot 10^{-48}]$, $[27.17272727, 4.191779163 \cdot 10^{-48}]$, $[27.18181818, 2.516353409 \cdot 10^{-48}]$, $[27.19090909, 1.507321545 \cdot 10^{-48}]$, $[27.20000000, 9.009611439 \cdot 10^{-49}]$, $[27.20909091, 5.373743058 \cdot 10^{-49}]$, $[27.21818182, 3.198329160 \cdot 10^{-49}]$, $[27.22727273, 1.899544770 \cdot 10^{-49}]$, $[27.23636364, 1.125798498 \cdot 10^{-49}]$, $[27.24545455, 6.658265970 \cdot 10^{-50}]$, $[27.25454545, 3.929664705 \cdot 10^{-50}]$, $[27.26363636, 2.314452251 \cdot 10^{-50}]$, $[27.27272727, 1.360328415 \cdot 10^{-50}]$, $[27.28181818, 7.978964362 \cdot 10^{-51}]$, $[27.29090909, 4.670472748 \cdot 10^{-51}]$, $[27.30000000, 2.728293111 \cdot 10^{-51}]$, $[27.30909091, 1.590528074 \cdot 10^{-51}]$, $[27.31818182, 9.253712429 \cdot 10^{-52}]$, $[27.32727273, 5.373028979 \cdot 10^{-52}]$, $[27.33636364, 3.113544129 \cdot 10^{-52}]$, $[27.34545455, 1.800643018 \cdot 10^{-52}]$, $[27.35454545, 1.039300235 \cdot 10^{-52}]$, $[27.36363636, 5.986862086 \cdot 10^{-53}]$, $[27.37272727, 3.441963682 \cdot 10^{-53}]$, $[27.38181818, 1.974995248 \cdot 10^{-53}]$, $[27.39090909, 1.131051737 \cdot 10^{-53}]$, $[27.40000000, 6.464864089 \cdot 10^{-54}]$, $[27.40909091, 3.688082867 \cdot 10^{-54}]$, $[27.41818182, 2.099955454 \cdot 10^{-54}]$, $[27.42727273, 1.193414738 \cdot 10^{-54}]$, $[27.43636364, 6.769371411 \cdot 10^{-55}]$, $[27.44545455, 3.832521651 \cdot 10^{-55}]$, $[27.45454545, 2.165727855 \cdot 10^{-55}]$, $[27.46363636, 1.221545846 \cdot 10^{-55}]$, $[27.47272727, 6.877108614 \cdot 10^{-56}]$, $[27.48181818, 3.864522048 \cdot 10^{-56}]$, $[27.49090909, 2.167619396 \cdot 10^{-56}]$, $[27.50000000, 1.213587544 \cdot 10^{-56}]$, $[27.50909091, 6.782089489 \cdot 10^{-57}]$, $[27.51818182, 3.783238294 \cdot 10^{-57}]$, $[27.52727273, 2.106566033 \cdot 10^{-57}]$, $[27.53636364, 1.170849439 \cdot 10^{-57}]$, $[27.54545455, 6.495984659 \cdot 10^{-58}]$, $[27.55454545,$

$3.597578125 \cdot 10^{-58}$], [27.56363636, $1.988841149 \cdot 10^{-58}$], [27.57272727, $1.097533710 \cdot 10^{-58}$], [27.58181818, $6.045981465 \cdot 10^{-59}$], [27.59090909, $3.324682396 \cdot 10^{-59}$], [27.60000000, $1.825034751 \cdot 10^{-59}$], [27.60909091, $1.000075810 \cdot 10^{-59}$], [27.61818182, $5.470646859 \cdot 10^{-60}$], [27.62727273, $2.987387456 \cdot 10^{-60}$], [27.63636364, $1.628525843 \cdot 10^{-60}$], [27.64545455, $8.862394521 \cdot 10^{-61}$], [27.65454545, $4.814640850 \cdot 10^{-61}$], [27.66363636, $2.611176046 \cdot 10^{-61}$], [27.67272727, $1.413744324 \cdot 10^{-61}$], [27.68181818, $7.641367070 \cdot 10^{-62}$], [27.69090909, $4.123250293 \cdot 10^{-62}$], [27.70000000, $2.221159476 \cdot 10^{-62}$], [27.70909091, $1.194521935 \cdot 10^{-62}$], [27.71818182, $6.413362350 \cdot 10^{-63}$], [27.72727273, $3.437617756 \cdot 10^{-63}$], [27.73636364, $1.839553496 \cdot 10^{-63}$], [27.74545455, $9.827728431 \cdot 10^{-64}$], [27.75454545, $5.241825916 \cdot 10^{-64}$], [27.76363636, $2.791281108 \cdot 10^{-64}$], [27.77272727, $1.483948706 \cdot 10^{-64}$], [27.78181818, $7.876464288 \cdot 10^{-65}$], [27.79090909, $4.173914885 \cdot 10^{-65}$], [27.80000000, $2.208302006 \cdot 10^{-65}$], [27.80909091, $1.166483663 \cdot 10^{-65}$], [27.81818182, $6.151866015 \cdot 10^{-66}$], [27.82727273, $3.239259710 \cdot 10^{-66}$], [27.83636364, $1.702934819 \cdot 10^{-66}$], [27.84545455, $8.938533645 \cdot 10^{-67}$], [27.85454545, $4.684391188 \cdot 10^{-67}$], [27.86363636, $2.451101299 \cdot 10^{-67}$], [27.87272727, $1.280540098 \cdot 10^{-67}$], [27.88181818, $6.679615937 \cdot 10^{-68}$], [27.89090909, $3.478874349 \cdot 10^{-68}$], [27.90000000, $1.809078741 \cdot 10^{-68}$], [27.90909091, $9.393126935 \cdot 10^{-69}$], [27.91818182, $4.869668604 \cdot 10^{-69}$], [27.92727273, $2.520737377 \cdot 10^{-69}$], [27.93636364, $1.302858466 \cdot 10^{-69}$], [27.94545455, $6.723737836 \cdot 10^{-70}$], [27.95454545, $3.464739840 \cdot 10^{-70}$], [27.96363636, $1.782703964 \cdot 10^{-70}$], [27.97272727, $9.158808356 \cdot 10^{-71}$], [27.98181818, $4.698424330 \cdot 10^{-71}$], [27.99090909, $2.406696863 \cdot 10^{-71}$], [28.00000000, $1.230973735 \cdot 10^{-71}$], [28.00909091, $6.286902932 \cdot 10^{-72}$], [28.01818182, $3.206177889 \cdot 10^{-72}$], [28.02727273, $1.632689754 \cdot 10^{-72}$], [28.03636364, $8.302085445 \cdot 10^{-73}$], [28.04545455, $4.215416387 \cdot 10^{-73}$], [28.05454545, $2.137301369 \cdot 10^{-73}$], [28.06363636, $1.082094753 \cdot 10^{-73}$], [28.07272727, $5.470679657 \cdot 10^{-74}$], [28.08181818, $2.761823710 \cdot 10^{-74}$], [28.09090909, $1.392295730 \cdot 10^{-74}$], [28.10000000, $7.008903420 \cdot 10^{-75}$], [28.10909091, $3.523334452 \cdot 10^{-75}$], [28.11818182, $1.768662732 \cdot 10^{-75}$], [28.12727273, $8.865958055 \cdot 10^{-76}$], [28.13636364, $4.438108680 \cdot 10^{-76}$], [28.14545455, $2.218522879 \cdot 10^{-76}$], [28.15454545, $1.107454010 \cdot 10^{-76}$], [28.16363636, $5.520588469 \cdot 10^{-77}$], [28.17272727, $2.748178872 \cdot 10^{-77}$], [28.18181818, $1.366175888 \cdot 10^{-77}$], [28.19090909, $6.782226157 \cdot 10^{-78}$], [28.20000000, $3.362358151 \cdot 10^{-78}$], [28.20909091,

$1.664653069 \cdot 10^{-78}$], [28.21818182, $8.230259961 \cdot 10^{-79}$], [28.22727273, $4.063641656 \cdot 10^{-79}$], [28.23636364, $2.003693334 \cdot 10^{-79}$], [28.24545455, $9.866498521 \cdot 10^{-80}$], [28.25454545, $4.851910130 \cdot 10^{-80}$], [28.26363636, $2.382770735 \cdot 10^{-80}$], [28.27272727, $1.168620487 \cdot 10^{-80}$], [28.28181818, $5.723851539 \cdot 10^{-81}$], [28.29090909, $2.799811146 \cdot 10^{-81}$], [28.30000000, $1.367717798 \cdot 10^{-81}$], [28.30909091, $6.672575551 \cdot 10^{-82}$], [28.31818182, $3.251034557 \cdot 10^{-82}$], [28.32727273, $1.581912969 \cdot 10^{-82}$], [28.33636364, $7.687379449 \cdot 10^{-83}$], [28.34545455, $3.730874010 \cdot 10^{-83}$], [28.35454545, $1.808344500 \cdot 10^{-83}$], [28.36363636, $8.753703887 \cdot 10^{-84}$], [28.37272727, $4.231987623 \cdot 10^{-84}$], [28.38181818, $2.043339486 \cdot 10^{-84}$], [28.39090909, $9.853306637 \cdot 10^{-85}$], [28.40000000, $4.745374790 \cdot 10^{-85}$], [28.40909091, $2.282484258 \cdot 10^{-85}$], [28.41818182, $1.096466843 \cdot 10^{-85}$], [28.42727273, $5.260600586 \cdot 10^{-86}$], [28.43636364, $2.520745076 \cdot 10^{-86}$], [28.44545455, $1.206362819 \cdot 10^{-86}$], [28.45454545, $5.766124395 \cdot 10^{-87}$], [28.46363636, $2.752635682 \cdot 10^{-87}$], [28.47272727, $1.312422688 \cdot 10^{-87}$], [28.48181818, $6.249720251 \cdot 10^{-88}$], [28.49090909, $2.972424660 \cdot 10^{-88}$], [28.50000000, $1.411972127 \cdot 10^{-88}$], [28.50909091, $6.698968411 \cdot 10^{-89}$], [28.51818182, $3.174371929 \cdot 10^{-89}$], [28.52727273, $1.502371330 \cdot 10^{-89}$], [28.53636364, $7.101790765 \cdot 10^{-90}$], [28.54545455, $3.352980802 \cdot 10^{-90}$], [28.55454545, $1.581132837 \cdot 10^{-90}$], [28.56363636, $7.446997818 \cdot 10^{-91}$], [28.57272727, $3.503250085 \cdot 10^{-91}$], [28.58181818, $1.646036886 \cdot 10^{-91}$], [28.59090909, $7.724812465 \cdot 10^{-92}$], [28.60000000, $3.620910014 \cdot 10^{-92}$], [28.60909091, $1.695236769 \cdot 10^{-92}$], [28.61818182, $7.927336112 \cdot 10^{-93}$], [28.62727273, $3.702626347 \cdot 10^{-93}$], [28.63636364, $1.727347168 \cdot 10^{-93}$], [28.64545455, $8.048925894 \cdot 10^{-94}$], [28.65454545, $3.746158911 \cdot 10^{-94}$], [28.66363636, $1.741509514 \cdot 10^{-94}$], [28.67272727, $8.086457568 \cdot 10^{-95}$], [28.68181818, $3.750463947 \cdot 10^{-95}$], [28.69090909, $1.737430010 \cdot 10^{-95}$], [28.70000000, $8.039456745 \cdot 10^{-96}$], [28.70909091, $3.715733607 \cdot 10^{-96}$], [28.71818182, $1.715387917 \cdot 10^{-96}$], [28.72727273, $7.910090657 \cdot 10^{-97}$], [28.73636364, $3.643370576 \cdot 10^{-97}$], [28.74545455, $1.676213916 \cdot 10^{-97}$], [28.75454545, $7.703022904 \cdot 10^{-98}$], [28.76363636, $3.535900512 \cdot 10^{-98}$], [28.77272727, $1.621240478 \cdot 10^{-98}$], [28.78181818, $7.425143515 \cdot 10^{-99}$], [28.79090909, $3.396829452 \cdot 10^{-99}$], [28.80000000, $1.552228230 \cdot 10^{-99}$], [28.80909091, $7.085195400 \cdot 10^{-100}$], [28.81818182, $3.230457139 \cdot 10^{-100}$], [28.82727273, $1.471273842 \cdot 10^{-100}$], [28.83636364, $6.693324922 \cdot 10^{-101}$], [28.84545455, $3.041659911 \cdot 10^{-101}$], [28.85454545, $1.380706088 \cdot 10^{-101}$], [28.86363636,

$6.260588456 \cdot 10^{-102}$], [28.87272727, $2.835658263 \cdot 10^{-102}$], [28.88181818, $1.282977181 \cdot 10^{-102}$], [28.89090909, $5.798447958 \cdot 10^{-103}$], [28.90000000, $2.617784340 \cdot 10^{-103}$], [28.90909091, $1.180556322 \cdot 10^{-103}$], [28.91818182, $5.318286974 \cdot 10^{-104}$], [28.92727273, $2.393263371 \cdot 10^{-104}$], [28.93636364, $1.075831699 \cdot 10^{-104}$], [28.94545455, $4.830974339 \cdot 10^{-105}$], [28.95454545, $2.167020894 \cdot 10^{-105}$], [28.96363636, $9.710259744 \cdot 10^{-106}$], [28.97272727, $4.346496813 \cdot 10^{-106}$], [28.98181818, $1.943524523 \cdot 10^{-106}$], [28.99090909, $8.681288235 \cdot 10^{-107}$], [29.00000000, $3.873674708 \cdot 10^{-107}$], [29.00909091, $1.726665643 \cdot 10^{-107}$], [29.01818182, $7.688484728 \cdot 10^{-108}$], [29.02727273, $3.419967110 \cdot 10^{-108}$], [29.03636364, $1.519682970 \cdot 10^{-108}$], [29.04545455, $6.745826371 \cdot 10^{-109}$], [29.05454545, $2.991366236 \cdot 10^{-109}$], [29.06363636, $1.325126760 \cdot 10^{-109}$], [29.07272727, $5.864078581 \cdot 10^{-110}$], [29.08181818, $2.592374485 \cdot 10^{-110}$], [29.09090909, $1.144859900 \cdot 10^{-110}$], [29.10000000, $5.050851678 \cdot 10^{-111}$], [29.10909091, $2.226053190 \cdot 10^{-111}$], [29.11818182, $9.800902368 \cdot 10^{-112}$], [29.12727273, $4.310792456 \cdot 10^{-112}$], [29.13636364, $1.894129122 \cdot 10^{-112}$], [29.14545455, $8.314273842 \cdot 10^{-113}$], [29.15454545, $3.645878350 \cdot 10^{-113}$], [29.16363636, $1.597143470 \cdot 10^{-113}$], [29.17272727, $6.989568527 \cdot 10^{-114}$], [29.18181818, $3.055781037 \cdot 10^{-114}$], [29.19090909, $1.334628039 \cdot 10^{-114}$], [29.20000000, $5.823245554 \cdot 10^{-115}$], [29.20909091, $2.538268058 \cdot 10^{-115}$], [29.21818182, $1.105294584 \cdot 10^{-115}$], [29.22727273, $4.808254119 \cdot 10^{-116}$], [29.23636364, $2.089614702 \cdot 10^{-116}$], [29.24545455, $9.072250970 \cdot 10^{-117}$], [29.25454545, $3.934907492 \cdot 10^{-117}$], [29.26363636, $1.705003247 \cdot 10^{-117}$], [29.27272727, $7.380532231 \cdot 10^{-118}$], [29.28181818, $3.191703264 \cdot 10^{-118}$], [29.29090909, $1.378892012 \cdot 10^{-118}$], [29.30000000, $5.951295151 \cdot 10^{-119}$], [29.30909091, $2.566059810 \cdot 10^{-119}$], [29.31818182, $1.105342023 \cdot 10^{-119}$], [29.32727273, $4.756656450 \cdot 10^{-120}$], [29.33636364, $2.044949897 \cdot 10^{-120}$], [29.34545455, $8.782940403 \cdot 10^{-121}$], [29.35454545, $3.768549175 \cdot 10^{-121}$], [29.36363636, $1.615422208 \cdot 10^{-121}$], [29.37272727, $6.917930040 \cdot 10^{-122}$], [29.38181818, $2.959683009 \cdot 10^{-122}$], [29.39090909, $1.265009639 \cdot 10^{-122}$], [29.40000000, $5.401604492 \cdot 10^{-123}$], [29.40909091, $2.304266870 \cdot 10^{-123}$], [29.41818182, $9.820296056 \cdot 10^{-124}$], [29.42727273, $4.181181219 \cdot 10^{-124}$], [29.43636364, $1.778512133 \cdot 10^{-124}$], [29.44545455, $7.557862108 \cdot 10^{-125}$], [29.45454545, $3.208679067 \cdot 10^{-125}$], [29.46363636, $1.360942304 \cdot 10^{-125}$], [29.47272727, $5.766870943 \cdot 10^{-126}$], [29.48181818, $2.441343245 \cdot 10^{-126}$], [29.49090909, $1.032539316 \cdot 10^{-126}$], [29.50000000, $4.362893198 \cdot 10^{-127}$], [29.50909091, $1.841763785 \cdot 10^{-127}$], [29.51818182,

$7.767581415 \cdot 10^{-128}$], [29.52727273, $3.272890340 \cdot 10^{-128}$], [29.53636364, $1.377755369 \cdot 10^{-128}$], [29.54545455, $5.794408297 \cdot 10^{-129}$], [29.55454545, $2.434690440 \cdot 10^{-129}$], [29.56363636, $1.022062554 \cdot 10^{-129}$], [29.57272727, $4.286587695 \cdot 10^{-130}$], [29.58181818, $1.796172084 \cdot 10^{-130}$], [29.59090909, $7.519477990 \cdot 10^{-131}$], [29.60000000, $3.145086061 \cdot 10^{-131}$], [29.60909091, $1.314268439 \cdot 10^{-131}$], [29.61818182, $5.487113975 \cdot 10^{-132}$], [29.62727273, $2.288832095 \cdot 10^{-132}$], [29.63636364, $9.538842358 \cdot 10^{-133}$], [29.64545455, $3.971832828 \cdot 10^{-133}$], [29.65454545, $1.652348336 \cdot 10^{-133}$], [29.66363636, $6.867986751 \cdot 10^{-134}$], [29.67272727, $2.852176209 \cdot 10^{-134}$], [29.68181818, $1.183434477 \cdot 10^{-134}$], [29.69090909, $4.906083838 \cdot 10^{-135}$], [29.70000000, $2.032125578 \cdot 10^{-135}$], [29.70909091, $8.409940327 \cdot 10^{-136}$], [29.71818182, $3.477475379 \cdot 10^{-136}$], [29.72727273, $1.436699652 \cdot 10^{-136}$], [29.73636364, $5.930628056 \cdot 10^{-137}$], [29.74545455, $2.446077305 \cdot 10^{-137}$], [29.75454545, $1.008036994 \cdot 10^{-137}$], [29.76363636, $4.150702191 \cdot 10^{-138}$], [29.77272727, $1.707683934 \cdot 10^{-138}$], [29.78181818, $7.019985524 \cdot 10^{-139}$], [29.79090909, $2.883432054 \cdot 10^{-139}$], [29.80000000, $1.183395637 \cdot 10^{-139}$], [29.80909091, $4.852872389 \cdot 10^{-140}$], [29.81818182, $1.988466798 \cdot 10^{-140}$], [29.82727273, $8.141234165 \cdot 10^{-141}$], [29.83636364, $3.330553422 \cdot 10^{-141}$], [29.84545455, $1.361440287 \cdot 10^{-141}$], [29.85454545, $5.560816451 \cdot 10^{-142}$], [29.86363636, $2.269540677 \cdot 10^{-142}$], [29.87272727, $9.255469470 \cdot 10^{-143}$], [29.88181818, $3.771564736 \cdot 10^{-143}$], [29.89090909, $1.535708576 \cdot 10^{-143}$], [29.90000000, $6.248296223 \cdot 10^{-144}$], [29.90909091, $2.540278473 \cdot 10^{-144}$], [29.91818182, $1.031975165 \cdot 10^{-144}$], [29.92727273, $4.189156388 \cdot 10^{-145}$], [29.93636364, $1.699238904 \cdot 10^{-145}$], [29.94545455, $6.887377810 \cdot 10^{-146}$], [29.95454545, $2.789497273 \cdot 10^{-146}$], [29.96363636, $1.128941509 \cdot 10^{-146}$], [29.97272727, $4.565530265 \cdot 10^{-147}$], [29.98181818, $1.844956099 \cdot 10^{-147}$], [29.99090909, $7.450004581 \cdot 10^{-148}$], [30.00000000, $3.006099362 \cdot 10^{-148}$], [30.00909091, $1.212067868 \cdot 10^{-148}$], [30.01818182, $4.883462121 \cdot 10^{-149}$], [30.02727273, $1.966103564 \cdot 10^{-149}$], [30.03636364, $7.909754236 \cdot 10^{-150}$], [30.04545455, $3.179786230 \cdot 10^{-150}$], [30.05454545, $1.277354543 \cdot 10^{-150}$], [30.06363636, $5.127478158 \cdot 10^{-151}$], [30.07272727, $2.056720216 \cdot 10^{-151}$], [30.08181818, $8.243769549 \cdot 10^{-152}$], [30.09090909, $3.301838929 \cdot 10^{-152}$], [30.10000000, $1.321495022 \cdot 10^{-152}$], [30.10909091, $5.285121726 \cdot 10^{-153}$], [30.11818182, $2.112148780 \cdot 10^{-153}$], [30.12727273, $8.434791308 \cdot 10^{-154}$], [30.13636364, $3.365928011 \cdot 10^{-154}$], [30.14545455, $1.342197226 \cdot 10^{-154}$], [30.15454545, $5.348220984 \cdot 10^{-155}$], [30.16363636, $2.129533080 \cdot 10^{-155}$], [30.17272727,

$8.473095965 \cdot 10^{-156}$], [30.18181818, $3.368862654 \cdot 10^{-156}$], [30.19090909, $1.338470530 \cdot 10^{-156}$], [30.20000000, $5.313976947 \cdot 10^{-157}$], [30.20909091, $2.108225330 \cdot 10^{-157}$], [30.21818182, $8.357997109 \cdot 10^{-158}$], [30.22727273, $3.311133740 \cdot 10^{-158}$], [30.23636364, $1.310817435 \cdot 10^{-158}$], [30.24545455, $5.185618043 \cdot 10^{-159}$], [30.25454545, $2.049999287 \cdot 10^{-159}$], [30.26363636, $8.098489114 \cdot 10^{-160}$], [30.27272727, $3.197082507 \cdot 10^{-160}$], [30.28181818, $1.261263655 \cdot 10^{-160}$], [30.29090909, $4.972364612 \cdot 10^{-161}$], [30.30000000, $1.958971705 \cdot 10^{-161}$], [30.30909091, $7.712669758 \cdot 10^{-162}$], [30.31818182, $3.034562961 \cdot 10^{-162}$], [30.32727273, $1.193180302 \cdot 10^{-162}$], [30.33636364, $4.688547833 \cdot 10^{-163}$], [30.34545455, $1.841183205 \cdot 10^{-163}$], [30.35454545, $7.225804734 \cdot 10^{-164}$], [30.36363636, $2.834068429 \cdot 10^{-164}$], [30.37272727, $1.110897007 \cdot 10^{-164}$], [30.38181818, $4.351922778 \cdot 10^{-165}$], [30.39090909, $1.703872650 \cdot 10^{-165}$], [30.40000000, $6.667244092 \cdot 10^{-166}$], [30.40909091, $2.607435555 \cdot 10^{-166}$], [30.41818182, $1.019162756 \cdot 10^{-166}$], [30.42727273, $3.981446920 \cdot 10^{-167}$], [30.43636364, $1.554570272 \cdot 10^{-167}$], [30.44545455, $6.066753321 \cdot 10^{-168}$], [30.45454545, $2.366373114 \cdot 10^{-168}$], [30.46363636, $9.225611929 \cdot 10^{-169}$], [30.47272727, $3.594977287 \cdot 10^{-169}$], [30.48181818, $1.400199079 \cdot 10^{-169}$], [30.49090909, $5.451040826 \cdot 10^{-170}$], [30.50000000, $2.121133848 \cdot 10^{-170}$], [30.50909091, $8.250082405 \cdot 10^{-171}$], [30.51818182, $3.207393236 \cdot 10^{-171}$], [30.52727273, $1.246382944 \cdot 10^{-171}$], [30.53636364, $4.841247522 \cdot 10^{-172}$], [30.54545455, $1.879620451 \cdot 10^{-172}$], [30.55454545, $7.294409057 \cdot 10^{-173}$], [30.56363636, $2.829544477 \cdot 10^{-173}$], [30.57272727, $1.097104845 \cdot 10^{-173}$], [30.58181818, $4.251899740 \cdot 10^{-174}$], [30.59090909, $1.647094695 \cdot 10^{-174}$], [30.60000000, $6.377515119 \cdot 10^{-175}$], [30.60909091, $2.468185539 \cdot 10^{-175}$], [30.61818182, $9.547568560 \cdot 10^{-176}$], [30.62727273, $3.691399379 \cdot 10^{-176}$], [30.63636364, $1.426482478 \cdot 10^{-176}$], [30.64545455, $5.509500197 \cdot 10^{-177}$], [30.65454545, $2.126771523 \cdot 10^{-177}$], [30.66363636, $8.205105985 \cdot 10^{-178}$], [30.67272727, $3.163686824 \cdot 10^{-178}$], [30.68181818, $1.219099891 \cdot 10^{-178}$], [30.69090909, $4.694740577 \cdot 10^{-179}$], [30.70000000, $1.806757295 \cdot 10^{-179}$], [30.70909091, $6.948527993 \cdot 10^{-180}$], [30.71818182, $2.670416058 \cdot 10^{-180}$], [30.72727273, $1.025524487 \cdot 10^{-180}$], [30.73636364, $3.935333321 \cdot 10^{-181}$], [30.74545455, $1.508941361 \cdot 10^{-181}$], [30.75454545, $5.781028608 \cdot 10^{-182}$], [30.76363636, $2.212921324 \cdot 10^{-182}$], [30.77272727, $8.463319908 \cdot 10^{-183}$], [30.78181818, $3.233813454 \cdot 10^{-183}$], [30.79090909, $1.234450762 \cdot 10^{-183}$], [30.80000000, $4.707627184 \cdot 10^{-184}$], [30.80909091, $1.793429983 \cdot 10^{-184}$], [30.81818182, $6.825039647 \cdot 10^{-185}$], [30.82727273,

$2.594468253 \cdot 10^{-185}$], [30.83636364, $9.851395224 \cdot 10^{-186}$], [30.84545455, $3.736257664 \cdot 10^{-186}$], [30.85454545, $1.415300963 \cdot 10^{-186}$], [30.86363636, $5.354471502 \cdot 10^{-187}$], [30.87272727, $2.023125640 \cdot 10^{-187}$], [30.88181818, $7.633958678 \cdot 10^{-188}$], [30.89090909, $2.876599355 \cdot 10^{-188}$], [30.90000000, $1.082413245 \cdot 10^{-188}$], [30.90909091, $4.066980165 \cdot 10^{-189}$], [30.91818182, $1.525797376 \cdot 10^{-189}$], [30.92727273, $5.715412974 \cdot 10^{-190}$], [30.93636364, $2.137488652 \cdot 10^{-190}$], [30.94545455, $7.980761349 \cdot 10^{-191}$], [30.95454545, $2.974728053 \cdot 10^{-191}$], [30.96363636, $1.106853086 \cdot 10^{-191}$], [30.97272727, $4.111013375 \cdot 10^{-192}$], [30.98181818, $1.524050751 \cdot 10^{-192}$], [30.99090909, $5.639179492 \cdot 10^{-193}$], [31.00000000, $2.082434907 \cdot 10^{-193}$], [31.00909091, $7.674280644 \cdot 10^{-194}$], [31.01818182, $2.822180596 \cdot 10^{-194}$], [31.02727273, $1.035574266 \cdot 10^{-194}$], [31.03636364, $3.791347127 \cdot 10^{-195}$], [31.04545455, $1.384796938 \cdot 10^{-195}$], [31.05454545, $5.045693869 \cdot 10^{-196}$], [31.06363636, $1.833822556 \cdot 10^{-196}$], [31.07272727, $6.647398437 \cdot 10^{-197}$], [31.08181818, $2.403018691 \cdot 10^{-197}$], [31.09090909, $8.662095105 \cdot 10^{-198}$], [31.10000000, $3.113108442 \cdot 10^{-198}$], [31.10909091, $1.115350846 \cdot 10^{-198}$], [31.11818182, $3.982996025 \cdot 10^{-199}$], [31.12727273, $1.417485404 \cdot 10^{-199}$], [31.13636364, $5.026436550 \cdot 10^{-200}$], [31.14545455, $1.775618612 \cdot 10^{-200}$], [31.15454545, $6.247316643 \cdot 10^{-201}$], [31.16363636, $2.188711680 \cdot 10^{-201}$], [31.17272727, $7.633449332 \cdot 10^{-202}$], [31.18181818, $2.649501522 \cdot 10^{-202}$], [31.19090909, $9.149108405 \cdot 10^{-203}$], [31.20000000, $3.142024736 \cdot 10^{-203}$], [31.20909091, $1.072716298 \cdot 10^{-203}$], [31.21818182, $3.639273810 \cdot 10^{-204}$], [31.22727273, $1.226281855 \cdot 10^{-204}$], [31.23636364, $4.101889167 \cdot 10^{-205}$], [31.24545455, $1.361292042 \cdot 10^{-205}$], [31.25454545, $4.479582052 \cdot 10^{-206}$], [31.26363636, $1.460796010 \cdot 10^{-206}$], [31.27272727, $4.718255042 \cdot 10^{-207}$], [31.28181818, $1.508896867 \cdot 10^{-207}$], [31.29090909, $4.777774522 \cdot 10^{-208}$], [31.30000000, $1.498926975 \cdot 10^{-208}$], [31.30909091, $4.668385532 \cdot 10^{-209}$], [31.31818182, $1.449284234 \cdot 10^{-209}$], [31.32727273, $4.518308033 \cdot 10^{-210}$], [31.33636364, $1.431853673 \cdot 10^{-210}$], [31.34545455, $4.691753725 \cdot 10^{-211}$], [31.35454545, $1.620495293 \cdot 10^{-211}$], [31.36363636, $5.986323766 \cdot 10^{-212}$], [31.37272727, $2.370762803 \cdot 10^{-212}$], [31.38181818, $9.952660284 \cdot 10^{-213}$], [31.39090909, $4.347255839 \cdot 10^{-213}$], [31.40000000, $1.939888567 \cdot 10^{-213}$], [31.40909091, $8.722366589 \cdot 10^{-214}$], [31.41818182, $3.916982408 \cdot 10^{-214}$], [31.42727273, $1.748040135 \cdot 10^{-214}$], [31.43636364, $7.732893077 \cdot 10^{-215}$], [31.44545455, $3.387509928 \cdot 10^{-215}$], [31.45454545, $1.469227026 \cdot 10^{-215}$], [31.46363636, $6.310766671 \cdot 10^{-216}$], [31.47272727, $2.685775029 \cdot 10^{-216}$], [31.48181818,

$1.133181604 \cdot 10^{-216}$], [31.49090909, $4.742727618 \cdot 10^{-217}$], [31.50000000,
 $1.970173536 \cdot 10^{-217}$], [31.50909091, $8.127593469 \cdot 10^{-218}$], [31.51818182,
 $3.331315491 \cdot 10^{-218}$], [31.52727273, $1.357256136 \cdot 10^{-218}$], [31.53636364,
 $5.498921732 \cdot 10^{-219}$], [31.54545455, $2.216271970 \cdot 10^{-219}$], [31.55454545,
 $8.888790583 \cdot 10^{-220}$], [31.56363636, $3.548676937 \cdot 10^{-220}$], [31.57272727,
 $1.410625506 \cdot 10^{-220}$], [31.58181818, $5.584501657 \cdot 10^{-221}$], [31.59090909,
 $2.202319788 \cdot 10^{-221}$], [31.60000000, $8.653393810 \cdot 10^{-222}$], [31.60909091,
 $3.388297846 \cdot 10^{-222}$], [31.61818182, $1.322322895 \cdot 10^{-222}$], [31.62727273,
 $5.144222861 \cdot 10^{-223}$], [31.63636364, $1.995208193 \cdot 10^{-223}$], [31.64545455,
 $7.716097267 \cdot 10^{-224}$], [31.65454545, $2.975764411 \cdot 10^{-224}$], [31.66363636,
 $1.144556125 \cdot 10^{-224}$], [31.67272727, $4.390925186 \cdot 10^{-225}$], [31.68181818,
 $1.680330922 \cdot 10^{-225}$], [31.69090909, $6.414900821 \cdot 10^{-226}$], [31.70000000,
 $2.443291427 \cdot 10^{-226}$], [31.70909091, $9.285007259 \cdot 10^{-227}$], [31.71818182,
 $3.520790252 \cdot 10^{-227}$], [31.72727273, $1.332221042 \cdot 10^{-227}$], [31.73636364,
 $5.030557994 \cdot 10^{-228}$], [31.74545455, $1.895761217 \cdot 10^{-228}$], [31.75454545,
 $7.130189747 \cdot 10^{-229}$], [31.76363636, $2.676637339 \cdot 10^{-229}$], [31.77272727,
 $1.002925644 \cdot 10^{-229}$], [31.78181818, $3.751088633 \cdot 10^{-230}$], [31.79090909,
 $1.400467024 \cdot 10^{-230}$], [31.80000000, $5.219537805 \cdot 10^{-231}$], [31.80909091,
 $1.942005964 \cdot 10^{-231}$], [31.81818182, $7.213455750 \cdot 10^{-232}$], [31.82727273,
 $2.675005623 \cdot 10^{-232}$], [31.83636364, $9.903941826 \cdot 10^{-233}$], [31.84545455,
 $3.661056563 \cdot 10^{-233}$], [31.85454545, $1.351238877 \cdot 10^{-233}$], [31.86363636,
 $4.979629189 \cdot 10^{-234}$], [31.87272727, $1.832366863 \cdot 10^{-234}$], [31.88181818,
 $6.732701453 \cdot 10^{-235}$], [31.89090909, $2.470235453 \cdot 10^{-235}$], [31.90000000,
 $9.050438597 \cdot 10^{-236}$], [31.90909091, $3.311258531 \cdot 10^{-236}$], [31.91818182,
 $1.209813350 \cdot 10^{-236}$], [31.92727273, $4.414229006 \cdot 10^{-237}$], [31.93636364,
 $1.608465426 \cdot 10^{-237}$], [31.94545455, $5.853262202 \cdot 10^{-238}$], [31.95454545,
 $2.127269211 \cdot 10^{-238}$], [31.96363636, $7.721361443 \cdot 10^{-239}$], [31.97272727,
 $2.799116013 \cdot 10^{-239}$], [31.98181818, $1.013472746 \cdot 10^{-239}$], [31.99090909,
 $3.665016594 \cdot 10^{-240}$], [32.00000000, $1.323795925 \cdot 10^{-240}$], [32.00909091,
 $4.775907482 \cdot 10^{-241}$], [32.01818182, $1.721032755 \cdot 10^{-241}$], [32.02727273,
 $6.194830118 \cdot 10^{-242}$], [32.03636364, $2.227334638 \cdot 10^{-242}$], [32.04545455,
 $7.999562663 \cdot 10^{-243}$], [32.05454545, $2.869992611 \cdot 10^{-243}$], [32.06363636,
 $1.028580562 \cdot 10^{-243}$], [32.07272727, $3.682547001 \cdot 10^{-244}$], [32.08181818,
 $1.317105086 \cdot 10^{-244}$], [32.09090909, $4.706137967 \cdot 10^{-245}$], [32.10000000,
 $1.679930187 \cdot 10^{-245}$], [32.10909091, $5.991157482 \cdot 10^{-246}$], [32.11818182,
 $2.134686375 \cdot 10^{-246}$], [32.12727273, $7.599281872 \cdot 10^{-247}$], [32.13636364,

$2.702948997 \cdot 10^{-247}$], [32.14545455, $9.605988893 \cdot 10^{-248}$], [32.15454545, $3.411126262 \cdot 10^{-248}$], [32.16363636, $1.210369615 \cdot 10^{-248}$], [32.17272727, $4.291570305 \cdot 10^{-249}$], [32.18181818, $1.520570102 \cdot 10^{-249}$], [32.19090909, $5.383976596 \cdot 10^{-250}$], [32.20000000, $1.905115900 \cdot 10^{-250}$], [32.20909091, $6.737157556 \cdot 10^{-251}$], [32.21818182, $2.381141107 \cdot 10^{-251}$], [32.22727273, $8.411302718 \cdot 10^{-252}$], [32.23636364, $2.969806629 \cdot 10^{-252}$], [32.24545455, $1.048087200 \cdot 10^{-252}$], [32.25454545, $3.697336756 \cdot 10^{-253}$], [32.26363636, $1.303831220 \cdot 10^{-253}$], [32.27272727, $4.596352463 \cdot 10^{-254}$], [32.28181818, $1.619884236 \cdot 10^{-254}$], [32.29090909, $5.707589424 \cdot 10^{-255}$], [32.30000000, $2.010662287 \cdot 10^{-255}$], [32.30909091, $7.082113416 \cdot 10^{-256}$], [32.31818182, $2.494271067 \cdot 10^{-256}$], [32.32727273, $8.784176371 \cdot 10^{-257}$], [32.33636364, $3.093531013 \cdot 10^{-257}$], [32.34545455, $1.089489421 \cdot 10^{-257}$], [32.35454545, $3.837296206 \cdot 10^{-258}$], [32.36363636, $1.351697385 \cdot 10^{-258}$], [32.37272727, $4.762147487 \cdot 10^{-259}$], [32.38181818, $1.678077324 \cdot 10^{-259}$], [32.39090909, $5.914559756 \cdot 10^{-260}$], [32.40000000, $2.085204600 \cdot 10^{-260}$], [32.40909091, $7.353666984 \cdot 10^{-261}$], [32.41818182, $2.594180373 \cdot 10^{-261}$], [32.42727273, $9.154776443 \cdot 10^{-262}$], [32.43636364, $3.231882539 \cdot 10^{-262}$], [32.44545455, $1.141381683 \cdot 10^{-262}$], [32.45454545, $4.032545670 \cdot 10^{-263}$], [32.46363636, $1.425294379 \cdot 10^{-263}$], [32.47272727, $5.039747516 \cdot 10^{-264}$], [32.48181818, $1.782757143 \cdot 10^{-264}$], [32.49090909, $6.308894934 \cdot 10^{-265}$], [32.50000000, $2.233515041 \cdot 10^{-265}$], [32.50909091, $7.910319719 \cdot 10^{-266}$], [32.51818182, $2.802607258 \cdot 10^{-266}$], [32.52727273, $9.933114728 \cdot 10^{-267}$], [32.53636364, $3.521714885 \cdot 10^{-267}$], [32.54545455, $1.248986316 \cdot 10^{-267}$], [32.55454545, $4.430818230 \cdot 10^{-268}$], [32.56363636, $1.572243875 \cdot 10^{-268}$], [32.57272727, $5.580224092 \cdot 10^{-269}$], [32.58181818, $1.980908213 \cdot 10^{-269}$], [32.59090909, $7.033032527 \cdot 10^{-270}$], [32.60000000, $2.497298829 \cdot 10^{-270}$], [32.60909091, $8.868122362 \cdot 10^{-271}$], [32.61818182, $3.149267203 \cdot 10^{-271}$], [32.62727273, $1.118374510 \cdot 10^{-271}$], [32.63636364, $3.971441173 \cdot 10^{-272}$], [32.64545455, $1.410182769 \cdot 10^{-272}$], [32.65454545, $5.006710692 \cdot 10^{-273}$], [32.66363636, $1.777309574 \cdot 10^{-273}$], [32.67272727, $6.307991988 \cdot 10^{-274}$], [32.68181818, $2.238313995 \cdot 10^{-274}$], [32.69090909, $7.940310701 \cdot 10^{-275}$], [32.70000000, $2.815955928 \cdot 10^{-275}$], [32.70909091, $9.983247882 \cdot 10^{-276}$], [32.71818182, $3.538032483 \cdot 10^{-276}$], [32.72727273, $1.253379585 \cdot 10^{-276}$], [32.73636364, $4.438351731 \cdot 10^{-277}$], [32.74545455, $1.570967361 \cdot 10^{-277}$], [32.75454545, $5.557859902 \cdot 10^{-278}$], [32.76363636, $1.965315363 \cdot 10^{-278}$], [32.77272727, $6.945938687 \cdot 10^{-279}$], [32.78181818, $2.453545332 \cdot 10^{-279}$], [32.79090909,

$8.661889615 \cdot 10^{-280}$], [32.80000000, $3.056174516 \cdot 10^{-280}$], [32.80909091, $1.077662259 \cdot 10^{-280}$], [32.81818182, $3.797683900 \cdot 10^{-281}$], [32.82727273, $1.337456532 \cdot 10^{-281}$], [32.83636364, $4.707158897 \cdot 10^{-282}$], [32.84545455, $1.655580989 \cdot 10^{-282}$], [32.85454545, $5.819007472 \cdot 10^{-283}$], [32.86363636, $2.043851172 \cdot 10^{-283}$], [32.87272727, $7.173760359 \cdot 10^{-284}$], [32.88181818, $2.516155493 \cdot 10^{-284}$], [32.89090909, $8.818957592 \cdot 10^{-285}$], [32.90000000, $3.088749691 \cdot 10^{-285}$], [32.90909091, $1.081012513 \cdot 10^{-285}$], [32.91818182, $3.780580303 \cdot 10^{-286}$], [32.92727273, $1.321184486 \cdot 10^{-286}$], [32.93636364, $4.613638155 \cdot 10^{-287}$], [32.94545455, $1.609892092 \cdot 10^{-287}$], [32.95454545, $5.613342740 \cdot 10^{-288}$], [32.96363636, $1.955764510 \cdot 10^{-288}$], [32.97272727, $6.808958359 \cdot 10^{-289}$], [32.98181818, $2.368716412 \cdot 10^{-289}$], [32.99090909, $8.234043011 \cdot 10^{-290}$], [33.00000000, $2.860095238 \cdot 10^{-290}$], [33.00909091, $9.926931322 \cdot 10^{-291}$], [33.01818182, $3.442839496 \cdot 10^{-291}$], [33.02727273, $1.193125334 \cdot 10^{-291}$], [33.03636364, $4.131648791 \cdot 10^{-292}$], [33.04545455, $1.429649196 \cdot 10^{-292}$], [33.05454545, $4.943166668 \cdot 10^{-293}$], [33.06363636, $1.707858309 \cdot 10^{-293}$], [33.07272727, $5.896177808 \cdot 10^{-294}$], [33.08181818, $2.034056449 \cdot 10^{-294}$], [33.09090909, $7.011821865 \cdot 10^{-295}$], [33.10000000, $2.415328179 \cdot 10^{-295}$], [33.10909091, $8.313827106 \cdot 10^{-296}$], [33.11818182, $2.859616361 \cdot 10^{-296}$], [33.12727273, $9.828768205 \cdot 10^{-297}$], [33.13636364, $3.375808143 \cdot 10^{-297}$], [33.14545455, $1.158635396 \cdot 10^{-297}$], [33.15454545, $3.973831531 \cdot 10^{-298}$], [33.16363636, $1.361975245 \cdot 10^{-298}$], [33.17272727, $4.664765217 \cdot 10^{-299}$], [33.18181818, $1.596596319 \cdot 10^{-299}$], [33.19090909, $5.460965036 \cdot 10^{-300}$], [33.20000000, $1.866624791 \cdot 10^{-300}$], [33.20909091, $6.376211133 \cdot 10^{-301}$], [33.21818182, $2.176663451 \cdot 10^{-301}$], [33.22727273, $7.425880778 \cdot 10^{-302}$], [33.23636364, $2.531851057 \cdot 10^{-302}$], [33.24545455, $8.627152514 \cdot 10^{-303}$], [33.25454545, $2.937932606 \cdot 10^{-303}$], [33.26363636, $9.999248084 \cdot 10^{-304}$], [33.27272727, $3.401342633 \cdot 10^{-304}$], [33.28181818, $1.156371920 \cdot 10^{-304}$], [33.29090909, $3.929303863 \cdot 10^{-305}$], [33.30000000, $1.334478653 \cdot 10^{-305}$], [33.30909091, $4.529943548 \cdot 10^{-306}$], [33.31818182, $1.536973830 \cdot 10^{-306}$], [33.32727273, $5.212429763 \cdot 10^{-307}$], [33.33636364, $1.766939531 \cdot 10^{-307}$], [33.34545455, $5.987129625 \cdot 10^{-308}$], [33.35454545, $2.027864767 \cdot 10^{-308}$], [33.36363636, $6.865790853 \cdot 10^{-309}$], [33.37272727, $2.323706679 \cdot 10^{-309}$], [33.38181818, $7.861747188 \cdot 10^{-310}$], [33.39090909, $2.658959207 \cdot 10^{-310}$], [33.40000000, $8.990146955 \cdot 10^{-311}$], [33.40909091, $3.038728779 \cdot 10^{-311}$], [33.41818182, $1.026820233 \cdot 10^{-311}$], [33.42727273, $3.468815926 \cdot 10^{-312}$], [33.43636364, $1.171545481 \cdot 10^{-312}$], [33.44545455,

$3.955801011 \cdot 10^{-313}], [33.45454545, 1.335404992 \cdot 10^{-313}], [33.46363636,$
 $4.507131479 \cdot 10^{-314}], [33.47272727, 1.520901156 \cdot 10^{-314}], [33.48181818,$
 $5.131207168 \cdot 10^{-315}], [33.49090909, 1.730850395 \cdot 10^{-315}], [33.50000000,$
 $5.837459518 \cdot 10^{-316}], [33.50909091, 1.968406742 \cdot 10^{-316}], [33.51818182,$
 $6.636420188 \cdot 10^{-317}], [33.52727273, 2.237081320 \cdot 10^{-317}], [33.53636364,$
 $7.539777720 \cdot 10^{-318}], [33.54545455, 2.540757287 \cdot 10^{-318}], [33.55454545,$
 $8.560428413 \cdot 10^{-319}], [33.56363636, 2.883712955 \cdot 10^{-319}], [33.57272727,$
 $9.712342466 \cdot 10^{-320}], [33.58181818, 3.270714575 \cdot 10^{-320}], [33.59090909,$
 $1.101272325 \cdot 10^{-320}], [33.60000000, 3.705492344 \cdot 10^{-321}], [33.60909091,$
 $1.245045428 \cdot 10^{-321}], [33.61818182, 4.199557990 \cdot 10^{-322}], [33.62727273,$
 $1.432790373 \cdot 10^{-322}], [33.63636364, 4.940656458 \cdot 10^{-323}], [33.64545455,$
 $1.482196938 \cdot 10^{-323}], [33.65454545, 4.940656458 \cdot 10^{-324}], [33.66363636, 0.],$
[33.67272727, 0.], [33.68181818, 0.], [33.69090909, 0.], [33.70000000, 0.],
[33.70909091, 0.], [33.71818182, 0.], [33.72727273, 0.], [33.73636364, 0.],
[33.74545455, 0.], [33.75454545, 0.], [33.76363636, 0.], [33.77272727, 0.],
[33.78181818, 0.], [33.79090909, 0.], [33.80000000, 0.], [33.80909091, 0.],
[33.81818182, 0.], [33.82727273, 0.], [33.83636364, 0.], [33.84545455, 0.],
[33.85454545, 0.], [33.86363636, 0.], [33.87272727, 0.], [33.88181818, 0.],
[33.89090909, 0.], [33.90000000, 0.], [33.90909091, 0.], [33.91818182, 0.],
[33.92727273, 0.], [33.93636364, 0.], [33.94545455, 0.], [33.95454545, 0.],
[33.96363636, 0.], [33.97272727, 0.], [33.98181818, 0.], [33.99090909, 0.],
[34.00000000, 0.], [34.00909091, 0.], [34.01818182, 0.], [34.02727273, 0.],
[34.03636364, 0.], [34.04545455, 0.], [34.05454545, 0.], [34.06363636, 0.],
[34.07272727, 0.], [34.08181818, 0.], [34.09090909, 0.], [34.10000000, 0.],
[34.10909091, 0.], [34.11818182, 0.], [34.12727273, 0.], [34.13636364, 0.],
[34.14545455, 0.], [34.15454545, 0.], [34.16363636, 0.], [34.17272727, 0.],
[34.18181818, 0.], [34.19090909, 0.], [34.20000000, 0.], [34.20909091, 0.],
[34.21818182, 0.], [34.22727273, 0.], [34.23636364, 0.], [34.24545455, 0.],
[34.25454545, 0.], [34.26363636, 0.], [34.27272727, 0.], [34.28181818, 0.],
[34.29090909, 0.], [34.30000000, 0.], [34.30909091, 0.], [34.31818182, 0.],
[34.32727273, 0.], [34.33636364, 0.], [34.34545455, 0.], [34.35454545, 0.],
[34.36363636, 0.], [34.37272727, 0.], [34.38181818, 0.], [34.39090909, 0.],
[34.40000000, 0.], [34.40909091, 0.], [34.41818182, 0.], [34.42727273, 0.],
[34.43636364, 0.], [34.44545455, 0.], [34.45454545, 0.], [34.46363636, 0.],
[34.47272727, 0.], [34.48181818, 0.], [34.49090909, 0.], [34.50000000, 0.],
[34.50909091, 0.], [34.51818182, 0.], [34.52727273, 0.], [34.53636364, 0.],

[34.54545455, 0.], [34.55454545, 0.], [34.56363636, 0.], [34.57272727, 0.],
[34.58181818, 0.], [34.59090909, 0.], [34.60000000, 0.], [34.60909091, 0.],
[34.61818182, 0.], [34.62727273, 0.], [34.63636364, 0.], [34.64545455, 0.],
[34.65454545, 0.], [34.66363636, 0.], [34.67272727, 0.], [34.68181818, 0.],
[34.69090909, 0.], [34.70000000, 0.], [34.70909091, 0.], [34.71818182, 0.],
[34.72727273, 0.], [34.73636364, 0.], [34.74545455, 0.], [34.75454545, 0.],
[34.76363636, 0.], [34.77272727, 0.], [34.78181818, 0.], [34.79090909, 0.],
[34.80000000, 0.], [34.80909091, 0.], [34.81818182, 0.], [34.82727273, 0.],
[34.83636364, 0.], [34.84545455, 0.], [34.85454545, 0.], [34.86363636, 0.],
[34.87272727, 0.], [34.88181818, 0.], [34.89090909, 0.], [34.90000000, 0.],
[34.90909091, 0.], [34.91818182, 0.], [34.92727273, 0.], [34.93636364, 0.],
[34.94545455, 0.], [34.95454545, 0.], [34.96363636, 0.], [34.97272727, 0.],
[34.98181818, 0.], [34.99090909, 0.], [35.00000000, 0.], [35.00909091, 0.],
[35.01818182, 0.], [35.02727273, 0.], [35.03636364, 0.], [35.04545455, 0.],
[35.05454545, 0.], [35.06363636, 0.], [35.07272727, 0.], [35.08181818, 0.],
[35.09090909, 0.], [35.10000000, 0.], [35.10909091, 0.], [35.11818182, 0.],
[35.12727273, 0.], [35.13636364, 0.], [35.14545455, 0.], [35.15454545, 0.],
[35.16363636, 0.], [35.17272727, 0.], [35.18181818, 0.], [35.19090909, 0.],
[35.20000000, 0.], [35.20909091, 0.], [35.21818182, 0.], [35.22727273, 0.],
[35.23636364, 0.], [35.24545455, 0.], [35.25454545, 0.], [35.26363636, 0.],
[35.27272727, 0.], [35.28181818, 0.], [35.29090909, 0.], [35.30000000, 0.],
[35.30909091, 0.], [35.31818182, 0.], [35.32727273, 0.], [35.33636364, 0.],
[35.34545455, 0.], [35.35454545, 0.], [35.36363636, 0.], [35.37272727, 0.],
[35.38181818, 0.], [35.39090909, 0.], [35.40000000, 0.], [35.40909091, 0.],
[35.41818182, 0.], [35.42727273, 0.], [35.43636364, 0.], [35.44545455, 0.],
[35.45454545, 0.], [35.46363636, 0.], [35.47272727, 0.], [35.48181818, 0.],
[35.49090909, 0.], [35.50000000, 0.], [35.50909091, 0.], [35.51818182, 0.],
[35.52727273, 0.], [35.53636364, 0.], [35.54545455, 0.], [35.55454545, 0.],
[35.56363636, 0.], [35.57272727, 0.], [35.58181818, 0.], [35.59090909, 0.],
[35.60000000, 0.], [35.60909091, 0.], [35.61818182, 0.], [35.62727273, 0.],
[35.63636364, 0.], [35.64545455, 0.], [35.65454545, 0.], [35.66363636, 0.],
[35.67272727, 0.], [35.68181818, 0.], [35.69090909, 0.], [35.70000000, 0.],
[35.70909091, 0.], [35.71818182, 0.], [35.72727273, 0.], [35.73636364, 0.],
[35.74545455, 0.], [35.75454545, 0.], [35.76363636, 0.], [35.77272727, 0.],
[35.78181818, 0.], [35.79090909, 0.], [35.80000000, 0.], [35.80909091, 0.],
[35.81818182, 0.], [35.82727273, 0.], [35.83636364, 0.], [35.84545455, 0.],

[35.85454545, 0.], [35.86363636, 0.], [35.87272727, 0.], [35.88181818, 0.],
[35.89090909, 0.], [35.90000000, 0.], [35.90909091, 0.], [35.91818182, 0.],
[35.92727273, 0.], [35.93636364, 0.], [35.94545455, 0.], [35.95454545, 0.],
[35.96363636, 0.], [35.97272727, 0.], [35.98181818, 0.], [35.99090909, 0.],
[36.00000000, 0.], [36.00909091, 0.], [36.01818182, 0.], [36.02727273, 0.],
[36.03636364, 0.], [36.04545455, 0.], [36.05454545, 0.], [36.06363636, 0.],
[36.07272727, 0.], [36.08181818, 0.], [36.09090909, 0.], [36.10000000, 0.],
[36.10909091, 0.], [36.11818182, 0.], [36.12727273, 0.], [36.13636364, 0.],
[36.14545455, 0.], [36.15454545, 0.], [36.16363636, 0.], [36.17272727, 0.],
[36.18181818, 0.], [36.19090909, 0.], [36.20000000, 0.], [36.20909091, 0.],
[36.21818182, 0.], [36.22727273, 0.], [36.23636364, 0.], [36.24545455, 0.],
[36.25454545, 0.], [36.26363636, 0.], [36.27272727, 0.], [36.28181818, 0.],
[36.29090909, 0.], [36.30000000, 0.], [36.30909091, 0.], [36.31818182, 0.],
[36.32727273, 0.], [36.33636364, 0.], [36.34545455, 0.], [36.35454545, 0.],
[36.36363636, 0.], [36.37272727, 0.], [36.38181818, 0.], [36.39090909, 0.],
[36.40000000, 0.], [36.40909091, 0.], [36.41818182, 0.], [36.42727273, 0.],
[36.43636364, 0.], [36.44545455, 0.], [36.45454545, 0.], [36.46363636, 0.],
[36.47272727, 0.], [36.48181818, 0.], [36.49090909, 0.], [36.50000000, 0.],
[36.50909091, 0.], [36.51818182, 0.], [36.52727273, 0.], [36.53636364, 0.],
[36.54545455, 0.], [36.55454545, 0.], [36.56363636, 0.], [36.57272727, 0.],
[36.58181818, 0.], [36.59090909, 0.], [36.60000000, 0.], [36.60909091, 0.],
[36.61818182, 0.], [36.62727273, 0.], [36.63636364, 0.], [36.64545455, 0.],
[36.65454545, 0.], [36.66363636, 0.], [36.67272727, 0.], [36.68181818, 0.],
[36.69090909, 0.], [36.70000000, 0.], [36.70909091, 0.], [36.71818182, 0.],
[36.72727273, 0.], [36.73636364, 0.], [36.74545455, 0.], [36.75454545, 0.],
[36.76363636, 0.], [36.77272727, 0.], [36.78181818, 0.], [36.79090909, 0.],
[36.80000000, 0.], [36.80909091, 0.], [36.81818182, 0.], [36.82727273, 0.],
[36.83636364, 0.], [36.84545455, 0.], [36.85454545, 0.], [36.86363636, 0.],
[36.87272727, 0.], [36.88181818, 0.], [36.89090909, 0.], [36.90000000, 0.],
[36.90909091, 0.], [36.91818182, 0.], [36.92727273, 0.], [36.93636364, 0.],
[36.94545455, 0.], [36.95454545, 0.], [36.96363636, 0.], [36.97272727, 0.],
[36.98181818, 0.], [36.99090909, 0.], [37.00000000, 0.], [37.00909091, 0.],
[37.01818182, 0.], [37.02727273, 0.], [37.03636364, 0.], [37.04545455, 0.],
[37.05454545, 0.], [37.06363636, 0.], [37.07272727, 0.], [37.08181818, 0.],
[37.09090909, 0.], [37.10000000, 0.], [37.10909091, 0.], [37.11818182, 0.],
[37.12727273, 0.], [37.13636364, 0.], [37.14545455, 0.], [37.15454545, 0.],

[37.16363636, 0.], [37.17272727, 0.], [37.18181818, 0.], [37.19090909, 0.],
[37.20000000, 0.], [37.20909091, 0.], [37.21818182, 0.], [37.22727273, 0.],
[37.23636364, 0.], [37.24545455, 0.], [37.25454545, 0.], [37.26363636, 0.],
[37.27272727, 0.], [37.28181818, 0.], [37.29090909, 0.], [37.30000000, 0.],
[37.30909091, 0.], [37.31818182, 0.], [37.32727273, 0.], [37.33636364, 0.],
[37.34545455, 0.], [37.35454545, 0.], [37.36363636, 0.], [37.37272727, 0.],
[37.38181818, 0.], [37.39090909, 0.], [37.40000000, 0.], [37.40909091, 0.],
[37.41818182, 0.], [37.42727273, 0.], [37.43636364, 0.], [37.44545455, 0.],
[37.45454545, 0.], [37.46363636, 0.], [37.47272727, 0.], [37.48181818, 0.],
[37.49090909, 0.], [37.50000000, 0.], [37.50909091, 0.], [37.51818182, 0.],
[37.52727273, 0.], [37.53636364, 0.], [37.54545455, 0.], [37.55454545, 0.],
[37.56363636, 0.], [37.57272727, 0.], [37.58181818, 0.], [37.59090909, 0.],
[37.60000000, 0.], [37.60909091, 0.], [37.61818182, 0.], [37.62727273, 0.],
[37.63636364, 0.], [37.64545455, 0.], [37.65454545, 0.], [37.66363636, 0.],
[37.67272727, 0.], [37.68181818, 0.], [37.69090909, 0.], [37.70000000, 0.],
[37.70909091, 0.], [37.71818182, 0.], [37.72727273, 0.], [37.73636364, 0.],
[37.74545455, 0.], [37.75454545, 0.], [37.76363636, 0.], [37.77272727, 0.],
[37.78181818, 0.], [37.79090909, 0.], [37.80000000, 0.], [37.80909091, 0.],
[37.81818182, 0.], [37.82727273, 0.], [37.83636364, 0.], [37.84545455, 0.],
[37.85454545, 0.], [37.86363636, 0.], [37.87272727, 0.], [37.88181818, 0.],
[37.89090909, 0.], [37.90000000, 0.], [37.90909091, 0.], [37.91818182, 0.],
[37.92727273, 0.], [37.93636364, 0.], [37.94545455, 0.], [37.95454545, 0.],
[37.96363636, 0.], [37.97272727, 0.], [37.98181818, 0.], [37.99090909, 0.],
[38.00000000, 0.], [38.00909091, 0.], [38.01818182, 0.], [38.02727273, 0.],
[38.03636364, 0.], [38.04545455, 0.], [38.05454545, 0.], [38.06363636, 0.],
[38.07272727, 0.], [38.08181818, 0.], [38.09090909, 0.], [38.10000000, 0.],
[38.10909091, 0.], [38.11818182, 0.], [38.12727273, 0.], [38.13636364, 0.],
[38.14545455, 0.], [38.15454545, 0.], [38.16363636, 0.], [38.17272727, 0.],
[38.18181818, 0.], [38.19090909, 0.], [38.20000000, 0.], [38.20909091, 0.],
[38.21818182, 0.], [38.22727273, 0.], [38.23636364, 0.], [38.24545455, 0.],
[38.25454545, 0.], [38.26363636, 0.], [38.27272727, 0.], [38.28181818, 0.],
[38.29090909, 0.], [38.30000000, 0.], [38.30909091, 0.], [38.31818182, 0.],
[38.32727273, 0.], [38.33636364, 0.], [38.34545455, 0.], [38.35454545, 0.],
[38.36363636, 0.], [38.37272727, 0.], [38.38181818, 0.], [38.39090909, 0.],
[38.40000000, 0.], [38.40909091, 0.], [38.41818182, 0.], [38.42727273, 0.],
[38.43636364, 0.], [38.44545455, 0.], [38.45454545, 0.], [38.46363636, 0.],

[38.47272727, 0.], [38.48181818, 0.], [38.49090909, 0.], [38.50000000, 0.],
[38.50909091, 0.], [38.51818182, 0.], [38.52727273, 0.], [38.53636364, 0.],
[38.54545455, 0.], [38.55454545, 0.], [38.56363636, 0.], [38.57272727, 0.],
[38.58181818, 0.], [38.59090909, 0.], [38.60000000, 0.], [38.60909091, 0.],
[38.61818182, 0.], [38.62727273, 0.], [38.63636364, 0.], [38.64545455, 0.],
[38.65454545, 0.], [38.66363636, 0.], [38.67272727, 0.], [38.68181818, 0.],
[38.69090909, 0.], [38.70000000, 0.], [38.70909091, 0.], [38.71818182, 0.],
[38.72727273, 0.], [38.73636364, 0.], [38.74545455, 0.], [38.75454545, 0.],
[38.76363636, 0.], [38.77272727, 0.], [38.78181818, 0.], [38.79090909, 0.],
[38.80000000, 0.], [38.80909091, 0.], [38.81818182, 0.], [38.82727273, 0.],
[38.83636364, 0.], [38.84545455, 0.], [38.85454545, 0.], [38.86363636, 0.],
[38.87272727, 0.], [38.88181818, 0.], [38.89090909, 0.], [38.90000000, 0.],
[38.90909091, 0.], [38.91818182, 0.], [38.92727273, 0.], [38.93636364, 0.],
[38.94545455, 0.], [38.95454545, 0.], [38.96363636, 0.], [38.97272727, 0.],
[38.98181818, 0.], [38.99090909, 0.], [39.00000000, 0.], [39.00909091, 0.],
[39.01818182, 0.], [39.02727273, 0.], [39.03636364, 0.], [39.04545455, 0.],
[39.05454545, 0.], [39.06363636, 0.], [39.07272727, 0.], [39.08181818, 0.],
[39.09090909, 0.], [39.10000000, 0.], [39.10909091, 0.], [39.11818182, 0.],
[39.12727273, 0.], [39.13636364, 0.], [39.14545455, 0.], [39.15454545, 0.],
[39.16363636, 0.], [39.17272727, 0.], [39.18181818, 0.], [39.19090909, 0.],
[39.20000000, 0.], [39.20909091, 0.], [39.21818182, 0.], [39.22727273, 0.],
[39.23636364, 0.], [39.24545455, 0.], [39.25454545, 0.], [39.26363636, 0.],
[39.27272727, 0.], [39.28181818, 0.], [39.29090909, 0.], [39.30000000, 0.],
[39.30909091, 0.], [39.31818182, 0.], [39.32727273, 0.], [39.33636364, 0.],
[39.34545455, 0.], [39.35454545, 0.], [39.36363636, 0.], [39.37272727, 0.],
[39.38181818, 0.], [39.39090909, 0.], [39.40000000, 0.], [39.40909091, 0.],
[39.41818182, 0.], [39.42727273, 0.], [39.43636364, 0.], [39.44545455, 0.],
[39.45454545, 0.], [39.46363636, 0.], [39.47272727, 0.], [39.48181818, 0.],
[39.49090909, 0.], [39.50000000, 0.], [39.50909091, 0.], [39.51818182, 0.],
[39.52727273, 0.], [39.53636364, 0.], [39.54545455, 0.], [39.55454545, 0.],
[39.56363636, 0.], [39.57272727, 0.], [39.58181818, 0.], [39.59090909, 0.],
[39.60000000, 0.], [39.60909091, 0.], [39.61818182, 0.], [39.62727273, 0.],
[39.63636364, 0.], [39.64545455, 0.], [39.65454545, 0.], [39.66363636, 0.],
[39.67272727, 0.], [39.68181818, 0.], [39.69090909, 0.], [39.70000000, 0.],
[39.70909091, 0.], [39.71818182, 0.], [39.72727273, 0.], [39.73636364, 0.],
[39.74545455, 0.], [39.75454545, 0.], [39.76363636, 0.], [39.77272727, 0.],

[39.78181818, 0.], [39.79090909, 0.], [39.80000000, 0.], [39.80909091, 0.],
[39.81818182, 0.], [39.82727273, 0.], [39.83636364, 0.], [39.84545455, 0.],
[39.85454545, 0.], [39.86363636, 0.], [39.87272727, 0.], [39.88181818, 0.],
[39.89090909, 0.], [39.90000000, 0.], [39.90909091, 0.], [39.91818182, 0.],
[39.92727273, 0.], [39.93636364, 0.], [39.94545455, 0.], [39.95454545, 0.],
[39.96363636, 0.], [39.97272727, 0.], [39.98181818, 0.], [39.99090909, 0.],
[40.00000000, 0.], [40.00909091, 0.], [40.01818182, 0.], [40.02727273, 0.],
[40.03636364, 0.], [40.04545455, 0.], [40.05454545, 0.], [40.06363636, 0.],
[40.07272727, 0.], [40.08181818, 0.], [40.09090909, 0.], [40.10000000, 0.],
[40.10909091, 0.], [40.11818182, 0.], [40.12727273, 0.], [40.13636364, 0.],
[40.14545455, 0.], [40.15454545, 0.], [40.16363636, 0.], [40.17272727, 0.],
[40.18181818, 0.], [40.19090909, 0.], [40.20000000, 0.], [40.20909091, 0.],
[40.21818182, 0.], [40.22727273, 0.], [40.23636364, 0.], [40.24545455, 0.],
[40.25454545, 0.], [40.26363636, 0.], [40.27272727, 0.], [40.28181818, 0.],
[40.29090909, 0.], [40.30000000, 0.], [40.30909091, 0.], [40.31818182, 0.],
[40.32727273, 0.], [40.33636364, 0.], [40.34545455, 0.], [40.35454545, 0.],
[40.36363636, 0.], [40.37272727, 0.], [40.38181818, 0.], [40.39090909, 0.],
[40.40000000, 0.], [40.40909091, 0.], [40.41818182, 0.], [40.42727273, 0.],
[40.43636364, 0.], [40.44545455, 0.], [40.45454545, 0.], [40.46363636, 0.],
[40.47272727, 0.], [40.48181818, 0.], [40.49090909, 0.], [40.50000000, 0.],
[40.50909091, 0.], [40.51818182, 0.], [40.52727273, 0.], [40.53636364, 0.],
[40.54545455, 0.], [40.55454545, 0.], [40.56363636, 0.], [40.57272727, 0.],
[40.58181818, 0.], [40.59090909, 0.], [40.60000000, 0.], [40.60909091, 0.],
[40.61818182, 0.], [40.62727273, 0.], [40.63636364, 0.], [40.64545455, 0.],
[40.65454545, 0.], [40.66363636, 0.], [40.67272727, 0.], [40.68181818, 0.],
[40.69090909, 0.], [40.70000000, 0.], [40.70909091, 0.], [40.71818182, 0.],
[40.72727273, 0.], [40.73636364, 0.], [40.74545455, 0.], [40.75454545, 0.],
[40.76363636, 0.], [40.77272727, 0.], [40.78181818, 0.], [40.79090909, 0.],
[40.80000000, 0.], [40.80909091, 0.], [40.81818182, 0.], [40.82727273, 0.],
[40.83636364, 0.], [40.84545455, 0.], [40.85454545, 0.], [40.86363636, 0.],
[40.87272727, 0.], [40.88181818, 0.], [40.89090909, 0.], [40.90000000, 0.],
[40.90909091, 0.], [40.91818182, 0.], [40.92727273, 0.], [40.93636364, 0.],
[40.94545455, 0.], [40.95454545, 0.], [40.96363636, 0.], [40.97272727, 0.],
[40.98181818, 0.], [40.99090909, 0.], [41.00000000, 0.], [41.00909091, 0.],
[41.01818182, 0.], [41.02727273, 0.], [41.03636364, 0.], [41.04545455, 0.],
[41.05454545, 0.], [41.06363636, 0.], [41.07272727, 0.], [41.08181818, 0.],

[41.09090909, 0.], [41.10000000, 0.], [41.10909091, 0.], [41.11818182, 0.],
[41.12727273, 0.], [41.13636364, 0.], [41.14545455, 0.], [41.15454545, 0.],
[41.16363636, 0.], [41.17272727, 0.], [41.18181818, 0.], [41.19090909, 0.],
[41.20000000, 0.], [41.20909091, 0.], [41.21818182, 0.], [41.22727273, 0.],
[41.23636364, 0.], [41.24545455, 0.], [41.25454545, 0.], [41.26363636, 0.],
[41.27272727, 0.], [41.28181818, 0.], [41.29090909, 0.], [41.30000000, 0.],
[41.30909091, 0.], [41.31818182, 0.], [41.32727273, 0.], [41.33636364, 0.],
[41.34545455, 0.], [41.35454545, 0.], [41.36363636, 0.], [41.37272727, 0.],
[41.38181818, 0.], [41.39090909, 0.], [41.40000000, 0.], [41.40909091, 0.],
[41.41818182, 0.], [41.42727273, 0.], [41.43636364, 0.], [41.44545455, 0.],
[41.45454545, 0.], [41.46363636, 0.], [41.47272727, 0.], [41.48181818, 0.],
[41.49090909, 0.], [41.50000000, 0.], [41.50909091, 0.], [41.51818182, 0.],
[41.52727273, 0.], [41.53636364, 0.], [41.54545455, 0.], [41.55454545, 0.],
[41.56363636, 0.], [41.57272727, 0.], [41.58181818, 0.], [41.59090909, 0.],
[41.60000000, 0.], [41.60909091, 0.], [41.61818182, 0.], [41.62727273, 0.],
[41.63636364, 0.], [41.64545455, 0.], [41.65454545, 0.], [41.66363636, 0.],
[41.67272727, 0.], [41.68181818, 0.], [41.69090909, 0.], [41.70000000, 0.],
[41.70909091, 0.], [41.71818182, 0.], [41.72727273, 0.], [41.73636364, 0.],
[41.74545455, 0.], [41.75454545, 0.], [41.76363636, 0.], [41.77272727, 0.],
[41.78181818, 0.], [41.79090909, 0.], [41.80000000, 0.], [41.80909091, 0.],
[41.81818182, 0.], [41.82727273, 0.], [41.83636364, 0.], [41.84545455, 0.],
[41.85454545, 0.], [41.86363636, 0.], [41.87272727, 0.], [41.88181818, 0.],
[41.89090909, 0.], [41.90000000, 0.], [41.90909091, 0.], [41.91818182, 0.],
[41.92727273, 0.], [41.93636364, 0.], [41.94545455, 0.], [41.95454545, 0.],
[41.96363636, 0.], [41.97272727, 0.], [41.98181818, 0.], [41.99090909, 0.],
[42.00000000, 0.], [42.00909091, 0.], [42.01818182, 0.], [42.02727273, 0.],
[42.03636364, 0.], [42.04545455, 0.], [42.05454545, 0.], [42.06363636, 0.],
[42.07272727, 0.], [42.08181818, 0.], [42.09090909, 0.], [42.10000000, 0.],
[42.10909091, 0.], [42.11818182, 0.], [42.12727273, 0.], [42.13636364, 0.],
[42.14545455, 0.], [42.15454545, 0.], [42.16363636, 0.], [42.17272727, 0.],
[42.18181818, 0.], [42.19090909, 0.], [42.20000000, 0.], [42.20909091, 0.],
[42.21818182, 0.], [42.22727273, 0.], [42.23636364, 0.], [42.24545455, 0.],
[42.25454545, 0.], [42.26363636, 0.], [42.27272727, 0.], [42.28181818, 0.],
[42.29090909, 0.], [42.30000000, 0.], [42.30909091, 0.], [42.31818182, 0.],
[42.32727273, 0.], [42.33636364, 0.], [42.34545455, 0.], [42.35454545, 0.],
[42.36363636, 0.], [42.37272727, 0.], [42.38181818, 0.], [42.39090909, 0.],

[42.40000000, 0.], [42.40909091, 0.], [42.41818182, 0.], [42.42727273, 0.],
[42.43636364, 0.], [42.44545455, 0.], [42.45454545, 0.], [42.46363636, 0.],
[42.47272727, 0.], [42.48181818, 0.], [42.49090909, 0.], [42.50000000, 0.],
[42.50909091, 0.], [42.51818182, 0.], [42.52727273, 0.], [42.53636364, 0.],
[42.54545455, 0.], [42.55454545, 0.], [42.56363636, 0.], [42.57272727, 0.],
[42.58181818, 0.], [42.59090909, 0.], [42.60000000, 0.], [42.60909091, 0.],
[42.61818182, 0.], [42.62727273, 0.], [42.63636364, 0.], [42.64545455, 0.],
[42.65454545, 0.], [42.66363636, 0.], [42.67272727, 0.], [42.68181818, 0.],
[42.69090909, 0.], [42.70000000, 0.], [42.70909091, 0.], [42.71818182, 0.],
[42.72727273, 0.], [42.73636364, 0.], [42.74545455, 0.], [42.75454545, 0.],
[42.76363636, 0.], [42.77272727, 0.], [42.78181818, 0.], [42.79090909, 0.],
[42.80000000, 0.], [42.80909091, 0.], [42.81818182, 0.], [42.82727273, 0.],
[42.83636364, 0.], [42.84545455, 0.], [42.85454545, 0.], [42.86363636, 0.],
[42.87272727, 0.], [42.88181818, 0.], [42.89090909, 0.], [42.90000000, 0.],
[42.90909091, 0.], [42.91818182, 0.], [42.92727273, 0.], [42.93636364, 0.],
[42.94545455, 0.], [42.95454545, 0.], [42.96363636, 0.], [42.97272727, 0.],
[42.98181818, 0.], [42.99090909, 0.], [43.00000000, 0.], [43.00909091, 0.],
[43.01818182, 0.], [43.02727273, 0.], [43.03636364, 0.], [43.04545455, 0.],
[43.05454545, 0.], [43.06363636, 0.], [43.07272727, 0.], [43.08181818, 0.],
[43.09090909, 0.], [43.10000000, 0.], [43.10909091, 0.], [43.11818182, 0.],
[43.12727273, 0.], [43.13636364, 0.], [43.14545455, 0.], [43.15454545, 0.],
[43.16363636, 0.], [43.17272727, 0.], [43.18181818, 0.], [43.19090909, 0.],
[43.20000000, 0.], [43.20909091, 0.], [43.21818182, 0.], [43.22727273, 0.],
[43.23636364, 0.], [43.24545455, 0.], [43.25454545, 0.], [43.26363636, 0.],
[43.27272727, 0.], [43.28181818, 0.], [43.29090909, 0.], [43.30000000, 0.],
[43.30909091, 0.], [43.31818182, 0.], [43.32727273, 0.], [43.33636364, 0.],
[43.34545455, 0.], [43.35454545, 0.], [43.36363636, 0.], [43.37272727, 0.],
[43.38181818, 0.], [43.39090909, 0.], [43.40000000, 0.], [43.40909091, 0.],
[43.41818182, 0.], [43.42727273, 0.], [43.43636364, 0.], [43.44545455, 0.],
[43.45454545, 0.], [43.46363636, 0.], [43.47272727, 0.], [43.48181818, 0.],
[43.49090909, 0.], [43.50000000, 0.], [43.50909091, 0.], [43.51818182, 0.],
[43.52727273, 0.], [43.53636364, 0.], [43.54545455, 0.], [43.55454545, 0.],
[43.56363636, 0.], [43.57272727, 0.], [43.58181818, 0.], [43.59090909, 0.],
[43.60000000, 0.], [43.60909091, 0.], [43.61818182, 0.], [43.62727273, 0.],
[43.63636364, 0.], [43.64545455, 0.], [43.65454545, 0.], [43.66363636, 0.],
[43.67272727, 0.], [43.68181818, 0.], [43.69090909, 0.], [43.70000000, 0.],

[43.70909091, 0.], [43.71818182, 0.], [43.72727273, 0.], [43.73636364, 0.],
[43.74545455, 0.], [43.75454545, 0.], [43.76363636, 0.], [43.77272727, 0.],
[43.78181818, 0.], [43.79090909, 0.], [43.80000000, 0.], [43.80909091, 0.],
[43.81818182, 0.], [43.82727273, 0.], [43.83636364, 0.], [43.84545455, 0.],
[43.85454545, 0.], [43.86363636, 0.], [43.87272727, 0.], [43.88181818, 0.],
[43.89090909, 0.], [43.90000000, 0.], [43.90909091, 0.], [43.91818182, 0.],
[43.92727273, 0.], [43.93636364, 0.], [43.94545455, 0.], [43.95454545, 0.],
[43.96363636, 0.], [43.97272727, 0.], [43.98181818, 0.], [43.99090909, 0.],
[44.00000000, 0.], [44.00909091, 0.], [44.01818182, 0.], [44.02727273, 0.],
[44.03636364, 0.], [44.04545455, 0.], [44.05454545, 0.], [44.06363636, 0.],
[44.07272727, 0.], [44.08181818, 0.], [44.09090909, 0.], [44.10000000, 0.],
[44.10909091, 0.], [44.11818182, 0.], [44.12727273, 0.], [44.13636364, 0.],
[44.14545455, 0.], [44.15454545, 0.], [44.16363636, 0.], [44.17272727, 0.],
[44.18181818, 0.], [44.19090909, 0.], [44.20000000, 0.], [44.20909091, 0.],
[44.21818182, 0.], [44.22727273, 0.], [44.23636364, 0.], [44.24545455, 0.],
[44.25454545, 0.], [44.26363636, 0.], [44.27272727, 0.], [44.28181818, 0.],
[44.29090909, 0.], [44.30000000, 0.], [44.30909091, 0.], [44.31818182, 0.],
[44.32727273, 0.], [44.33636364, 0.], [44.34545455, 0.], [44.35454545, 0.],
[44.36363636, 0.], [44.37272727, 0.], [44.38181818, 0.], [44.39090909, 0.],
[44.40000000, 0.], [44.40909091, 0.], [44.41818182, 0.], [44.42727273, 0.],
[44.43636364, 0.], [44.44545455, 0.], [44.45454545, 0.], [44.46363636, 0.],
[44.47272727, 0.], [44.48181818, 0.], [44.49090909, 0.], [44.50000000, 0.],
[44.50909091, 0.], [44.51818182, 0.], [44.52727273, 0.], [44.53636364, 0.],
[44.54545455, 0.], [44.55454545, 0.], [44.56363636, 0.], [44.57272727, 0.],
[44.58181818, 0.], [44.59090909, 0.], [44.60000000, 0.], [44.60909091, 0.],
[44.61818182, 0.], [44.62727273, 0.], [44.63636364, 0.], [44.64545455, 0.],
[44.65454545, 0.], [44.66363636, 0.], [44.67272727, 0.], [44.68181818, 0.],
[44.69090909, 0.], [44.70000000, 0.], [44.70909091, 0.], [44.71818182, 0.],
[44.72727273, 0.], [44.73636364, 0.], [44.74545455, 0.], [44.75454545, 0.],
[44.76363636, 0.], [44.77272727, 0.], [44.78181818, 0.], [44.79090909, 0.],
[44.80000000, 0.], [44.80909091, 0.], [44.81818182, 0.], [44.82727273, 0.],
[44.83636364, 0.], [44.84545455, 0.], [44.85454545, 0.], [44.86363636, 0.],
[44.87272727, 0.], [44.88181818, 0.], [44.89090909, 0.], [44.90000000, 0.],
[44.90909091, 0.], [44.91818182, 0.], [44.92727273, 0.], [44.93636364, 0.],
[44.94545455, 0.], [44.95454545, 0.], [44.96363636, 0.], [44.97272727, 0.],
[44.98181818, 0.], [44.99090909, 0.], [45.00000000, 0.], [45.00909091, 0.],

[45.01818182, 0.], [45.02727273, 0.], [45.03636364, 0.], [45.04545455, 0.],
[45.05454545, 0.], [45.06363636, 0.], [45.07272727, 0.], [45.08181818, 0.],
[45.09090909, 0.], [45.10000000, 0.], [45.10909091, 0.], [45.11818182, 0.],
[45.12727273, 0.], [45.13636364, 0.], [45.14545455, 0.], [45.15454545, 0.],
[45.16363636, 0.], [45.17272727, 0.], [45.18181818, 0.], [45.19090909, 0.],
[45.20000000, 0.], [45.20909091, 0.], [45.21818182, 0.], [45.22727273, 0.],
[45.23636364, 0.], [45.24545455, 0.], [45.25454545, 0.], [45.26363636, 0.],
[45.27272727, 0.], [45.28181818, 0.], [45.29090909, 0.], [45.30000000, 0.],
[45.30909091, 0.], [45.31818182, 0.], [45.32727273, 0.], [45.33636364, 0.],
[45.34545455, 0.], [45.35454545, 0.], [45.36363636, 0.], [45.37272727, 0.],
[45.38181818, 0.], [45.39090909, 0.], [45.40000000, 0.], [45.40909091, 0.],
[45.41818182, 0.], [45.42727273, 0.], [45.43636364, 0.], [45.44545455, 0.],
[45.45454545, 0.], [45.46363636, 0.], [45.47272727, 0.], [45.48181818, 0.],
[45.49090909, 0.], [45.50000000, 0.], [45.50909091, 0.], [45.51818182, 0.],
[45.52727273, 0.], [45.53636364, 0.], [45.54545455, 0.], [45.55454545, 0.],
[45.56363636, 0.], [45.57272727, 0.], [45.58181818, 0.], [45.59090909, 0.],
[45.60000000, 0.], [45.60909091, 0.], [45.61818182, 0.], [45.62727273, 0.],
[45.63636364, 0.], [45.64545455, 0.], [45.65454545, 0.], [45.66363636, 0.],
[45.67272727, 0.], [45.68181818, 0.], [45.69090909, 0.], [45.70000000, 0.],
[45.70909091, 0.], [45.71818182, 0.], [45.72727273, 0.], [45.73636364, 0.],
[45.74545455, 0.], [45.75454545, 0.], [45.76363636, 0.], [45.77272727, 0.],
[45.78181818, 0.], [45.79090909, 0.], [45.80000000, 0.], [45.80909091, 0.],
[45.81818182, 0.], [45.82727273, 0.], [45.83636364, 0.], [45.84545455, 0.],
[45.85454545, 0.], [45.86363636, 0.], [45.87272727, 0.], [45.88181818, 0.],
[45.89090909, 0.], [45.90000000, 0.], [45.90909091, 0.], [45.91818182, 0.],
[45.92727273, 0.], [45.93636364, 0.], [45.94545455, 0.], [45.95454545, 0.],
[45.96363636, 0.], [45.97272727, 0.], [45.98181818, 0.], [45.99090909, 0.],
[46.00000000, 0.], [46.00909091, 0.], [46.01818182, 0.], [46.02727273, 0.],
[46.03636364, 0.], [46.04545455, 0.], [46.05454545, 0.], [46.06363636, 0.],
[46.07272727, 0.], [46.08181818, 0.], [46.09090909, 0.], [46.10000000, 0.],
[46.10909091, 0.], [46.11818182, 0.], [46.12727273, 0.], [46.13636364, 0.],
[46.14545455, 0.], [46.15454545, 0.], [46.16363636, 0.], [46.17272727, 0.],
[46.18181818, 0.], [46.19090909, 0.], [46.20000000, 0.], [46.20909091, 0.],
[46.21818182, 0.], [46.22727273, 0.], [46.23636364, 0.], [46.24545455, 0.],
[46.25454545, 0.], [46.26363636, 0.], [46.27272727, 0.], [46.28181818, 0.],
[46.29090909, 0.], [46.30000000, 0.], [46.30909091, 0.], [46.31818182, 0.],

[46.32727273, 0.], [46.33636364, 0.], [46.34545455, 0.], [46.35454545, 0.],
[46.36363636, 0.], [46.37272727, 0.], [46.38181818, 0.], [46.39090909, 0.],
[46.40000000, 0.], [46.40909091, 0.], [46.41818182, 0.], [46.42727273, 0.],
[46.43636364, 0.], [46.44545455, 0.], [46.45454545, 0.], [46.46363636, 0.],
[46.47272727, 0.], [46.48181818, 0.], [46.49090909, 0.], [46.50000000, 0.],
[46.50909091, 0.], [46.51818182, 0.], [46.52727273, 0.], [46.53636364, 0.],
[46.54545455, 0.], [46.55454545, 0.], [46.56363636, 0.], [46.57272727, 0.],
[46.58181818, 0.], [46.59090909, 0.], [46.60000000, 0.], [46.60909091, 0.],
[46.61818182, 0.], [46.62727273, 0.], [46.63636364, 0.], [46.64545455, 0.],
[46.65454545, 0.], [46.66363636, 0.], [46.67272727, 0.], [46.68181818, 0.],
[46.69090909, 0.], [46.70000000, 0.], [46.70909091, 0.], [46.71818182, 0.],
[46.72727273, 0.], [46.73636364, 0.], [46.74545455, 0.], [46.75454545, 0.],
[46.76363636, 0.], [46.77272727, 0.], [46.78181818, 0.], [46.79090909, 0.],
[46.80000000, 0.], [46.80909091, 0.], [46.81818182, 0.], [46.82727273, 0.],
[46.83636364, 0.], [46.84545455, 0.], [46.85454545, 0.], [46.86363636, 0.],
[46.87272727, 0.], [46.88181818, 0.], [46.89090909, 0.], [46.90000000, 0.],
[46.90909091, 0.], [46.91818182, 0.], [46.92727273, 0.], [46.93636364, 0.],
[46.94545455, 0.], [46.95454545, 0.], [46.96363636, 0.], [46.97272727, 0.],
[46.98181818, 0.], [46.99090909, 0.], [47.00000000, 0.], [47.00909091, 0.],
[47.01818182, 0.], [47.02727273, 0.], [47.03636364, 0.], [47.04545455, 0.],
[47.05454545, 0.], [47.06363636, 0.], [47.07272727, 0.], [47.08181818, 0.],
[47.09090909, 0.], [47.10000000, 0.], [47.10909091, 0.], [47.11818182, 0.],
[47.12727273, 0.], [47.13636364, 0.], [47.14545455, 0.], [47.15454545, 0.],
[47.16363636, 0.], [47.17272727, 0.], [47.18181818, 0.], [47.19090909, 0.],
[47.20000000, 0.], [47.20909091, 0.], [47.21818182, 0.], [47.22727273, 0.],
[47.23636364, 0.], [47.24545455, 0.], [47.25454545, 0.], [47.26363636, 0.],
[47.27272727, 0.], [47.28181818, 0.], [47.29090909, 0.], [47.30000000, 0.],
[47.30909091, 0.], [47.31818182, 0.], [47.32727273, 0.], [47.33636364, 0.],
[47.34545455, 0.], [47.35454545, 0.], [47.36363636, 0.], [47.37272727, 0.],
[47.38181818, 0.], [47.39090909, 0.], [47.40000000, 0.], [47.40909091, 0.],
[47.41818182, 0.], [47.42727273, 0.], [47.43636364, 0.], [47.44545455, 0.],
[47.45454545, 0.], [47.46363636, 0.], [47.47272727, 0.], [47.48181818, 0.],
[47.49090909, 0.], [47.50000000, 0.], [47.50909091, 0.], [47.51818182, 0.],
[47.52727273, 0.], [47.53636364, 0.], [47.54545455, 0.], [47.55454545, 0.],
[47.56363636, 0.], [47.57272727, 0.], [47.58181818, 0.], [47.59090909, 0.],
[47.60000000, 0.], [47.60909091, 0.], [47.61818182, 0.], [47.62727273, 0.],

[47.63636364, 0.], [47.64545455, 0.], [47.65454545, 0.], [47.66363636, 0.],
[47.67272727, 0.], [47.68181818, 0.], [47.69090909, 0.], [47.70000000, 0.],
[47.70909091, 0.], [47.71818182, 0.], [47.72727273, 0.], [47.73636364, 0.],
[47.74545455, 0.], [47.75454545, 0.], [47.76363636, 0.], [47.77272727, 0.],
[47.78181818, 0.], [47.79090909, 0.], [47.80000000, 0.], [47.80909091, 0.],
[47.81818182, 0.], [47.82727273, 0.], [47.83636364, 0.], [47.84545455, 0.],
[47.85454545, 0.], [47.86363636, 0.], [47.87272727, 0.], [47.88181818, 0.],
[47.89090909, 0.], [47.90000000, 0.], [47.90909091, 0.], [47.91818182, 0.],
[47.92727273, 0.], [47.93636364, 0.], [47.94545455, 0.], [47.95454545, 0.],
[47.96363636, 0.], [47.97272727, 0.], [47.98181818, 0.], [47.99090909, 0.],
[48.00000000, 0.], [48.00909091, 0.], [48.01818182, 0.], [48.02727273, 0.],
[48.03636364, 0.], [48.04545455, 0.], [48.05454545, 0.], [48.06363636, 0.],
[48.07272727, 0.], [48.08181818, 0.], [48.09090909, 0.], [48.10000000, 0.],
[48.10909091, 0.], [48.11818182, 0.], [48.12727273, 0.], [48.13636364, 0.],
[48.14545455, 0.], [48.15454545, 0.], [48.16363636, 0.], [48.17272727, 0.],
[48.18181818, 0.], [48.19090909, 0.], [48.20000000, 0.], [48.20909091, 0.],
[48.21818182, 0.], [48.22727273, 0.], [48.23636364, 0.], [48.24545455, 0.],
[48.25454545, 0.], [48.26363636, 0.], [48.27272727, 0.], [48.28181818, 0.],
[48.29090909, 0.], [48.30000000, 0.], [48.30909091, 0.], [48.31818182, 0.],
[48.32727273, 0.], [48.33636364, 0.], [48.34545455, 0.], [48.35454545, 0.],
[48.36363636, 0.], [48.37272727, 0.], [48.38181818, 0.], [48.39090909, 0.],
[48.40000000, 0.], [48.40909091, 0.], [48.41818182, 0.], [48.42727273, 0.],
[48.43636364, 0.], [48.44545455, 0.], [48.45454545, 0.], [48.46363636, 0.],
[48.47272727, 0.], [48.48181818, 0.], [48.49090909, 0.], [48.50000000, 0.],
[48.50909091, 0.], [48.51818182, 0.], [48.52727273, 0.], [48.53636364, 0.],
[48.54545455, 0.], [48.55454545, 0.], [48.56363636, 0.], [48.57272727, 0.],
[48.58181818, 0.], [48.59090909, 0.], [48.60000000, 0.], [48.60909091, 0.],
[48.61818182, 0.], [48.62727273, 0.], [48.63636364, 0.], [48.64545455, 0.],
[48.65454545, 0.], [48.66363636, 0.], [48.67272727, 0.], [48.68181818, 0.],
[48.69090909, 0.], [48.70000000, 0.], [48.70909091, 0.], [48.71818182, 0.],
[48.72727273, 0.], [48.73636364, 0.], [48.74545455, 0.], [48.75454545, 0.],
[48.76363636, 0.], [48.77272727, 0.], [48.78181818, 0.], [48.79090909, 0.],
[48.80000000, 0.], [48.80909091, 0.], [48.81818182, 0.], [48.82727273, 0.],
[48.83636364, 0.], [48.84545455, 0.], [48.85454545, 0.], [48.86363636, 0.],
[48.87272727, 0.], [48.88181818, 0.], [48.89090909, 0.], [48.90000000, 0.],
[48.90909091, 0.], [48.91818182, 0.], [48.92727273, 0.], [48.93636364, 0.],

```

[48.94545455, 0.], [48.95454545, 0.], [48.96363636, 0.], [48.97272727, 0.],
[48.98181818, 0.], [48.99090909, 0.], [49.00000000, 0.], [49.00909091, 0.],
[49.01818182, 0.], [49.02727273, 0.], [49.03636364, 0.], [49.04545455, 0.],
[49.05454545, 0.], [49.06363636, 0.], [49.07272727, 0.], [49.08181818, 0.],
[49.09090909, 0.], [49.10000000, 0.], [49.10909091, 0.], [49.11818182, 0.],
[49.12727273, 0.], [49.13636364, 0.], [49.14545455, 0.], [49.15454545, 0.],
[49.16363636, 0.], [49.17272727, 0.], [49.18181818, 0.], [49.19090909, 0.],
[49.20000000, 0.], [49.20909091, 0.], [49.21818182, 0.], [49.22727273, 0.],
[49.23636364, 0.], [49.24545455, 0.], [49.25454545, 0.], [49.26363636, 0.],
[49.27272727, 0.], [49.28181818, 0.], [49.29090909, 0.], [49.30000000, 0.],
[49.30909091, 0.], [49.31818182, 0.], [49.32727273, 0.], [49.33636364, 0.],
[49.34545455, 0.], [49.35454545, 0.], [49.36363636, 0.], [49.37272727, 0.],
[49.38181818, 0.], [49.39090909, 0.], [49.40000000, 0.], [49.40909091, 0.],
[49.41818182, 0.], [49.42727273, 0.], [49.43636364, 0.], [49.44545455, 0.],
[49.45454545, 0.], [49.46363636, 0.], [49.47272727, 0.], [49.48181818, 0.],
[49.49090909, 0.], [49.50000000, 0.], [49.50909091, 0.], [49.51818182, 0.],
[49.52727273, 0.], [49.53636364, 0.], [49.54545455, 0.], [49.55454545, 0.],
[49.56363636, 0.], [49.57272727, 0.], [49.58181818, 0.], [49.59090909, 0.],
[49.60000000, 0.], [49.60909091, 0.], [49.61818182, 0.], [49.62727273, 0.],
[49.63636364, 0.], [49.64545455, 0.], [49.65454545, 0.], [49.66363636, 0.],
[49.67272727, 0.], [49.68181818, 0.], [49.69090909, 0.], [49.70000000, 0.],
[49.70909091, 0.], [49.71818182, 0.], [49.72727273, 0.], [49.73636364, 0.],
[49.74545455, 0.], [49.75454545, 0.], [49.76363636, 0.], [49.77272727, 0.],
[49.78181818, 0.], [49.79090909, 0.], [49.80000000, 0.], [49.80909091, 0.],
[49.81818182, 0.], [49.82727273, 0.], [49.83636364, 0.], [49.84545455, 0.],
[49.85454545, 0.], [49.86363636, 0.], [49.87272727, 0.], [49.88181818, 0.],
[49.89090909, 0.], [49.90000000, 0.], [49.90909091, 0.], [49.91818182, 0.],
[49.92727273, 0.], [49.93636364, 0.], [49.94545455, 0.], [49.95454545, 0.],
[49.96363636, 0.], [49.97272727, 0.], [49.98181818, 0.], [49.99090909, 0.],
[50.00000000, 0.]]
```

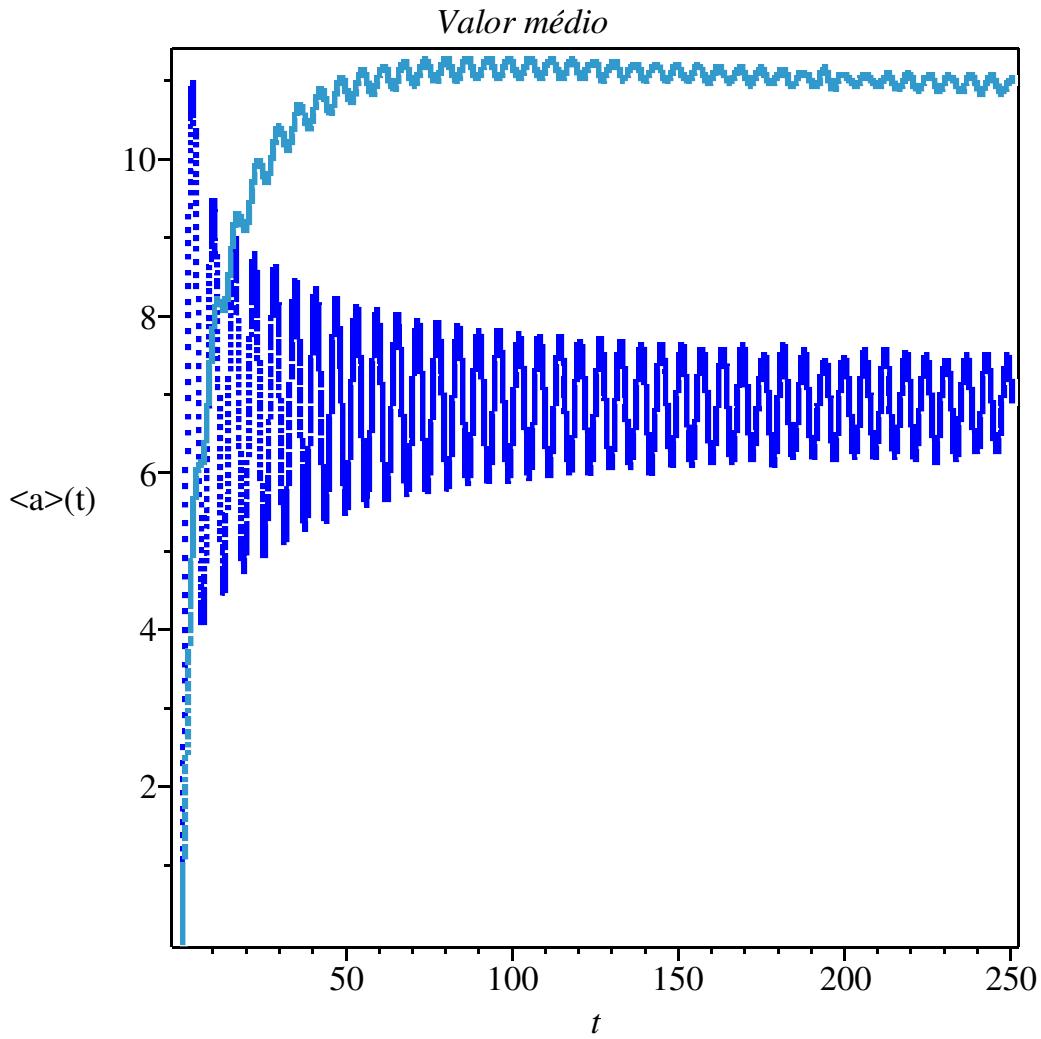
```

> aux1:=readdata(`amedioE25alpha05.dat`,2):
> aux2:=readdata(`amedioE145alpha04.dat`,2):
> aux3:=readdata(`pacoteE125alpha04.dat`,2):
> aux4:=readdata(`pacoteE135alpha04.dat`,2):
> w1:=pointplot(aux1,style=point,axes=box,symbol=point,color=
blue,labels=[t,"<a>(t)"]):
```

```

> macro(skyblue = COLOR(RGB, .1960, .6000, .8000)) :
> macro(palegreen=RGB(.5607, .7372, .5607)) :
> w2:=pointplot(aux2,style=point,axes=box,symbol=point,color=
  skyblue,labels=[t,"<a>(t)"],title=`Valor médio`):
> display([w1,w2]);

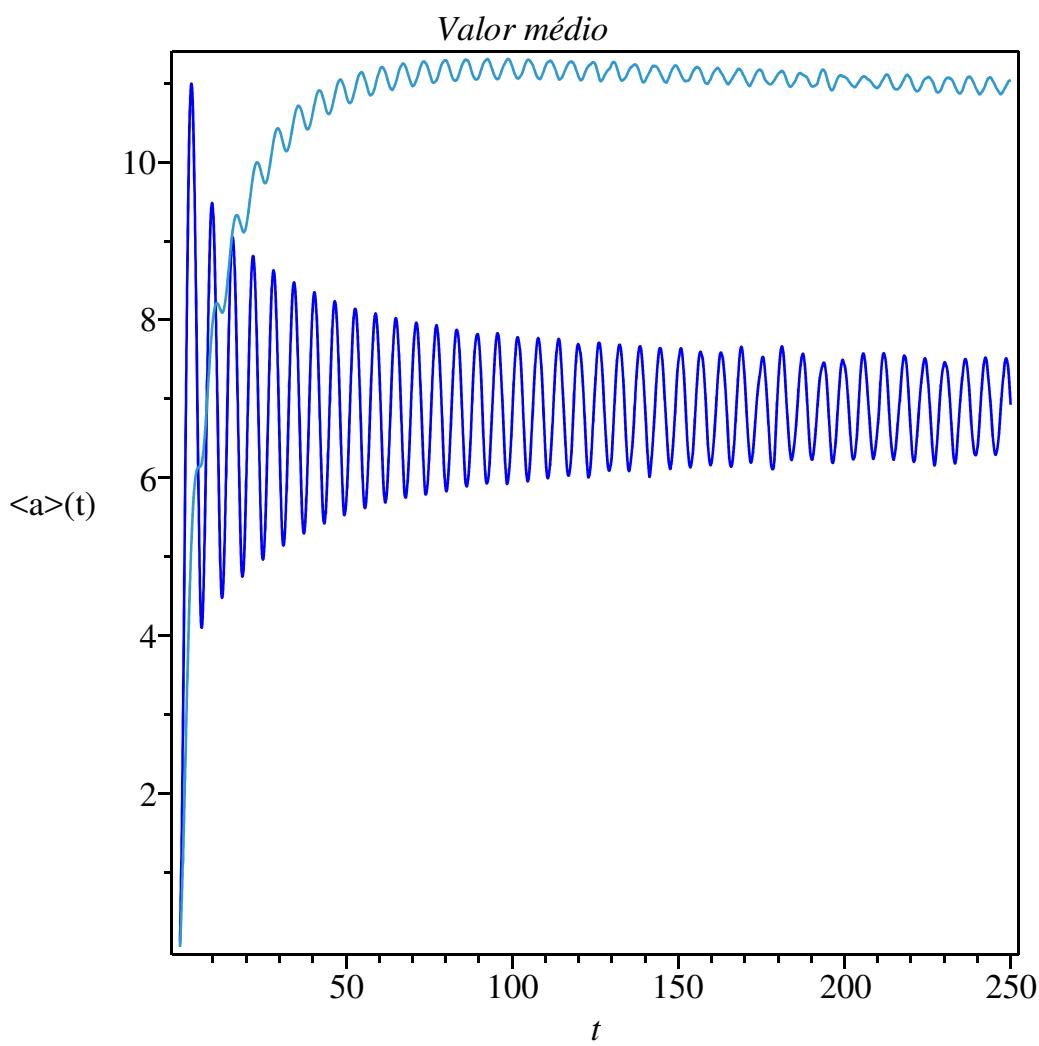
```



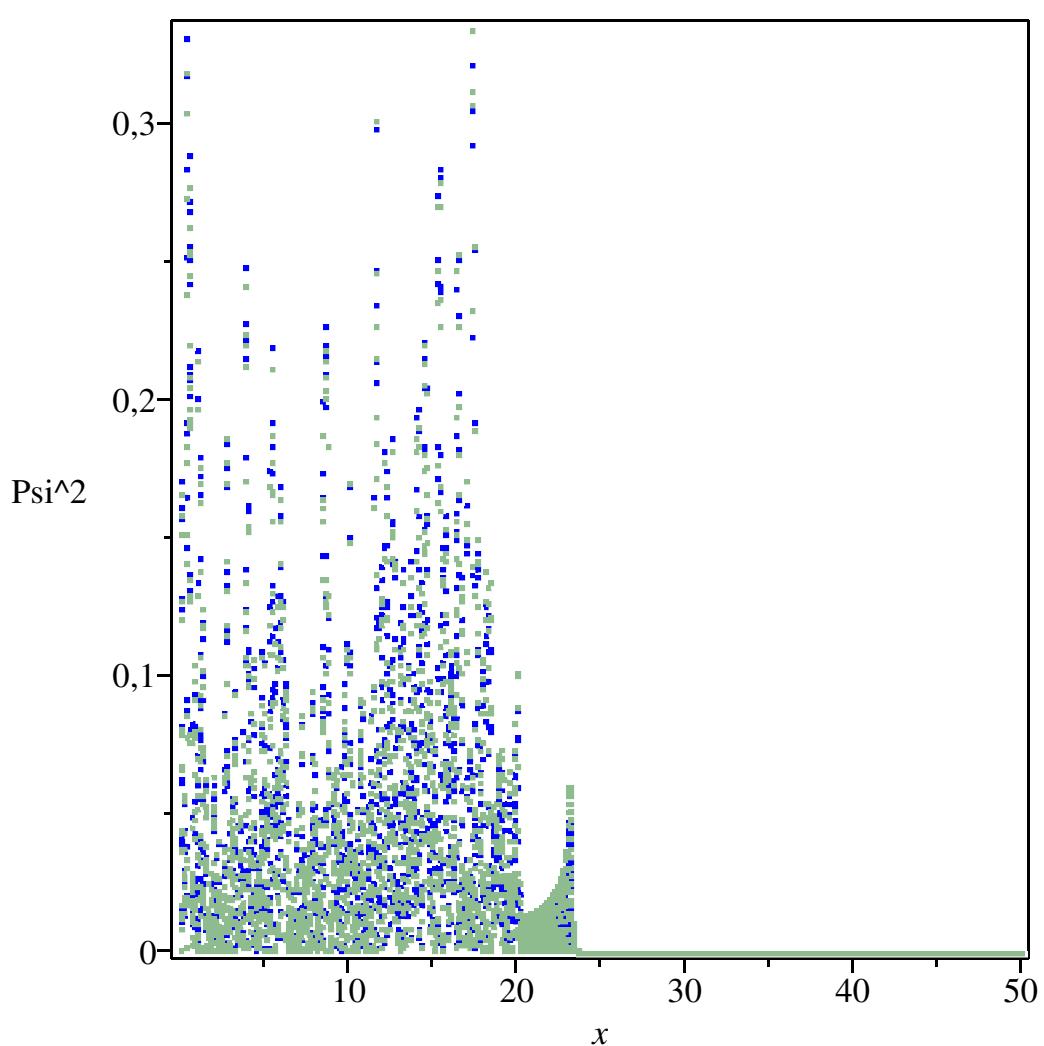
```

> w1b:=pointplot(aux1,style=line,axes=box,symbol=point,color=
  blue,labels=[t,"<a>(t)"]):
> w2b:=pointplot(aux2,style=line,axes=box,symbol=point,color=
  skyblue,labels=[t,"<a>(t)"],title=`Valor médio`):
> display([w1b,w2b]);

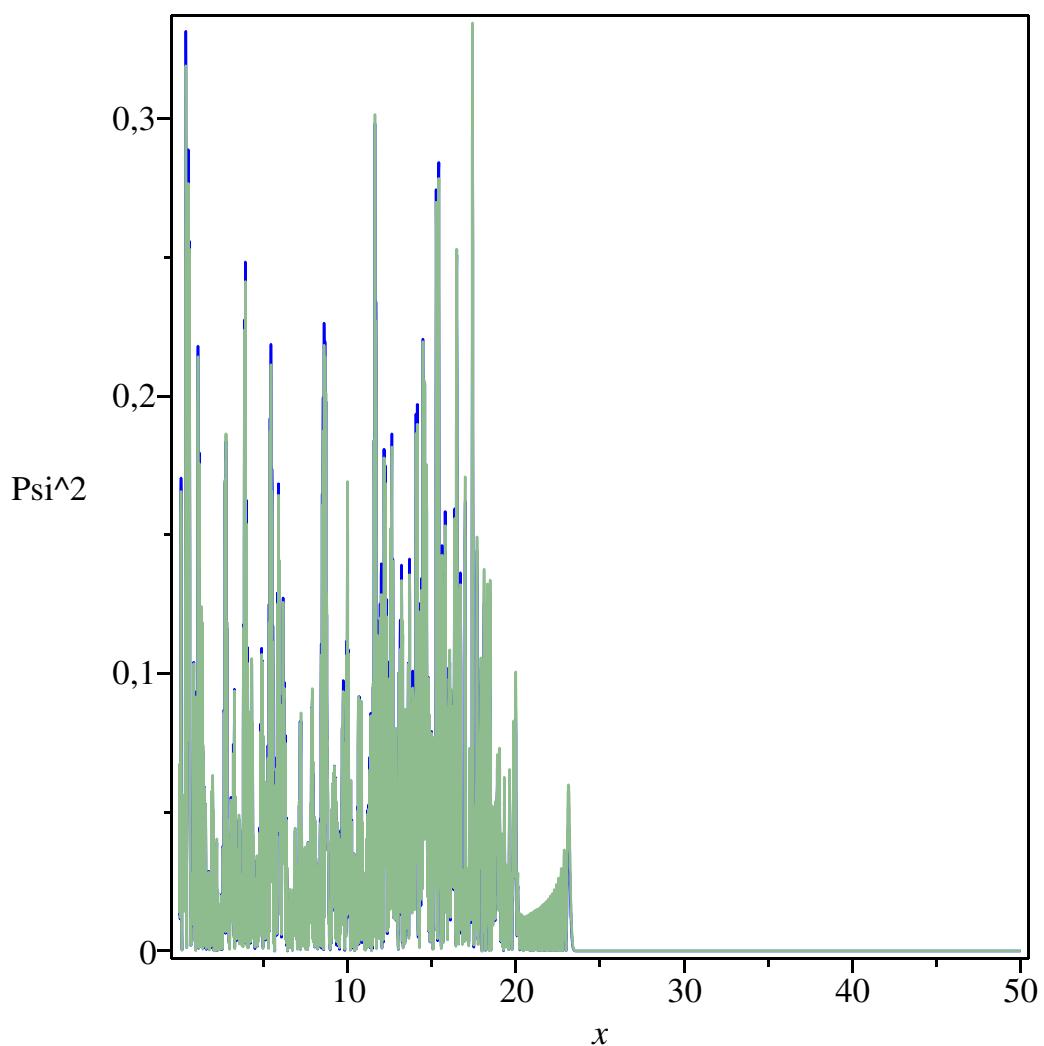
```



```
> w3:=pointplot(aux3,style=point,axes=box,symbol=point,color=blue,labels=[x,"Psi^2"]):
> w4:=pointplot(aux4,style=point,axes=box,symbol=point,color=palegreen,labels=[x,"Psi^2"]):
> display([w3,w4]);
```



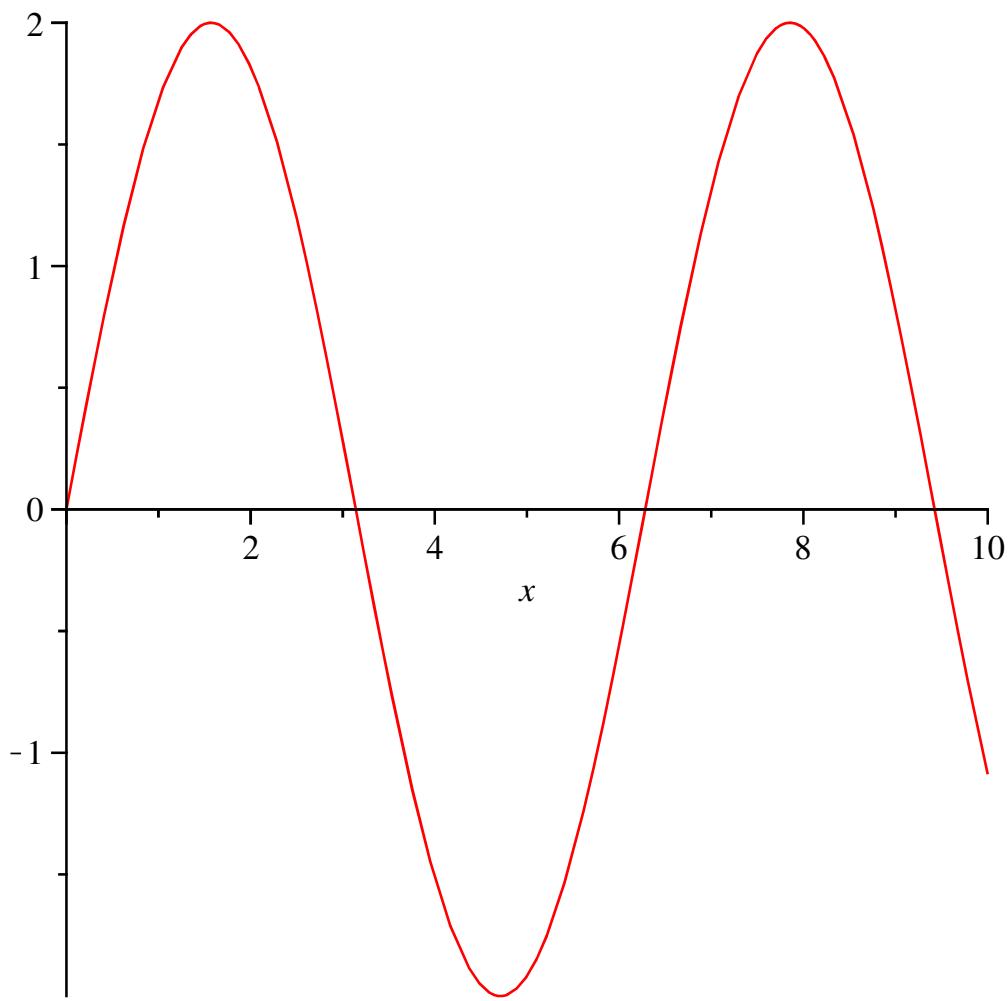
```
> w3b:=pointplot(aux3,style=line,axes=box,symbol=point,color=blue,labels=[x,"Psi^2"]):
> w4b:=pointplot(aux4,style=line,axes=box,symbol=point,color=palegreen,labels=[x,"Psi^2"]):
> display([w3b,w4b]);
```



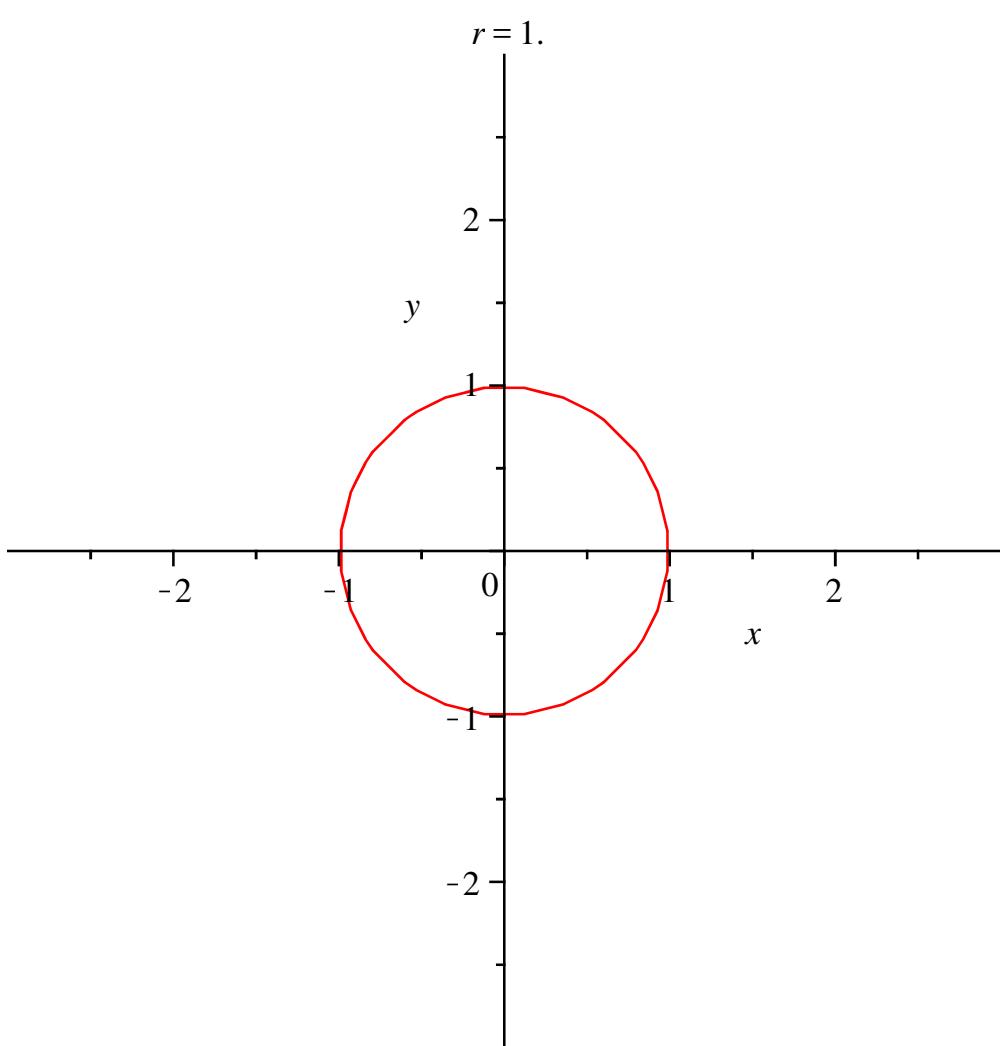
4.2. Animações

```
> ?animated  
> animate( plot, [A*sin(x), x=0..10], A=0..2 );
```

$$A = 2.0000$$



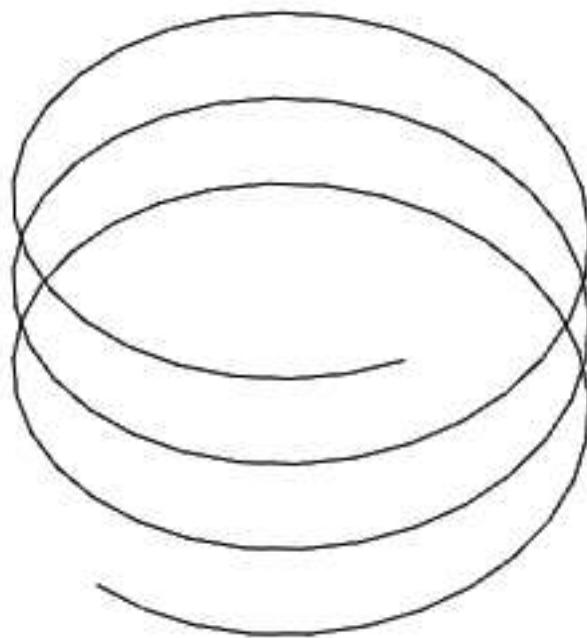
```
> animate(implicitplot, [x^2+y^2 = r^2, x = -3 .. 3, y = -3 .. 3], r = 1 .. 3, scaling = constrained);
```



Usando o comando "thickness" você pode definir a espessura da linha.

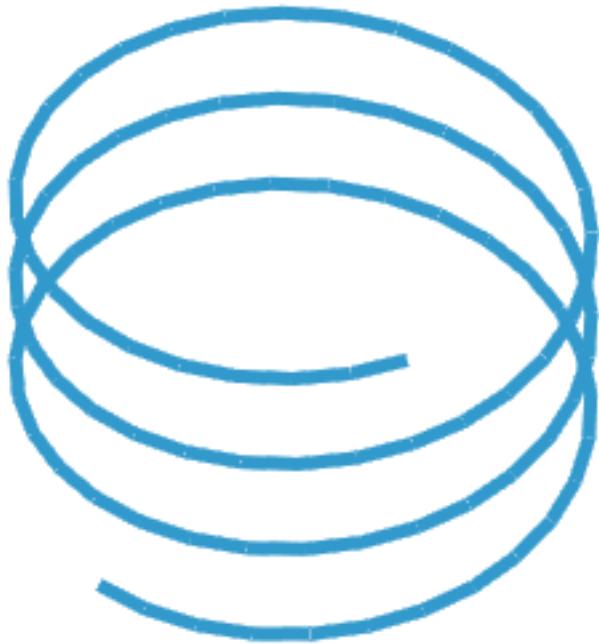
```
> opts := thickness = 1, numpoints = 100, color = black:  
> opts2 := thickness =5, numpoints = 100, color = skyblue:  
> animate(spacecurve, [[cos(t), sin(t), (2+sin(A))*t], t = 0 ..  
20, opts], A = 0 .. 2*Pi);
```

$$A = 0.$$

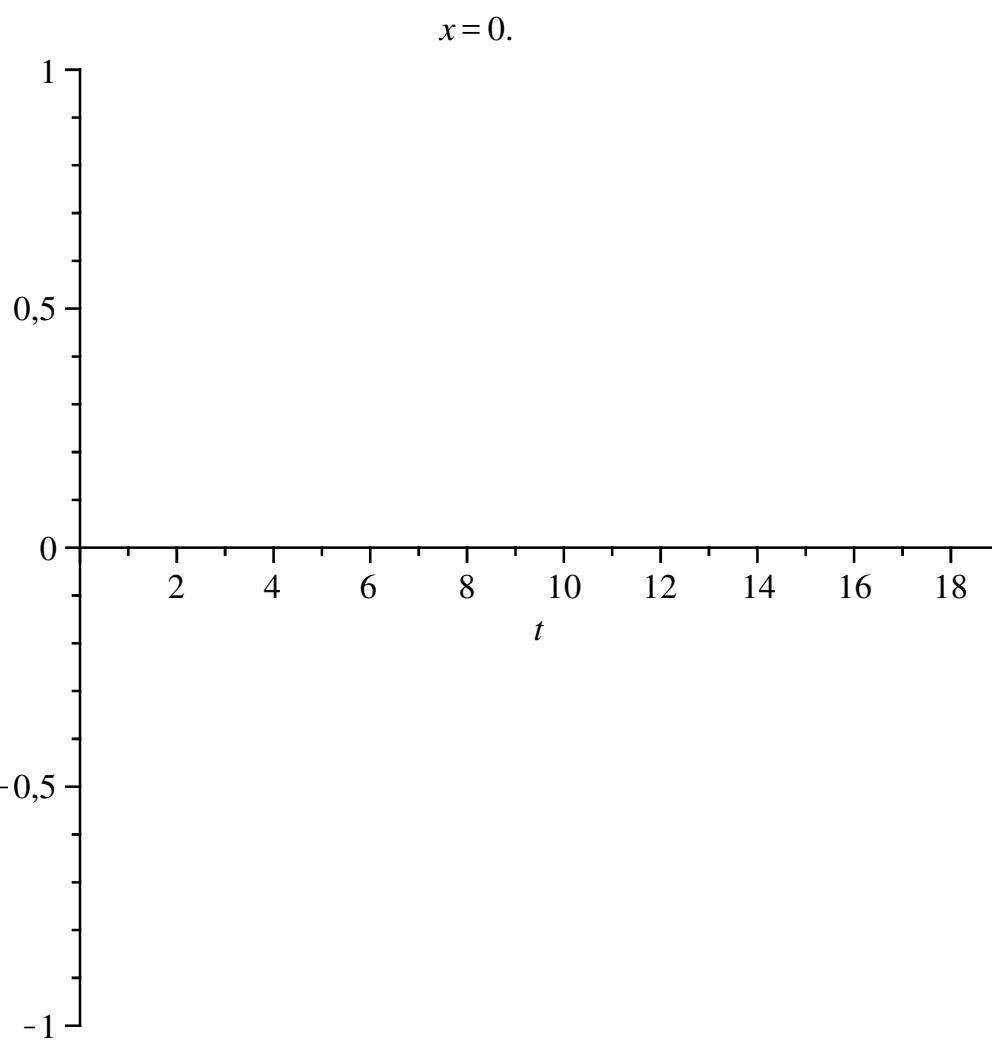


```
> animate(spacecurve, [[cos(t), sin(t), (2+sin(A))*t], t = 0 .. 20, opts2], A = 0 .. 2*Pi);
```

$A = 0.$

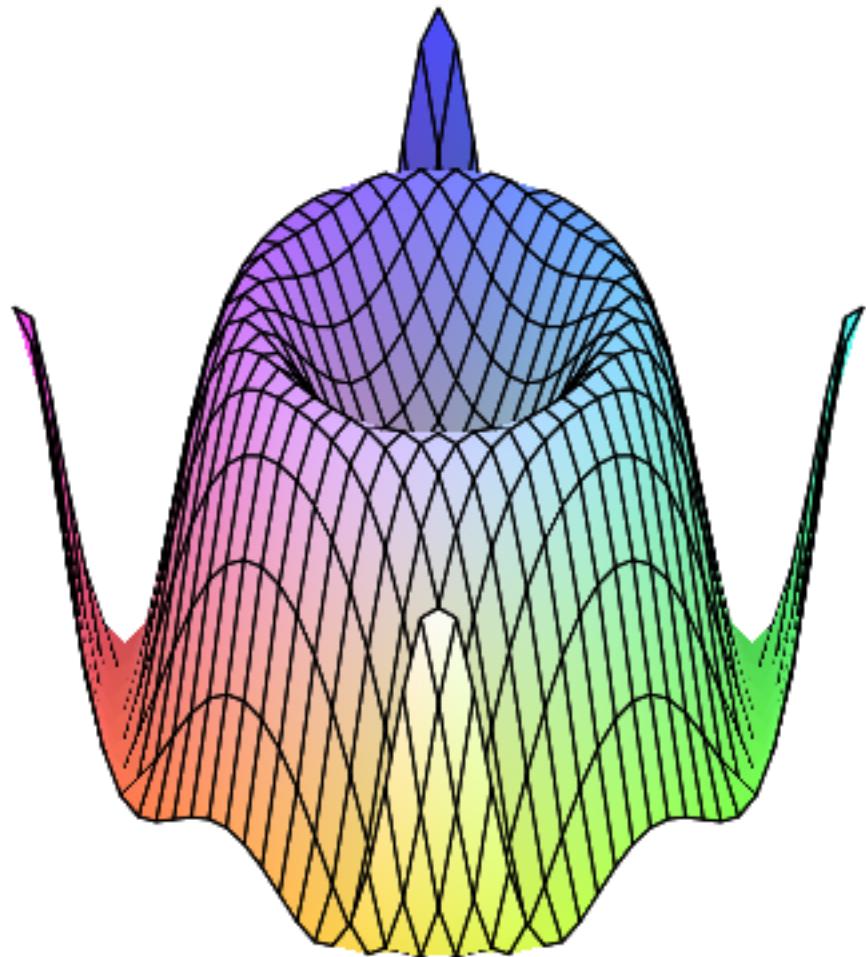


```
> animate(plot, [[sin(t), sin(t)*exp(-(1/5)*t)], t = 0 .. x],  
x = 0 .. 6*Pi, frames = 50);
```

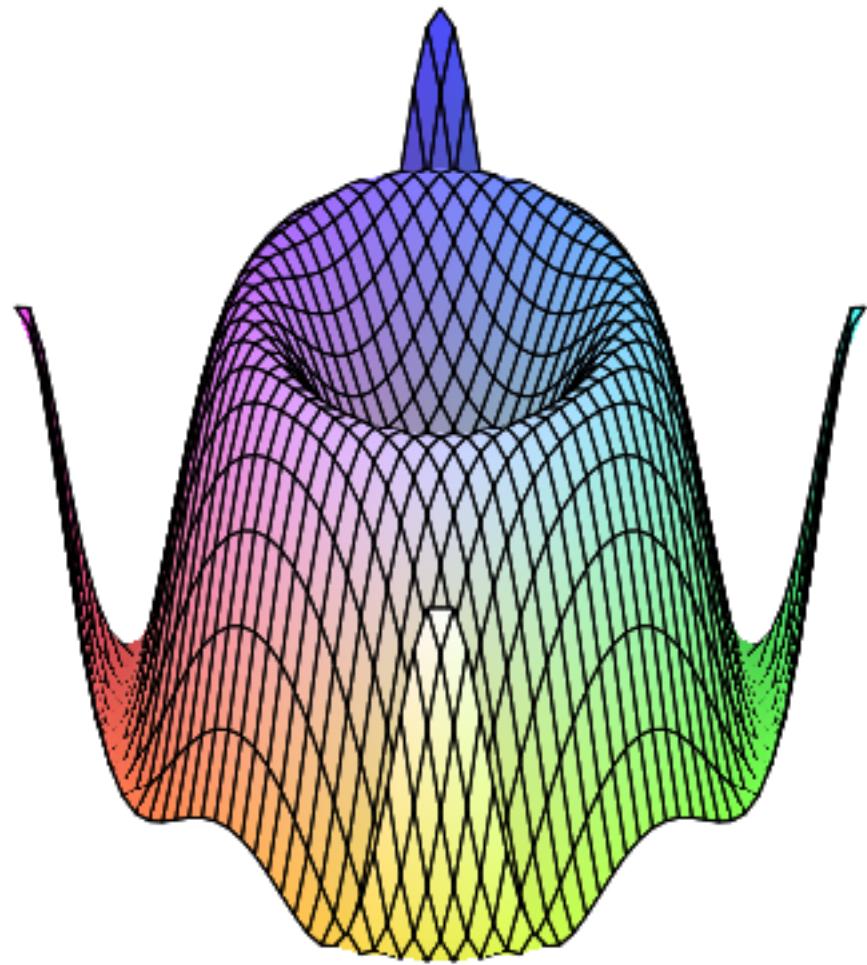


4.3. Gráfico de funções de variáveis

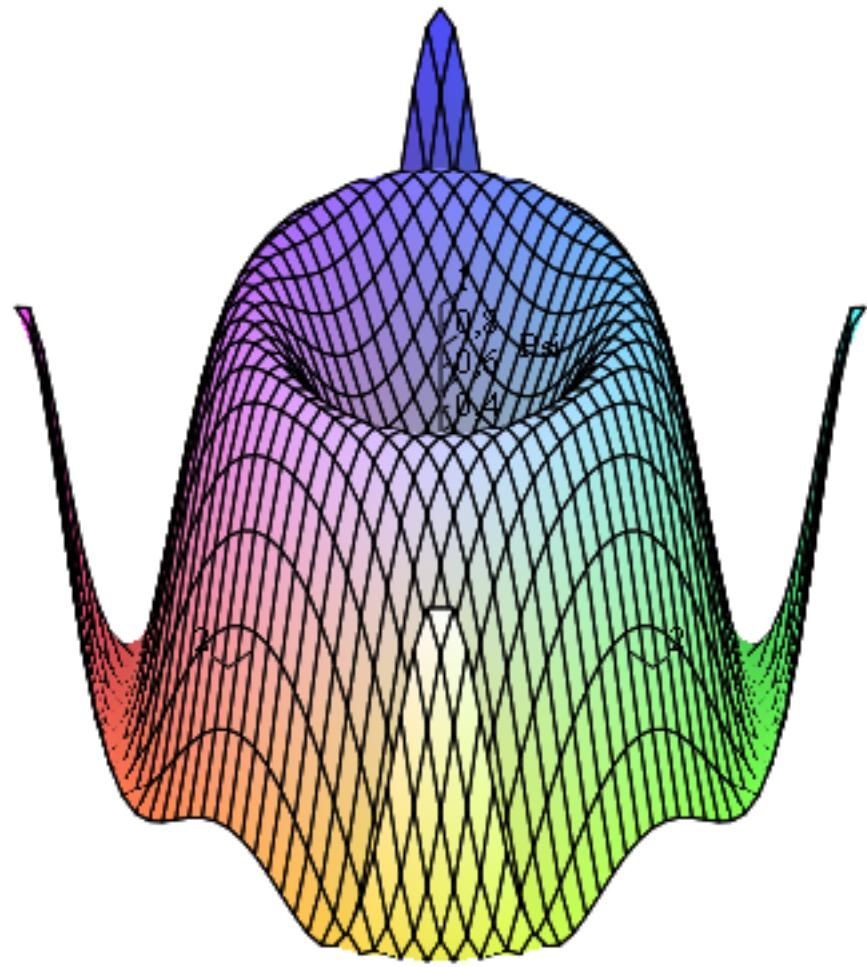
```
> m:=sin(x^2+y^2);  
m := sin( $x^2 + y^2$ )  
(4.6)  
> plot3d(m, x=-2..2, y=-2..2);
```



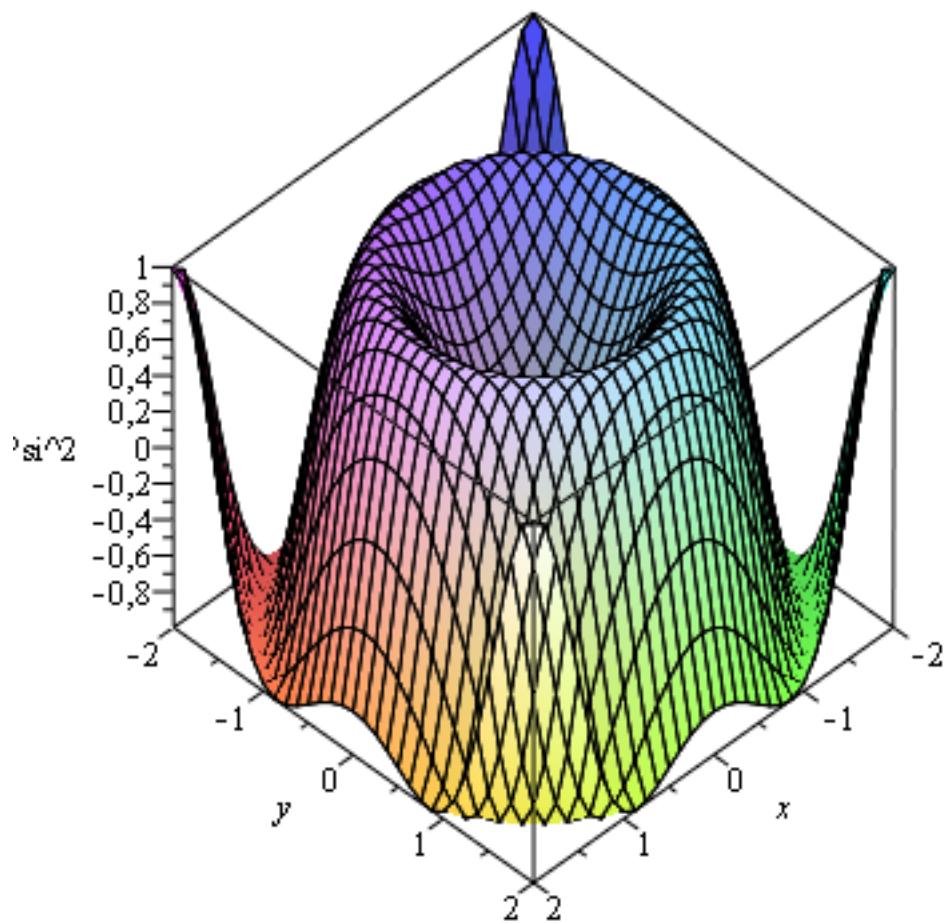
```
> plot3d(m, x=-2..2, y=-2..2, numpoints=1000);
```



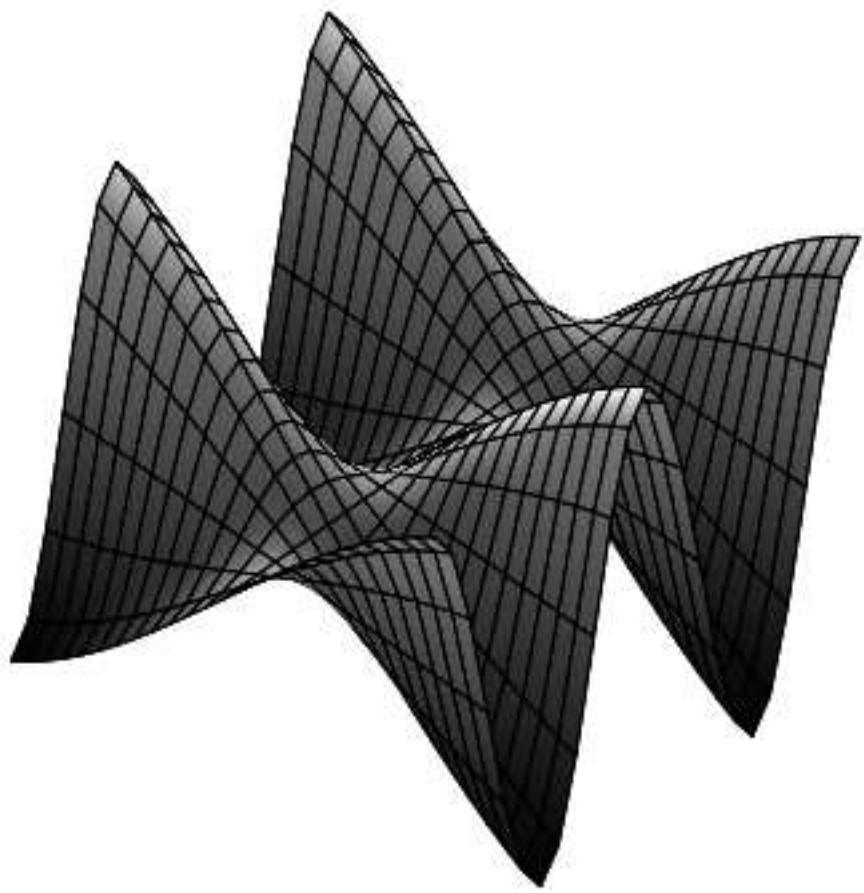
```
> plot3d(m, x=-2..2, y=-2..2, labels=[x,y,"Psi^2"], axes=normal,  
numpoints=1000);
```



```
> plot3d(m, x=-2..2, y=-2..2, labels=[x,y,"Psi^2"], axes=box,  
numpoints=1000);
```

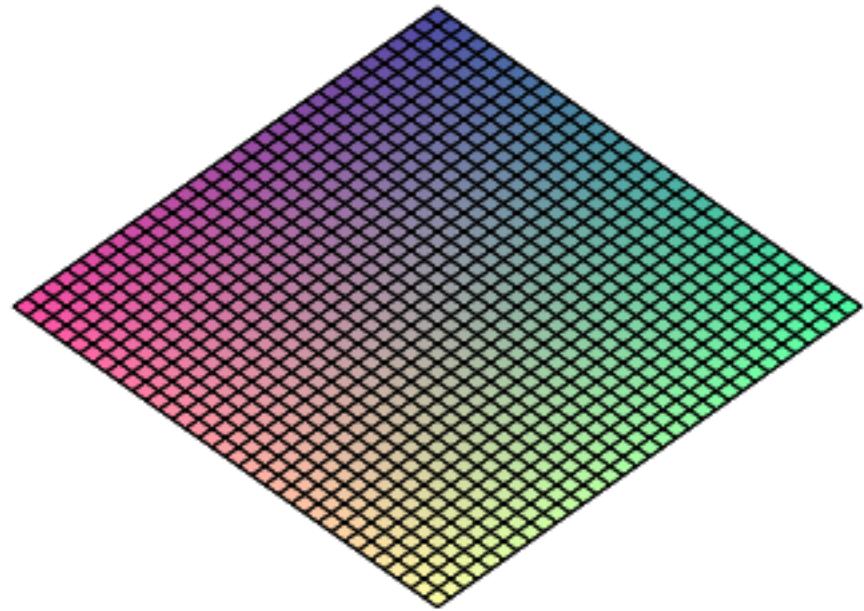


```
> plot3d(cos(x)*sin(y), x = -2*Pi .. 2*Pi, y = -1 .. 1, shading = zgrayscale, lightmodel = light2);
```



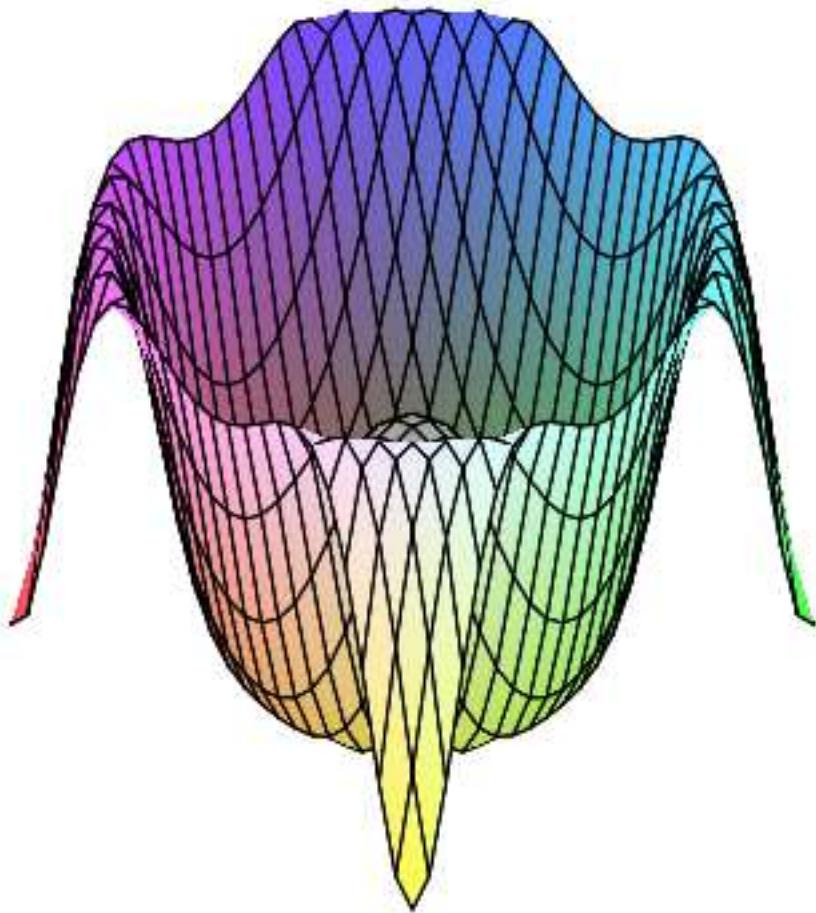
```
> m;

$$\sin(x^2 + y^2)$$
 (4.7)
> animate3d(t*m, x = -2 .. 2, y = -2 .. 2, t = 0 .. 15, numpoints=
1000, frames=50);
```

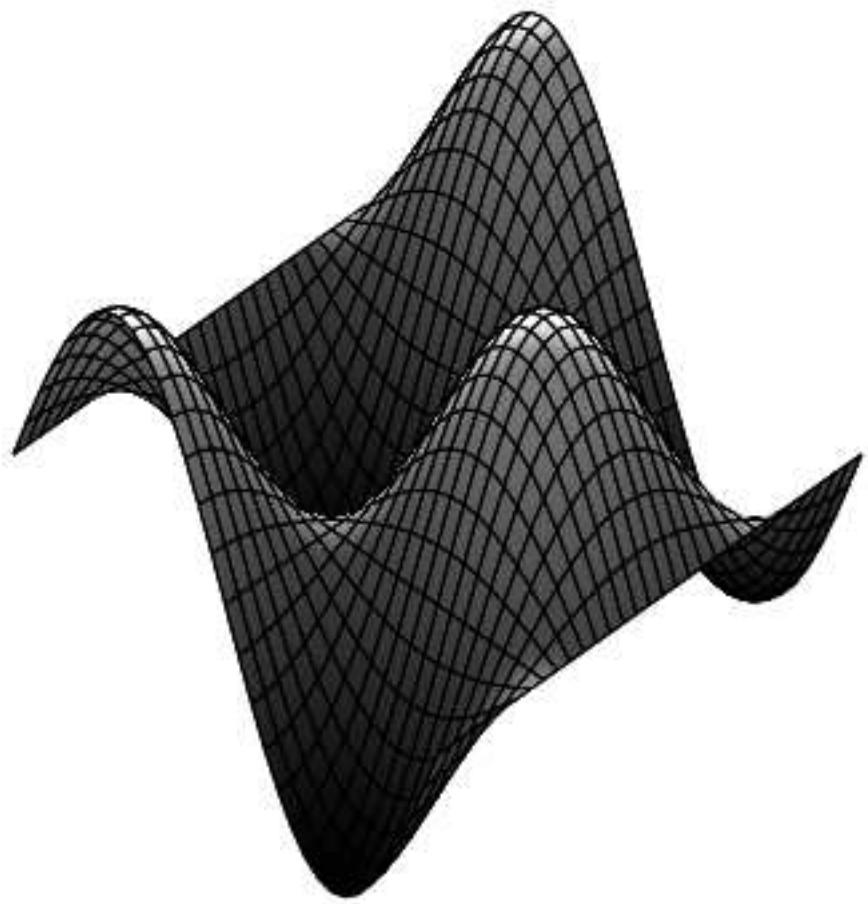


```
> animate(plot3d, [t*m, x = -2 .. 2, y=-2..2], t = -3 .. 3,  
numpoints=1000, trace = 5, frames = 50);
```

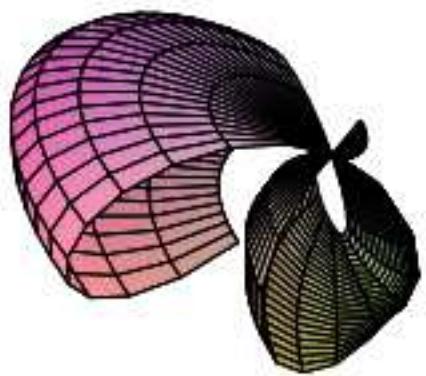
$t = -3.$



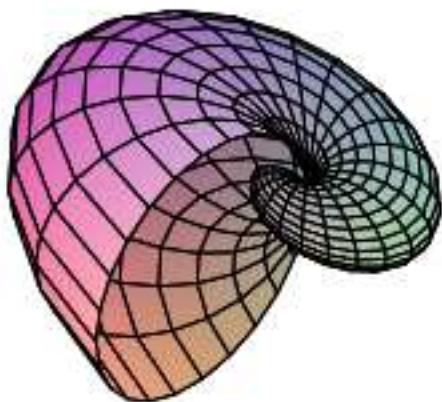
```
> animate3d(cos(t*x)*sin(t*y), x = -Pi .. Pi, y = -Pi .. Pi, t  
= 1 .. 2, numpoints=1000, shading = zgrayscale, lightmodel =  
light2);
```



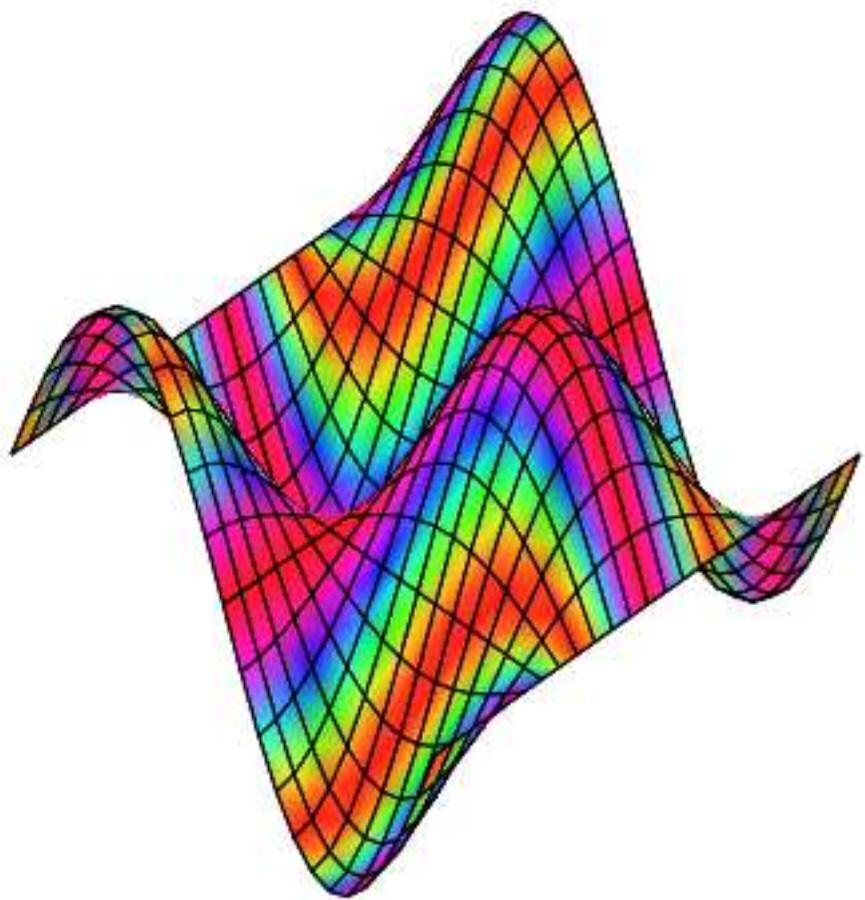
```
> animate3d(x*cos(t*u), x = 1 .. 3, t = 1 .. 4, u = 2 .. 4,  
coords = spherical);
```



```
> animate3d(1.3^x*sin(u*y), x = -1 .. 2*pi, y = 0 .. pi, u = 1 .. 8, coords = spherical);
```



```
> animate3d(cos(t*x)*sin(t*y), x = -Pi .. Pi, y = -Pi .. Pi, t  
= 1 .. 2, color = cos(x*y));
```



[Mais opções
[> ?plot

▼ V. Limites, Derivadas e Integrais

O ferramental do cálculo diferencial e integral faz parte também das rotinas já implementadas ao Maple.

5.1. Limites

$$\begin{aligned} &> \text{Limit}(F(x), x=0); \\ &= \lim_{x \rightarrow 0} F(x) \end{aligned} \tag{5.1}$$

$$\begin{aligned} &> \text{limit}(\sin(x)/x, x=0); \\ &= 1 \end{aligned} \tag{5.2}$$

$$\begin{aligned} &> \text{limit}(1/x, x=0); \\ &= \text{undefined} \end{aligned} \tag{5.3}$$

Nesse caso vemos que o limite de 1/x, quando x->0 não existe! Mas e seus limites laterais?

```
> Limit(1/x, x=0, right);
```

$$\lim_{x \rightarrow 0^+} \frac{1}{x} \quad (5.4)$$

```
> limit(1/x, x=0, right);
```

$$\infty \quad (5.5)$$

```
> Limit(1/x, x=0, left);
```

$$\lim_{x \rightarrow 0^-} \frac{1}{x} \quad (5.6)$$

```
> limit(1/x, x=0, left);
```

$$-\infty \quad (5.7)$$

```
> j:=((x+c)/(x-c))^x;
```

$$j := \left(\frac{x+c}{x-c} \right)^x \quad (5.8)$$

```
> limit(j, x=infinity);
```

$$e^{2c} \quad (5.9)$$

5.2. Derivada

```
> diff(F(x), x);
```

$$\frac{d}{dx} F(x) \quad (5.10)$$

```
> diff(sin(x), x);
```

$$\cos(x) \quad (5.11)$$

```
> diff(sin(x^2), x$6);
```

$$-64 \sin(x^2) x^6 + 480 \cos(x^2) x^4 + 720 \sin(x^2) x^2 - 120 \cos(x^2) \quad (5.12)$$

E quando a função for de duas variáveis?

```
> g:=F(x, y);
```

$$g := F(x, y) \quad (5.13)$$

```
> diff(g, x);
```

$$\frac{\partial}{\partial x} F(x, y) \quad (5.14)$$

```
> diff(tan(y/x), x);
```

$$-\frac{\left(1 + \tan\left(\frac{y}{x}\right)^2\right) y}{x^2} \quad (5.15)$$

```
> diff(tan(y/x), y);
```

$$\frac{1 + \tan\left(\frac{y}{x}\right)^2}{x} \quad (5.16)$$

5.3. Aplicações à Gráficos

Podemos ilustrar o uso destas ferramentas na construção do gráfico de uma função. Por simplicidade consideraremos uma função de uma variável.

```
> f:=1/3*x^3-6/2*x^2+5*x-7/3;
```

$$f := \frac{1}{3}x^3 - 3x^2 + 5x - \frac{7}{3}$$
 (5.17)

Trata-se de um polinômio. Logo, o domínio de f são os reais. Onde que a curva corta o eixo y ?

```
> y0:=subs(x=0, f);
```

$$y0 := -\frac{7}{3}$$
 (5.18)

>

Onde a curva corta o eixo x ?

```
> raizes:=[solve(f=0, x)];
```

$$raizes := [7, 1, 1]$$
 (5.19)

Checando os resultados.

```
> P1:=(op(1,raizes), subs(x=op(1,raizes), f));
```

$$P1 := 7, 0$$
 (5.20)

```
> P2:=(op(2,raizes), subs(x=op(2,raizes), f));
```

$$P2 := 1, 0$$
 (5.21)

Determinando os intervalos de crescimento e decrescimento da função

```
> f1:=diff(f, x);
```

$$f1 := x^2 - 6x + 5$$
 (5.22)

```
> solve(f1>0, x);
```

$$\text{RealRange}(-\infty, \text{Open}(1)), \text{RealRange}(\text{Open}(5), \infty)$$
 (5.23)

>

Vemos então que f é crescente no intervalo aberto de $] -\infty, 1[\cup]5, \infty[$. Consequentemente é decrescente no intervalo $[1, 5[$. O sinal da concavidade da curva será dada pela derivada a segunda.

```
> f2:=diff(f1, x);
```

$$f2 := 2x - 6$$
 (5.24)

```
> solve(f2>0, x);
```

$$\text{RealRange}(\text{Open}(3), \infty)$$
 (5.25)

Pontos de Mínimo, Máximo e Inflexão

```
> pontos:=[solve(f1=0, x)];
```

$$pontos := [5, 1]$$
 (5.26)

```
> minimo:=subs(x=op(1,pontos), f2);
```

$$minimo := 4$$
 (5.27)

```

> ponto_minimo:=[op(1,pontos),evalf(subs(x=op(1,pontos),f))];
      ponto_minimo := [5, -10.66666667]                                (5.28)

> maximo:=subs(x=op(2,pontos),f2);
      maximo := -4                                                 (5.29)

> ponto_maximo:=[op(2,pontos),evalf(subs(x=op(2,pontos),f))];
      ponto_maximo := [1, 0.]                                         (5.30)

> inflexao:=solve(f2=0,x);
      inflexao := 3                                              (5.31)

> ponto_inflexao:=[inflexao,evalf(subs(x=inflexao,f))];
      ponto_inflexao := [3, -5.333333333]                           (5.32)

```

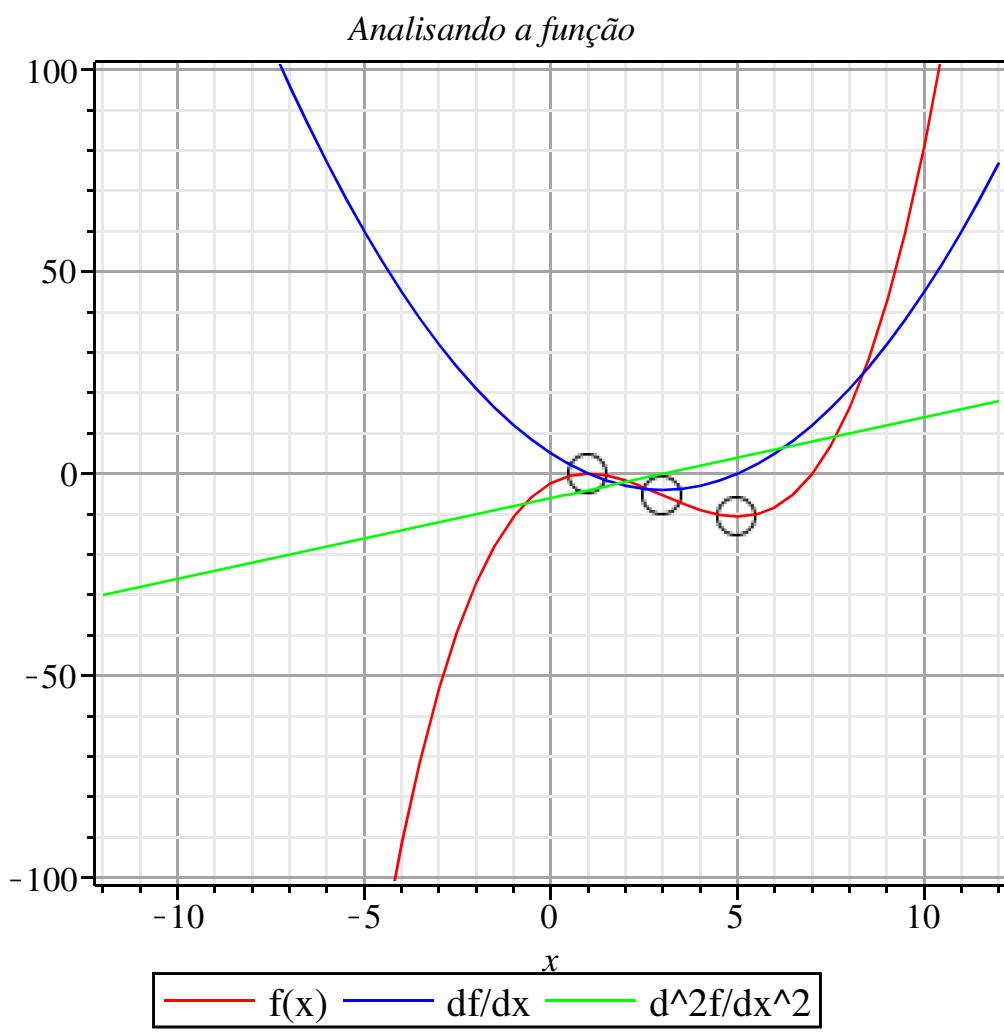
Resumindo

```

> ponto_minimo;evalf(ponto_maximo);evalf(ponto_inflexao);
      [5, -10.66666667]
      [1., 0.]
      [3., -5.333333333]                                         (5.33)

> macro(skyblue = COLOR(RGB, .1960, .6000, .8000)):
> graf1:=pointplot([ponto_minimo,ponto_maximo,ponto_inflexao],
gridlines = true,style=point,symbol = circle,symbolsize=30,
axes=box,color=black,labels=[x,""]);
> graf2:=plot([f,f1,f2],x=-12..12,-100..100,gridlines = true,
color=[red,blue,green],labels=[x,"y(x)"],legend = ["f(x)",
"df/dx","d^2f/dx^2"],title='Analizando a função'):
> display([graf1,graf2]);

```



5.5. Integrais

Pode ser entendido como o processo inverso da derivada.

Integrais indefinidas

$$> \text{Int}(F(x), x); \quad \int F(x) \, dx \quad (5.34)$$

Integrais definidas

$$> \text{Int}(F(x), x=a..b); \quad \int_a^b F(x) \, dx \quad (5.35)$$

Algumas Referências

[1] http://deeke.org/prog_maple.pdf

└ [2] <http://www.edipucrs.com.br/erematsul/minicursos/explorandorecursos.pdf>